



Table of Contents

1. PURPOSE OF PROCEDURE.....2	4. VALIDATION9
2. SEAKEEPING EXPERIMENTS.....2	4.1 Uncertainty Analysis9
2.1 Model Size2	4.2 Benchmark Tests9
2.2 Model Completeness.....3	5. REFERENCES10
2.3 Model Weight Distribution.....3	APPENDIX A10
2.4 Guidance System4	A.1 BACKGROUND TO ISO-GUM.....10
2.5 Free Running Tests.....4	A.1.1 Type A uncertainty11
2.6 Measurement of Wave Loads4	A.1.2 Type B uncertainty.....11
2.7 Measurement of Added Resistance..4	A.1.3 Standard uncertainty11
2.8 Measurement of Impact Loads.....4	A.1.4 Combined uncertainty12
2.9 Parameters to be Measured5	A.1.5 Expanded uncertainty.....12
2.10 Headings5	A.2 SOURCES OF UNCERTAINTY12
2.11 Regular Waves5	A.2.1 Type A uncertainty12
2.12 Transient Waves6	A.2.2 Type B uncertainty.....12
2.13 Irregular Waves.....6	Data presentation18
2.14 Data Presentation7	A.2.3 Example.....20
3. PARAMETERS8	A.2.4 Summary.....20
3.1 Parameters to be Considered.....8	
3.2 Recommendations of ITTC for Parameters8	

Updated / Edited by	Approved
26 th ITTC Seakeeping Committee	26 th ITTC
Date 04/2011	Date 09/2011

Seakeeping Experiments

1. PURPOSE OF PROCEDURE

This procedure outlines the recommended state-of-the-art practice of model seakeeping experiments for the evaluation of ship hull performance in predefined operational and environmental conditions.

The procedure describes requirements relevant to the selection of model size, completeness of its geometry, ballasting and mass distribution and possible model configurations. It provides recommendations for model response data measurements, and operational and environment parameters that should be included in the test plan.

The procedure also outlines the recommended approach to data analysis and presentation formats as well as the preferred approach to uncertainty analysis including theoretical background and practical examples.

2. SEAKEEPING EXPERIMENTS

2.1 Model Size

The size of the model should be such that tank wall interference is avoided for the range of wave frequencies and model speeds to be tested. Figure 1 and Table 1 give, in dimensionless form, a relationship between model length L_M tank breadth B_T , Froude number Fr and the highest wave frequency ω at which interference effects may occur in head waves.

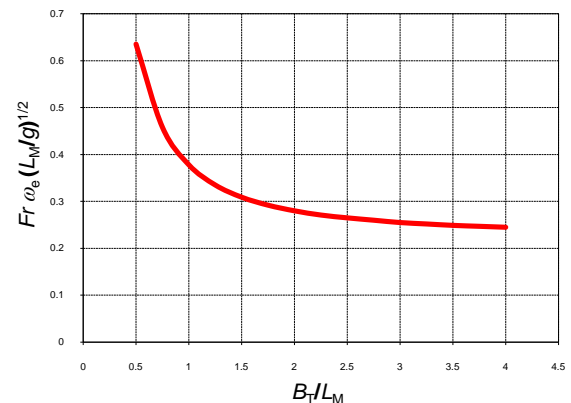


Figure 1. Maximum frequency at which tank interference occurs in head waves

B_T/L_M	$Fr \cdot \omega \sqrt{L_M / g}$
0.50	0.635
0.75	0.458
1.00	0.378
1.25	0.335
1.50	0.309
1.75	0.292
2.00	0.280
2.25	0.271
2.50	0.265
2.75	0.260
3.00	0.255
3.25	0.252
3.50	0.249
3.75	0.247
4.00	0.245

Table 1. Maximum frequency at which tank interference occurs in head waves

Those calculations are made by estimating the potential generated by a source with

harmonic strength. Calculations using the unified-slender ship theory were made by Kashiwagi & Ohkusu (1991).

Figure 2 shows where tank-wall effects are expected for a prolate spheroid of beam - length ratio 1/8. With $K = \omega^2/g$. The dotted lines in Figure 2 show the results of Figure 1.

Non published work of Fernandez shows that the finite depth must be taken into account in tank-wall effects for:

$$Fr \cdot \omega_e \sqrt{L_M} / g \leq 1/2$$

with ω_e , the encounter circular frequency.

These estimations use calculations of the potential generated by a source with harmonic strength in finite depth. Figure 3 shows results in the same format as Figure 1.

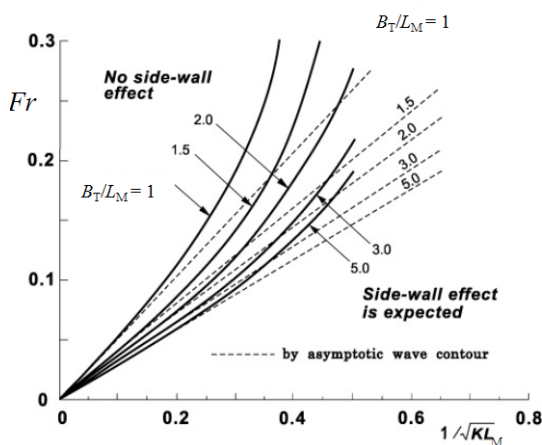


Figure 2. Estimation of tank-wall effects using unified slender theory.

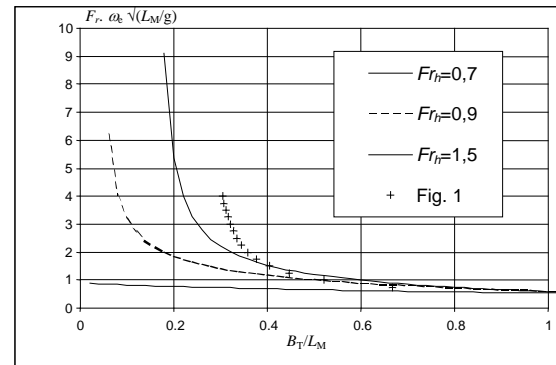


Figure 3. Maximum frequency at which tank interference occurs in head waves and finite depth.

2.2 Model Completeness


It is desirable that the model is complete up to the uppermost weather deck, including forecastle and bulwarks. A more complete modelling of deck fittings, deck houses and freeing ports may be necessary if parameters such as deck wetness are to be measured.

All appendages should be fitted, and the report should state which appendages were fitted during the experiments.

2.3 Model Weight Distribution

If bending moments, shears, and torsion experienced by the model in waves are to be measured, the longitudinal and transverse distributions of mass must be reproduced as correct as possible, and must be correctly reported. In other cases, only the radii of gyration need to be simulated. For tests in head or following waves with a model restrained in rolling, it is not necessary to simulate the transverse weight distribution.

If the longitudinal radii of gyration for pitch or yaw are unknown, a value of 0.25 L_{PP} should be used. If the transverse radius of

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 4 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

gyration is unknown, a value between $0.35B$ and $0.40B$, depending on the ship type, should be used. (These values are those without including the effect of added mass).

For experiments during which rolling is not restrained, the metacentric height should be simulated. If the vertical position of the centre of gravity is unknown, it should be established and reported. As an alternative to ballasting the model to a specified transverse radius of gyration, the natural period of rolling of the full-scale ship may be simulated.

When measuring loads on catamarans, cross products of inertia have to be taken into account.

2.4 Guidance System

The guidance system should be such as to impose the minimum restraint on the motions of the model. It is desirable that even in head or following waves the model should have the freedom to roll. In oblique waves, care also must be taken to minimize restraint on sway and yaw motions.

The report should describe in detail the characteristics of the guidance system.

2.5 Free Running Tests

Testing with a free running self-propelled model is preferred method for seakeeping experiments. Experiments are usually run at predefined speeds. Preliminary tests can be necessary to adjust the rpm in order to reach the desired speed in waves. Alternatively, the rpm can be automatically controlled.

The autopilot parameters should be chosen to reflect a realistic full-scale response of the model. These parameters should be reported.

Care has to be taken to reduce any influence of cables or safety lines on the model's motions to a minimum.

It is recommended that rpm and rudder action are continuously recorded.

2.6 Measurement of Wave Loads

Segmented models for measuring global loads should have natural frequencies far from the wave frequency range. These frequencies have to be measured and documented.

The mass, COG and inertias of each separate segment have to be known (measured or calculated) and reported. Preferably, the loads due to the mass and inertia of the segments should be separated from the total loads during analysis to get the wave-induced loads.


For global bending moment, sagging and hogging loads should be reported.

2.7 Measurement of Added Resistance

The power increase in waves can be measured directly with free running models or determined indirectly from measurements of added resistance on captive models (refer to ITTC recommended procedure 7.5-02-06-0.1).

2.8 Measurement of Impact Loads

The guidelines for the measurement of impact loads are presented in procedure 7.5-02-07-02.3 Loads and Responses Seakeeping, Experiments on Rarely Occurring Events.

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 5 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

2.9 Parameters to be Measured

The hull motions, motion rates and accelerations in the desired degrees of freedom should be measured.

Wave height measurements should be made with a probe mounted close to the model, but not causing interference. The probe should preferably be fixed to the carriage, but measurements may be made at a fixed point in the tank. In the latter case, the measuring point should be selected in the position where waves are fully formed without being affected by the waves reflected at the wave maker and the tank walls & beaches.

Non-contact probes are preferable for wave measurements moving with the model, especially at high speeds.

The capability to measure the following additional parameters should be provided:

- Relative motion. Measurements of the relative motion between the model and the water surface at points that allow correlation with wave and other motion data.
- Rudder angle. In cases where active rudder control is employed, the rudder control signal and actual rudder angle should be continuously monitored.
- Impact pressures on the hull or on deck at selected locations.
- Still water resistance and added resistance in waves (if not freely running).
- Water on deck.

- Propeller revolutions. Whenever a self-propelled model is used, the shaft revolutions should be recorded.
- Visual records. Tests should be recorded visually, preferably in a way allowing scaling of time.

Additionally, the following parameters may be measured depending on the test requirements:


- It is recommended that propeller torque and thrust be also continuously recorded.
- Encounter (heading) angle. The angle between the mean model heading and the wave direction.
- Leeway (or drift) angle. The angle between the mean model heading and the tangent to the path of *CG*.

2.10 Headings

When performing tests in oblique seas, the range of encounter angles between zero and 180 degrees should be selected in accordance with the stated test objectives. The 180 degrees heading represents head seas.

2.11 Regular Waves

For conventional ship forms, a sufficient number of tests should be carried out at each speed to provide adequate data for a minimum range of wavelengths from at least $0.5 L_{PP}$ to $2.0 L_{PP}$. More tests with closely spaced wavelengths can be necessary to ensure a good definition in the resonance region. Either the ratio of the wave height to L_{PP} or the ratio of wave height to wavelength should be maintained constant. (The recommended

	ITTC – Recommended Procedures and Guidelines		7.5-02 07-02.1 Page 6 of 22	
	Seakeeping Experiments		Effective Date 2011	Revision 04

value of the ratio of wave height to wavelength is around 1/50.)

In determining the motions, it is recommended that the average amplitude and period of at least 10 cycles be obtained. Alternatively, a spectral analysis following the procedures for irregular waves outlined below could be followed to obtain the mean amplitude and period of waves and responses. Guidelines for regular wave data analysis are given in the ITTC Recommended Procedure 7.5-02-07-03.2 “Analysis Procedure for Model Tests in Regular Waves”.

2.12 Transient Waves

The transient wave technique is an experimental technique in which a wave train that contains wave components of all the relevant frequencies is produced in such a way that the component waves reach a certain place in the test tank simultaneously so that a single large wave packet is formed. If a model structure is positioned at the place where the single large wave packet accumulates, response characteristics to regular waves of all the frequencies contained in the wave packet are obtained in one single experiment (provided the linear superposition assumption holds). This technique proves to be very efficient as a standard tool for evaluating RAO's of stationary offshore structures or towed/self propelled ships.

2.13 Irregular Waves

Tests should be carried out in waves corresponding to the sea conditions in which the vessel may be required to operate. In the absence of specific wave spectrum data the ITTC should be used for open ocean and JONSWAP spectrum should be used for


fetch-limited seas. When generating irregular waves in a tank, the input signal to the wave maker should be produced such that the generated waves are non-repeatable.

Irregular wave generation in experimental tanks is subjected to voluntary or involuntary truncation of idealized spectrum as a result of mechanical limits of wave making facilities. The truncation frequency is facility specific and depends on characteristics of the wave maker and model scale selected for the experiment. Selection of too low cut-off frequency affects properties of resultant spectrum and values of target significant wave height $H_{W1/3}$ and modal period T_p . If $n=f_T/f_P$: f_T is truncated frequency and f_P is peak frequency of idealized spectra, the recommended cut-off frequency for most facilities is $n>2$, and preferable n approaching 3.

Data should preferably be digitised before analysis, using sample rates appropriate for the avoidance of aliasing with the individual measured parameters. Care must be taken for the duration of the data acquisition so that enough data are recorded for the objective of the test.

The test duration is represented by total number of waves (encounters) N . The $N=50$ should be taken as a lower limit. Larger values are to be preferred and it is more usual to take $N=100$ as the standard; $N=200$ or above is considered excellent practice. For the following sea case, 30 minutes of equivalent full scale is considered sufficient.

The time interval between test runs is also important and can be tank specific. In most cases 20 minutes between runs is acceptable for a typical facility. The residuary tank

 INTERNATIONAL TOWING TANK CONFERENCE	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 7 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

disturbance of less than 1% of the next target wave height is a valid alternative.

The sample rate in the data acquisition needs to be fast enough in order to achieve sufficient resolution. A sampling rate corresponding to about 4 Hz at full scale is enough for most measurements but much higher rates (in the order of kHz) are necessary to detect peaks of slamming loads.

Energy spectra of waves and relevant responses should be produced through spectral analysis using either the indirect method of Fourier transformation of the autocorrelation function, or the direct method of splitting the record into suitable blocks and subjecting these to Fast Fourier Transform.

In addition to the spectral analysis, statistical analysis should be performed to produce at least the mean, maximum, minimum, and the mean of 1/3 highest values. In the presentation of the results the techniques utilised to smoothen spectral shapes, such as block overlapping, should be documented. When reporting statistics, the number of events and number of encounters should also be reported together with the overall statistics.

For the measurement and analysis of rarely occurring events such as slamming or wetness refer to ITTC recommended procedure 7.5-02-07-02.3.

2.14 Data Presentation

The coordinate system in which data are presented should be defined. Motion components should also be defined. Linear translations and rotations may be presented in non-dimensional form as being divided by wave elevation and wave slope respectively.

Rudder angles may be non-dimensionalized by wave slope or be presented in other appropriate non-dimensional form.


Translations	$\frac{x_{1,2,3}}{\zeta_A}$
Rotations	$\frac{x_{4,5,6}}{\kappa\zeta_A}$

Dimensional presentations can sometimes be more appropriate depending on the objectives of the experiment. Phase angles should be given in degrees and increases in resistance and propulsion parameters should be presented in the non-dimensional form. Accelerations should be made non-dimensional by $L_{PP}/(\zeta g_A)$. It is recommended that the results are plotted to a base of $\omega(L_{PP}/g)^{1/2}$ or $\omega_e(L_{PP}/g)^{1/2}$, although, depending on the objectives of the experiment, other bases such as wavelength - ship length ratio or wavelength may be appropriate. The limit of tank wall interference effects should be indicated on the plots.

For tests in irregular waves, the corresponding wave-energy spectrum should be defined.

When appropriate, performance in irregular waves should be presented in non-dimensional form involving a characteristic wave period or frequency and a characteristic wave height.

The results of statistical analyses may be presented to depict probability of exceedance and as cumulative probability distribution for selected responses.

 INTERNATIONAL TOWING TANK CONFERENCE	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 8 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

Tabular presentation of results is recommended in addition to plots.

3. PARAMETERS

3.1 Parameters to be Considered

The following parameters defining the tests are to be taken into account (as applicable):

- Scale
- Model dimensions
- Ratios of model to tank dimensions
- Hull configuration (lines, appendages, superstructures, ...)
- Loading conditions (displacement and draft)
- Mass distribution (COG, inertias, ...)
- Towing and/or restraining device characteristics (specially DOF)
- Speeds and headings
- Wave characteristics (heights, periods, spectra, dispersions, ...)
- Autopilot control law and gains
- Speed control characteristics
- Run duration
- Number of runs per test condition
- Positions of sensors (accelerometers, relative motion, encountered wave, ...)
- Resonance frequencies for segmented models
- Sampling frequency
- Sensor calibrations and accuracy

3.2 Recommendations of ITTC for Parameters

1975 Performance in irregular waves should be presented in non-dimensional form

involving wave characteristic period and characteristic wave height.

1978 Recommendation for open ocean spectral formulation:

$$S(\omega) = \frac{A}{\omega^5} e^{-B/\omega^4} \quad (1)$$

where

$$A = 173(\zeta_w)_{1/3}^2 / T_1^4$$

$$B = 691 / T_1^4$$

$$T_1 = 2\pi m_0 / m_1$$

1984 Recommendation for long crested limited fetch sea spectral formulation:

$$S_j(\omega) = 155 \frac{(\zeta_w)_{1/3}^2}{T_1^4 \omega^5} \exp\left(-\frac{944}{T_1^4 \omega^4}\right) 3.3^\gamma \quad (2)$$

where:


$$\gamma = \exp\left[-\frac{(0.191\omega T_1 - 1)^2}{2\sigma^2}\right] \quad (3)$$

$$\sigma = \begin{cases} 0.07 & \omega < 5.24 / T_1 \\ 0.09 & \omega > 5.24 / T_1 \end{cases}$$

This formulation can be used with other characteristic periods by use of the following approximate relations:

$$T_1 = 0.924T_{-1} = 0.834T_0 = 1.073T_2$$

Where T_{-1} is the energy average period ($2\pi m_{-1} / m_0$), T_0 is the spectral peak period, T_1 is the average period ($2\pi m_0 / m_1$) and T_2 is the average zero crossing period estimated from the spectrum ($2\pi \sqrt{m_0 / m_2}$).

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 9 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04


4. VALIDATION

4.1 Uncertainty Analysis

The detailed procedure of uncertainty analysis following the principles behind the ISO-GUM is shown in the Appendix A.

4.2 Benchmark Tests

- 1) Seagoing Quality of Ships. (7th ITTC, 1955, pp.247-293). A model of the Todd-Forest Series 60 with $C_B=0.60$. Results from 7 tanks are presented.
 $Fr = 0, 0.18, 0.21, 0.24, 0.27$ and 0.30
 $L_{pp}/H = 36, 48, 60, 72$
 $\lambda/_{pp} = 0.75, 1.0, 1.25, 1.5$
- 2) Comparative Tests at Three Experimental Establishments with the Same Model. (11th ITTC, 1966, pp.332-342)
 British Towing Tank Panel: A 10 ft. Fibre-glass model of the S.S. Cairndhu.
 A series of experiments on a ship model in regular waves using different test techniques.
 Data obtained in irregular and transient waves and some result predicted by the theory (based on Korvin Kroukovsky's work and employing the added mass and damping coefficients calculated by Grim).
- 3) Full Scale Destroyer Motion Tests in Head Seas (11th ITTC, 1966, pp.342-350).
 Comparison among motion response obtained from full scale tests, model experiments and computer calculations for destroyer H.M. "Groningen" of the Royal Netherlands Navy
- 4) Experiments in Head Seas For Series 60.
 - 4-1) Comparative Tests of a Series 60 Ship Model in Regular Waves (11th ITTC, 1966, pp.411-415). Series 60 with $C_B=0.60$.
 - 4-2) Experiments on Heaving and Pitching Motions of a Ship Model in Regular Longitudinal Waves (11th ITTC, 1966, pp.415-418). Series 60 with $C_B=0.60$.
 - 4-3) Experiments on the Series 60 with $C_B=0.60$ and 0.70 Ship Models in Regular Head Waves (11th ITTC, 1966, pp.418-420)
 - 4-4) Comparison of Measured Ship Motions and Thrust Increase of Series 60 Ship Models in Regular Head Waves (11th ITTC, 1966, pp. 420-426).
 - 4-5) Estimation of Ship Behaviour at Sea from Limited Observation (11th ITTC, 1966, pp.426-428)
- 5) Analysis of the S-175 Comparative Study (17th ITTC, 1984, pp.503-511).
- 6) S-175 Comparative Model Experiments (18th ITTC, 1987, pp.415-427)
- 7) Rare Events (19th ITTC, 1990, pp.434-442). Comparison of results from tests at 12 establishments in irregular waves. Absolute and relative motions. S-175 at $Fr=0.275$.
- 8) The ITTC Database of Seakeeping Experiments (20th ITTC, 1993, pp.449-451).
- 8-1) Tests of Two Dimensional Models. Added mass, damping and wave exciting forces

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 10 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

8-2) Tests of a Wigley hull form. Added masses, damping, exciting forces and seakeeping motions and loads.

8-3) Tests for S-175.

9) The ITTC Database of Seakeeping Experiments (21st ITTC, 1996, pp.43). S-175, high speed marine vehicle

10) Numerical and Experimental Investigation to Evaluate Wave-Induced Global Design Loads for Fast Ships (Schellin et al, 2003). Two segmented models of fast ships (Fr up to 0.63) were tested in head seas. Motions and global loads are reported. The results are compared with several non-linear codes.

5. REFERENCES

Kashiwagi, N. and Ohkusu, M., 1991, “A new theory for side-wall interference effects on forward-speed radiation and diffraction forces”, Schiffstechnik, vol. 38.

Schellin, T.E. et al, 2003, “Numerical and Experimental Investigation to Evaluate Wave-Induced Global Design Loads for Fast Ships”, Transactions SNAME, vol. 111, pp. 437-461.

ISO/IEC 2008, “Guide 98-3, Uncertainty of measurements – Part 3: Guide to the expression of uncertainty in measurements (GUM: 1995)”, 2008 Switzerland.

ITTC (2008), “Discussion to the 25th ITTC Seakeeping Committee by Joe Longo, Claus Simonsen, Fred Stern”, Proceeding of 25th ITTC-Volume III, September 2008, Fukuoka, Japan, pp. 697-701.


Kishev, R., (1998), “Uncertainty Analysis of Dynamic Model tests and Its Application to Capsizing Simulation in Waves”, Proceedings of International Workshop on Modeling of Ocean Environments in Waves & Current Basin, February, 1998, Taejon, Korea.

Yum, D.J., Lee, H.Y. and Lee, C.M., 1993. Uncertainty Analysis for Seakeeping Model Tests. *Journal of the Society of Naval Architects of Korea*, 30 (3): 75-89.

Appendix A

A.1 BACKGROUND TO ISO-GUM

The recommendation of the ITTC 2008 was to adopt the ISO-GUM (International Organization for Standardization, Guide to the Expression of Uncertainty in Measurements, ISO 1995) approach to conducting uncertainty analysis of experimental results. The ISO GUM recognises two groups of uncertainty, type A and type B, which are based on way in which the uncertainty is evaluated. Type A represents the random category of uncertainty evaluated by using statistical analysis of repeated measurements of, nominally, the same observation; type B components are estimated by means other than repeated observations. The “other means” may include previous measurements, past experience or general knowledge, handbook information, manufacturer specification or data provided as a certificate. A detailed approach to uncertainty analysis in experimental hydrodynamics can be found in ITTC procedure 7.5-02-01-01.

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 11 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

A.1.1 Type A uncertainty

The fundamental form of uncertainty associated with a measurement is type A, $u(\bar{q})$, which can be expressed as a standard deviation. Type A uncertainty is typically based upon the analysis of repeated measurements which characterizes the randomness of the experimental process. The most common approach to estimating type A uncertainty is by undertaking end-to-end multiple repeated runs; care should be taken to ensure that as many factors as possible that affect repeatability of experiment are accounted for. Numbers of repeats should be as large as practicable in order to minimize type A uncertainty; however 10 repeats indicates good experimental practice. However, in most seakeeping tests it is not practicable to carry out multiple repeats for all experimental conditions. It may be more feasible to select only characteristic or unique test conditions (due to environment and/or operations) for which repeat runs should be undertaken and reported. Historic database of information on Type A uncertainty could be created (occasionally confirmed) and used to report uncertainty for routine experiments.

A.1.2 Type B uncertainty

Type B uncertainty, characterised as u_i^2 or u_i , may be considered as an approximation to the experimental variance or standard deviation respectively. In the same way as type A uncertainty, type B is assumed to be equal to the standard deviation u_i . Typically type B uncertainty can be estimated from

quoted values of uncertainty, assumed statistical distribution of the parameters and factors depending on a level of confidence in the measurement. Generally, the experimenter can assume that the type B uncertainty is normally distributed around some mean, however, in some specific cases it may be pertinent to consider alternatives such as triangular or rectangular distributions. For type B uncertainty that are assumed to be normally distributed Table A1 shows the factors that need to be applied for some examples of confidence.

Confidence Level [%]	Factor
50	0.6757
68.27	1.
90	1.645
95	1.96
99	2.576
99.73	3


Table A1. Confidence factors for normally distributed type B uncertainties

For example, this means that, statistically, you can have 95% confidence that a measurement lies within a value of $\pm 1.96 u_i$.

A.1.3 Standard uncertainty

The standard uncertainty, $u(y)$, in a measured value is the summation of type A and all of the type B uncertainties and can be calculated using the uncertainty propagation formula:

$$u(y) = \left(\sum_{i=1}^N u^2(\bar{q}) + \sum_{j=1}^K u_j^2 \right)^{\frac{1}{2}} \quad (\text{A1})$$

 INTERNATIONAL TOWING TANK CONFERENCE	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 12 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

A.1.4 Combined uncertainty

A further step is required when result of an experiment is derived from values of a number of other measurement variables (x_i). The most common situation where this is undertaken in seakeeping experiments is when the results are non-dimensionalised. In this case, the combined uncertainty $u_c(y)$ is applied to express uncertainty in the derived result.

$$u_c(y) = \left(\sum_{i=1}^N \left(\frac{\partial f}{\partial x_i} \right)^2 u^2(x_i) + 2 \sum_{i=1}^{N-1} \sum_{j=i+1}^N \frac{\partial f}{\partial x_i} \frac{\partial f}{\partial x_j} u(x_i, x_j) \right)^{\frac{1}{2}} \quad (\text{A2})$$

The second term in the combined uncertainty formula represents the cross correlation between two or more variables. These terms are zero when variables are considered to be independent. The $\frac{\partial f}{\partial x_i}$ term

is the partial derivative with respect to variable x_i , also known as the sensitivity coefficient and $u(x_i)$ is the standard uncertainty of variable x_i .

A.1.5 Expanded uncertainty

When presenting the results of experiments along with interval expressing some level of confidence in that measurement then the expanded uncertainty U is applied.

$$U = k u_c(y) \quad (\text{A3})$$

Where, k represents the confidence factor, and the result of the measurement can be interpreted as $y-U \leq Y \leq y+U$.

So, Y can be interpreted as the best estimate that the resultant measurement lies

within the range $y-U$ and $y+U$; the value of U is defined by k . For cases where the uncertainty can be assumed to be normally distributed the confidence factors presented in Table 1 can be used. For example, a value $k=2.576$ value gives confidence level of 99%.

A.2 SOURCES OF UNCERTAINTY


A typical requirement from a seakeeping experiment is to obtain the basic rigid body motions (surge, sway, heave, roll, pitch and yaw), accelerations and relative motions at specific locations, waves, model speed, and propulsion and steering systems characteristics (propeller revolutions, rudder angle). All of these measured parameters are subjected to type A and type B uncertainties that need to be estimated as a part of the experimentation procedure.

A.2.1 Type A uncertainty

Type A uncertainty is evaluated by taking repeated measurements of the same experimental condition (recommended number of repeated runs is 10). Since repeating the entire set of test runs in a seakeeping experiment makes the programme prohibitively long (and hence expensive) it is recommended that only a few selected representative test conditions should be repeated to obtain some understanding of the type A uncertainty.

A.2.2 Type B uncertainty

There are elemental type B uncertainties that are an inherent part of each sensor, its calibration, the data acquisition system, processing and analysis.

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 13 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

All of these elemental type B uncertainties should be accounted for, using same type of formulation in equation A2, to determine the type B uncertainty for each measured parameter.

Sensors.

Measurements of the rigid body motions of the model, accelerations and relative motions, propulsion and control parameters are usually primary requirements of seakeeping experiments. Specifications provided by the manufacturers of the sensors used in experiments, coupled with past experience in the use of such sensors, allows an estimation of the relevant type B uncertainty to be made. The manufacturer may present sensor uncertainty information as standard deviations (or multiples of) or as an expanded uncertainty with a specified confidence level. This information can be translated to a standard deviation and can be used to obtain the standard type B uncertainty for that particular element. For example, a sensor specification stating that roll and pitch angles are measured to a dynamic accuracy of 0.5 degrees rms can be interpreted as a 0.5 degree standard uncertainty in roll and pitch. In most cases individual sources of uncertainty need to be identified from available specification documents and the uncertainty propagation formula should be used to obtain the standard uncertainty given in (A1).

Elemental sources of uncertainty that are usually identified from manufacturer's specification may include: non-linearity, hysteresis, non-repeatability, zero offset drift, span temperature coefficient, and resolution.

Calibrations.

Before used in experiments, all instruments need to be calibrated; either bench or in-situ calibration or else factory calibration constants are applied.

Calibration characterises an instrument's uncertainty but does not eliminate it; indeed, the calibration process itself is subject to uncertainties. Generally, a system level, in-situ end-to-end calibration is advisable that includes as many of the possible elemental sources of uncertainty in the calibration procedure. A few, additional, elemental sources of uncertainty need to be considered when estimating uncertainty: calibration standards (quality of calibration specimens or injection source), calibration curve fitting, calibration set up (misalignments) and A/D conversion.

The uncertainty associated with the quality of the calibration standard and calibration device/jig set-up misalignments can be estimated from the manufacturer's specification. Uncertainty due to calibration standards B_{CS} can be estimated using:

$$B_{CS} = \sqrt{\sum (A_{CG} \cdot W_i)^2} \quad (A4)$$


A_{CG} accuracy of calibration specimens; e.g., weight, distance, angle...

W_i physical values of calibration points; weight, distance, angle...

The uncertainty associated with misalignment in the calibration set-up uncertainty can be evaluated from:

$$B_{CM} = \sum (W(1 - \cos \alpha_j)) \quad (A5)$$

W nominal measurement value

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 14 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

α angle of misalignment in relevant plane.

The curve fitting uncertainty can be estimated using the standard error of estimation (SEE) formula:

$$SEE = \left[\frac{1}{n(n-1)} \sum_{k=1}^n (y_n - y_{LS,k})^2 \right]^{1/2} \quad (A6)$$

In the formula n is the number of calibration samples, y_n is calibration data point, and $y_{LS,n}$ is fitted value. In most cases $n \geq 7$ is recommended. It can be assumed that the SEE value is approximately equal to the standard uncertainty.

Generally, the majority of data acquisition systems that are currently in use employ a 16-bit (or better) analogue to digital (A/D) converters. However, some specific equipment may still use 12-bit A/Ds to acquire model data.

The type B uncertainty associated with the A/D conversion is equivalent to $\frac{1}{2}$ the resultant resolution and can be estimated from:

$$B_{CAD} = \frac{1}{2} \frac{TotalVoltageRange}{A/Dbits} \cdot CalibrationFactor \quad (A7)$$

The *TotalVoltageRange* is typically equal to either ± 10 Volts or ± 5 Volts; the *A/Dbits* value is 2^{16} or 2^{12} for 16 and 12 bit convertors respectively, the *CalibrationFactor* is a calibration constant that translates voltage to physical units. Typically, uncertainty due to resolution of 16-bit system would be negligible, but for 12-bit system it could be significant for higher precision instrument.


In the case of measuring instruments that are provided with manufacturer calibration data (most modern digital instruments) calibration standards are reflecting standards of high precision source (voltage) that, normally, is expected to be considerably more accurate than accuracy that can be achieved in a physical bench calibration.

It is advisable, if practical, to conduct in-situ end-to-end (with all model systems being active) calibration of the sensors that are to be used in the experiment. In such a situation, the calibration process should include all or most elemental type B uncertainty sources, which are difficult to estimate individually. However, for in-situ calibration they don't have to be individually identified and estimated.

This approach does not exclude the need for uncertainty analyses due to calibration standards, set up, curve fitting and other related sources of uncertainty but hopefully overall simplifies the procedure.

Data Acquisition System.

In case when in-situ end-to-end calibration procedure is applied all data acquisition system elemental error sources are included in the process except for noise due to variation in surrounding external environment (temperature, humidity) and other used devices (propulsion motor). Good testing practice requires screening of all noise sources, but when this appears to be difficult those effects should be estimated.

	ITTC – Recommended Procedures and Guidelines	7.5-02 07-02.1 Page 15 of 22	
	Seakeeping Experiments	Effective Date 2011	Revision 04

Data processing.

Type B uncertainty due to data reduction and analysis should include any uncertainty related to data integration, differentiation, filtering and other methods of data manipulation. It can be evaluated based on previous experience of working with data processing systems. Uncertainty due to any data reduction associated with the calculation of basic statistics (mean, standard deviation) should be considered negligible, however, for more complex data manipulations resultant uncertainty may need to be considered. These uncertainties can be estimated by using the same data manipulation process with a known signal with known analytical solution (sin or cosine) comparing the processed and analytic outputs.

Data analysis.

Model speed and heading. - Model speed uncertainty is subjected to both type A and type B uncertainties. The type A component is calculated using equation for the standard uncertainty (the uncertainty propagation formulae A1) and the combined uncertainty (A2). The Type B uncertainty component is dependent upon the method in which the model speed is obtained. If, during the experiments, the model is attached to or follows the carriage and speed of the model can be assumed to be equal to the speed of the carriage, then the method presented in ITTC 2008 7.5-02.07-02.1 and that suggested by Fogash (1992) can be used.

Under the assumption that model speed, v , through the water is equal to the speed of towing carriage, the model speed is determined from

$$v = \frac{n/5000\pi D}{t} = \frac{f\pi D}{5000} \quad (\text{A8})$$

where D (m) is the diameter of carriage wheel and n is the number of light pulses sensed by the photo coupler during the time period t . The 5000 number is facility specific and indicates number of pulses per single turn of carriage wheel. The measured quantities and error sources for the estimation of model speed and error limit are the diameter of carriage wheel and the pulse frequency f ($= n/t$).

The combined uncertainty becomes, in this case:

$$u_c(v) = \left[\left(\frac{\partial v}{\partial f} \right)^2 u^2(f) + \left(\frac{\partial v}{\partial D} \right)^2 u^2(D) \right]^{\frac{1}{2}} \quad (\text{A9})$$

$$u_c(v) = \left[\left(\frac{\pi D}{5000} \right)^2 u^2(f) + \left(\frac{\pi f}{5000} \right)^2 u^2(D) \right]^{\frac{1}{2}} \quad (\text{A10})$$

If a free running model is used in the experiments and, for example, an optical tracking system is used for to determine model position, then $v=s/t$ should be applied, and the instantaneous and/or mean speed can be calculated (s is distance between two consecutive sampled positions, and t is time between two consecutive samples). In this case, the combined uncertainty formula can be used to obtain model speed uncertainty:

$$u_C(v) = \left[\left(\frac{\partial v}{\partial s} \right)^2 u^2(s) + \left(\frac{\partial v}{\partial t} \right)^2 u^2(t) \right]^{\frac{1}{2}} \quad (\text{A11})$$

$$u_C(v) = \left[\left(\frac{l}{t} \right)^2 u^2(s) + \left(-\frac{s}{t^2} \right)^2 u^2(t) \right]^{\frac{1}{2}} \quad (\text{A12})$$

Standard uncertainties $u(s)$ and $u(t)$ need to be estimated based on information provided on model positions and accuracy of sample time. Nominal values of s and t should be applied to obtain combined uncertainty.

Similarly if a captive model is used or free running model follows the carriage the heading angle is assumed to be equal to the heading of the carriage with respect to the oncoming waves. For free running, self-propelled models when an optical system is used to obtain model positions the instantaneous (and mean) heading angle can be estimated from consecutive longitudinal and lateral positions of the model. The estimate of combined uncertainty in heading is then based on the uncertainty in the lateral and longitudinal position of the previous and next location of the model, and the nominal longitudinal and lateral distance between those two points. The arctangent is applied to estimate the uncertainty in the angle based on the uncertainty in the ratio of the lateral (ΔY) and longitudinal (ΔX) consecutive positions. Uncertainty in the ratio can be calculated from:

$$u\left(\frac{\Delta Y}{\Delta X}\right) = \left[\left(\frac{\partial \left(\frac{\Delta Y}{\Delta X} \right)}{\partial (\Delta Y)} \right)^2 u^2(\Delta Y) + \left(\frac{\partial \left(\frac{\Delta Y}{\Delta X} \right)}{\partial (\Delta X)} \right)^2 u^2(\Delta X) \right]^{\frac{1}{2}}$$

(A13)

$$u\left(\frac{\Delta Y}{\Delta X}\right) = \left[\left(\frac{1}{\Delta X} \right)^2 u^2(\Delta Y) + \left(-\frac{\Delta Y}{(\Delta X)^2} \right)^2 u^2(\Delta X) \right]^{\frac{1}{2}}$$

(A14)

Nominal ΔX and ΔY values are calculated from the mean heading angle, and the appropriate uncertainty can be used to calculate uncertainty in the ratio.

In case when model heading is obtained after double integration of yaw rate measurement, both uncertainty of yaw rate measurement and accuracy of integration procedure need to be included in combined uncertainty estimate.

Model geometry and mass distribution - sources of uncertainty in model geometry are model length (L_{PP}), width (B) and draft (T). For seakeeping experiments the position of centre of gravity (KG) and longitudinal radius of gyration (k_{yy}) are also important and their respective uncertainties need to be determined.

Typical suggested tolerances on the principal parameters associated with model geometry are $\pm 0.05\%$ on linear dimensions larger than 2m, and $\pm 1\text{mm}$ on dimensions less than 2 m, and $\pm 1\%$ on model displacement. In all cases they are the type B uncertainties that are constant for the duration of experiment. Examples of achieved and/or suggested uncertainties of model main parameters and mass properties as well as presented results are shown in Kishev (1998) and ITTC (2008).

Uncertainties in model geometry can be determined using past experience in model construction. For instance, if a model

manufacturer states that a 5-metre long model is accurate to within +/-2.5 mm with 90% confidence, then one can assume that the expanded uncertainty of the model length is +/-2.5 mm. The standard uncertainty can be estimated, using the confidence factor in Table 1, from expression $2.5/1.645=1.52$ assuming that a normal distribution can be applied to represent the stated value. So, the resultant standard uncertainty of the length is ~1.5 mm.

To estimate the uncertainty in the model \overline{KG} and k_{yy} , the propagation of uncertainty needs to be applied to the formula used to calculate these respective values. For example if \overline{KG} of a model is estimated based on inclining experiments and the following formula is employed: $\overline{KG} = \overline{KB} + \overline{BM} - \overline{GM}$. The vertical centre of buoyancy (\overline{KB}) and transverse metacenter (\overline{BM}) are geometry dependent, when metacentric height (\overline{GM}) can be obtained from inclining experiment. The combined uncertainty in \overline{KG} can be evaluated from:

$$u_c(\overline{KG}) = \left[\left(\frac{\partial \overline{KG}}{\partial \overline{KB}} \right)^2 u^2(\overline{KB}) + \left(\frac{\partial \overline{KG}}{\partial \overline{BM}} \right)^2 u^2(\overline{BM}) + \left(\frac{\partial \overline{KG}}{\partial \overline{GM}} \right)^2 u^2(\overline{GM}) \right]^{\frac{1}{2}} \quad (\text{A15})$$

The standard uncertainty of \overline{GM} can be estimated by applying combined uncertainty formula to:

$$\overline{GM} = \frac{w \cdot d}{W \cdot \tan(\varphi)} \quad (\text{A16})$$

Where, w is inclining weight, d is distance the inclining weight is moved, W model displacement, φ is heel angle when inclined.

The combined uncertainty of \overline{GM} can be presented as:

$$u_c(\overline{GM}) = \left[\left(\frac{\partial \overline{GM}}{\partial w} \right)^2 u^2(w) + \left(\frac{\partial \overline{GM}}{\partial d} \right)^2 u^2(d) + \left(\frac{\partial \overline{GM}}{\partial W} \right)^2 u^2(W) + \left(\frac{\partial \overline{GM}}{\partial \varphi} \right)^2 u^2(\varphi) \right]^{\frac{1}{2}} \quad (\text{A17})$$

$$u_c(\overline{GM}) = \left[\left(\frac{d}{W \cdot \tan \varphi} \right)^2 u^2(w) + \left(\frac{w}{W \cdot \tan \varphi} \right)^2 u^2(d) + \left(-\frac{w \cdot d}{W^2 \tan^2 \varphi} \right)^2 u^2(W) + \left(-\frac{w \cdot d}{W \cdot \sin^2 \varphi} \right)^2 u^2(\varphi) \right]^{\frac{1}{2}} \quad (\text{A18})$$

Standard uncertainty of \overline{KB} and \overline{BM} can be evaluated by assuming a simplified geometry of hull form and using known standard uncertainties of main parameters.

For example, the transverse \overline{BM} for a triangle-prism shaped vessel with a rectangular water plane area can be calculated from:

$$\overline{BM} = \frac{I}{V} = \frac{LB^3}{12V} = \frac{LB^3}{12 \cdot \frac{1}{2} LBT} = \frac{B^2}{6T} \quad (\text{A19})$$

Where, I is second moment of rectangular water plane area about its centreline, V volume of displacement, and L , B and T are length and breadth of water plane respectively and T is draft of the vessel.

The combined uncertainty of \overline{BM} is:

$$u_c(\overline{BM}) = \left[\left(\frac{\partial \overline{BM}}{\partial B} \right)^2 u^2(B) + \left(\frac{\partial \overline{BM}}{\partial T} \right)^2 u^2(T) \right]^{\frac{1}{2}} \quad (\text{A20})$$

$$u_c(\overline{BM}) = \left[\left(\frac{B}{3T} \right)^2 u^2(B) + \left(\frac{B^2}{6T^2} \right)^2 u^2(T) \right]^{\frac{1}{2}} \quad (\text{A21})$$

Nominal B and T values, and their respective uncertainties need to be applied to

calculate combined uncertainty in transverse \overline{BM} .

A similar procedure can be used to evaluate the combined uncertainty in the vertical location of centre of gravity and longitudinal radius of gyration k_{yy} that could be obtained a pendulum experiment.

Wave parameters – the uncertainty in wave measurements (regular and irregular) is one of major sources of uncertainty in experiments. Limitations of wave generators, the deterioration of wave properties propagating forward of experimental facilities and reflections from beach devices contribute to uncertainty in the wave environmental. Those uncertainties are difficult to estimate and are usually neglected. Target irregular wave properties are normally defined as significant wave height, modal period and type of spectrum. Target regular wave properties are described by wave amplitude and frequency. Wave matching is normally conducted based on a measurement in one selected-representative location, and supported by measurements in a few other locations to check for consistency. Two sources of error for which uncertainty could be estimated are difference between the target and matched wave(s) and uncertainty due to measuring and processing errors.

Either regular or irregular wave properties are generally obtained from measurements of wave displacement using devices such as a sonic wave probe and/or capacitance wave probes. Basic statistics from measurements provide rms that can be used as a first estimate of the amplitude of regular waves ($\zeta_A = \sqrt{2} \cdot rms$) and significant height of irregular waves ($H_{w1/3} = 4 \cdot rms$). Spectral

analysis can be also be employed to determine significant height of irregular waves $H_{w1/3} = 4\sqrt{m_0}$, where m_0 is area under the energy spectrum curve.

Total standard uncertainty in wave amplitude or height measurements should be evaluated using the uncertainty propagation formula. Type A uncertainty can be evaluated from repeated observations, although this can be impracticable for seakeeping experiments, and type B uncertainty established from properties of measuring device and data process.

Wave direction is also a significant parameter when undertaking experiments in oblique waves. Verification of waves propagation direction can be carried out using many instruments. One possible choice for the validation of wave direction with respect to the tank could be by using a 3D acoustic Doppler velocimeter. Periodic repeated wave measurements for selected wave directions can be carried out to determine standard deviation and standard uncertainty. The direction can be verified during wave matching for a specific experiment.

Data presentation

It is customary to present the final experimental results in a standardized format - usually non-dimensionalised. The linear translations from regular waves tests are typically non-dimensionalised by wave amplitude; rotations by wave slope and amplitude, and accelerations by $L_{PP}/(g \cdot \zeta_A)$. Generally these non-dimensional responses are presented to a base of the non-dimensional

encounter wave frequency given as $\omega_e \sqrt{\frac{L_{PP}}{g}}$

Therefore, the combined uncertainty u_c of the non-dimensional heave displacement $z' = z/\zeta_A$ can be calculated from the following:

$$u_c(z') = \left[\left(\frac{\partial z'}{\partial z} \right)^2 u^2(z) + \left(\frac{\partial z'}{\partial \zeta_A} \right)^2 u^2(\zeta_A) \right]^{1/2} \quad (\text{A22})$$

$$u_c(z') = \left[\left(\frac{1}{\zeta_A} \right)^2 u^2(z) + \left(-\frac{z}{\zeta_A^2} \right)^2 u^2(\zeta_A) \right]^{1/2} \quad (\text{A23})$$

Where, z and ζ_A are heave displacement and regular wave amplitude, $u(z)$ and $u(\zeta_A)$ are respective total standard uncertainties of measured heave displacement and wave amplitude including all type A and type B elemental error sources.

Similarly, combined uncertainty of non-dimensional encounter frequency

$\omega'_e = \omega_e \sqrt{\frac{L_{PP}}{g}}$ can be evaluated from:

$$u_c(\omega'_e) = \left[\left(\frac{\omega'_e}{\omega_e} \right)^2 u^2(\omega_e) + \left(\frac{\omega'_e}{L_{PP}} \right)^2 u^2(L_{PP}) \right]^{1/2} \quad (\text{A24})$$

$$u_c(\omega'_e) = \left[\left(\frac{L_{PP}}{g} \right) u^2(\omega_e) + \left(-\frac{\omega_e}{2(L_{PP} \cdot g)^{1/2}} \right)^2 u^2(L_{PP}) \right]^{1/2} \quad (\text{A25})$$

Again, ω_e , L_{PP} and g are respective nominal values, and $u(\omega_e)$ and $u(L_{PP})$ are respective standard uncertainties.

Motions in irregular seas are typically presented as plots of non-dimensional or significant values versus velocity, Froude number or sea state.

For example, formulae for non-dimensional pitch motion and the resulting combined uncertainty are as follow:

$$C_\theta = \frac{\theta \cdot L_{PP}}{2\pi \cdot H_{W1/3}} \quad (\text{A26})$$

$$u_c(c_\theta) = \sqrt{\left(\frac{\partial C_\theta}{\partial \theta} \right)^2 u^2(\theta) + \left(\frac{\partial C_\theta}{\partial H_{W1/3}} \right)^2 u^2(H_{W1/3}) + \left(\frac{\partial C_\theta}{\partial L_{PP}} \right)^2 u^2(L_{PP})}$$

Where:

$$\frac{\partial C_\theta}{\partial \theta} = \frac{L_{PP}}{2\pi \cdot H_{W1/3}}$$

$$\frac{\partial C_\theta}{\partial H_{W1/3}} = -\frac{\theta L_{PP}}{2 \cdot H_{W1/3}^2}$$

$$\frac{\partial C_\theta}{\partial L_{PP}} = \frac{\theta}{2 \cdot H_{W1/3}}$$

θ is the significant pitch angle response in irregular wave.


Combined uncertainty in estimation of Froude number ($Fr = V / \sqrt{gL_{PP}}$) can be expressed as follow:

$$u_c(Fr) = \sqrt{\left(\frac{\partial Fr}{\partial V} \right)^2 u^2(V) + \left(\frac{\partial Fr}{\partial L_{PP}} \right)^2 u^2(L_{PP})} \quad (\text{A27})$$

Where,

$$\frac{\partial Fr}{\partial V} = \frac{1}{\sqrt{gL_{PP}}}$$

$$\frac{\partial Fr}{\partial L_{PP}} = -\frac{V}{2\sqrt{gL_{PP}^3}}$$

	ITTC – Recommended Procedures and Guidelines		7.5-02 07-02.1 Page 20 of 22	
	Seakeeping Experiments		Effective Date 2011	Revision 04

Once the experimental data have been collected and reduced to non-dimensional format for a particular wave encounter frequency and/or Froude number, they can be presented in a tabular format or we may want to obtain a mathematical expression to represent the data. In this case regression can be performed on the experimental data (after data reduction) and a polynomial equation fit to represent the data. The type B uncertainty associated with the regression should be included in the analysis.

A.2.3 Example

Table A2 and Figure A1 present examples of total standard and combine uncertainty calculation of model parameters and responses from submarine model seakeeping surface experiments in irregular seas.

From the table one can conclude that the uncertainty in the model main parameter is

contained below 1%, and that the type B uncertainty is dominating model motions measurements.

A.2.4 Summary

The above presented procedure outlines ITTC recommended ISO GUM approach uncertainty analysis in seakeeping experiment measurements. Intention of the procedure is to emphasize details unique for seakeeping experiment measurements and data presentation. Background information for ISO GUM approach and assumptions are discussed in ITTC Specialists Committee on Uncertainty Analysis procedure 7.5-02-01-01. The methodologies presented here are relevant to uncertainties in measurements only. Subjects of uncertainty in predictions

Seakeeping Experiments

Effective Date
2011

Revision
04

Source of uncertainty		Units	Description of accuracy	Type A uncertainty	Type B uncertainty	Standard uncertainty
	Nominal Value					
Model Lpp	4.70	m	+/- 3 mm, 90% confidence		0.0018	0.002
Model B	0.51	m	+/- 2 mm, 90% confidence		0.0012	0.001
Model T	0.52	m	+/- 2 mm, 90% confidence		0.0012	0.001
Model D	671.14	m ³	resultant		0.0042	0.004
Model KB	0.29	m	resultant		0.0012	0.001
Model BM	0.302	m	resultant		0.0004	0.000
Model KG	0.264	m	inclining experiment		0.0015	0.002
Model kxx	0.213	m	swing frame		0.0024	0.002
Model GMt	0.038	m	resultant		0.0008	0.001
Speed 1	3.4	knots	Optical tracking Qualisys	0.057	0.012	0.059
Speed 2	6.2	knots	Optical tracking Qualisys	0.042	0.016	0.063
Speed 3	12.9	knots	Optical tracking Qualisys	0.052	0.028	0.108
Roll Angle 1	13.8	deg	FOG	0.190	2	2.009
Roll Angle 2	17.5	deg	FOG	0.169	2	2.007
Roll Angle 3	1.7	deg	FOG	0.054	2	2.001
Pitch Angle 1	3.5	deg	FOG	0.063	2	2.001
Pitch Angle 2	1.1	deg	FOG	0.028	2	2.000
Pitch Angle 3	0.7	deg	FOG	0.041	2	2.000
Heave Displ. 1	2.12	m	Motion Pack	0.030		0.030
Heave Displ. 2	2.14	m	Motion Pack	0.020		0.020
Heave Displ. 3	0.38	m	Motion Pack	0.017		0.017
Vert. Accel. 1	0.16	g	Honeywell, QA 1400	0.001	0.0031	0.003
Vert. Accel. 2	0.14	g	Honeywell, QA 1401	0.002	0.0031	0.004
Vert. Accel. 3	0.04	g	Honeywell, QA 1402	0.001	0.0031	0.003
Relative Mot. 1	1.33	m	ULS, USS 635	0.018	0.0013	0.018
Relative Mot. 2	1.43	m	ULS, USS 635	0.008	0.0013	0.008
Relative Mot. 3	0.69	m	ULS, USS 635	0.010	0.0013	0.010
Wave Elev. 1	2.62	m	Capacitance probe	0.004	0.004	0.005
Wave Elev. 2	1.84	m	Capacitance probe	0.005	0.004	0.007
Wave Elev. 3	0.64	m	Capacitance probe	0.006	0.004	0.007
						Combined Uncertainty
Froude no. 1	0.07					0.0022
Froude no. 2	0.12					0.0024
Froude no. 3	0.25					0.0041

Table A2. Estimate of uncertainty for responses during seakeeping experiments

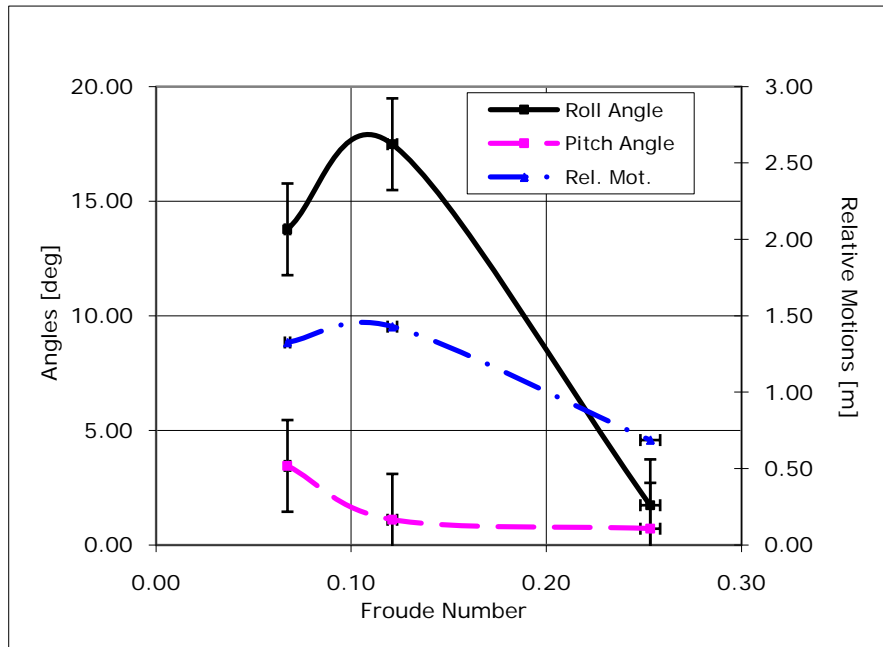


Figure A1. Example of responses and range of uncertainty