INTERNATIONAL TOWING TANK CONFERENCE

# ITTC Symbols and Terminology List 

## Alphabetic

Version 2021

June 2021

## Supersedes all previous versions

Updated by the $\mathbf{2 9}^{\text {th }}$ ITTC Quality Systems Group

NOTE: bold letters are used to denote vectors
Red colour identifies the additions/modifications of this version of the List

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| A | MS | (fundamental, statistical, stochastic) Average, sample mean |  |  |
| :---: | :---: | :---: | :---: | :---: |
| A | AP | (fluid mechanics, lifting surfaces) Projected area | $b c_{M}$ | $\mathrm{m}^{2}$ |
| A | A, AR, AREA | (ships, basic quantities) Area in general |  | $\mathrm{m}^{2}$ |
| A |  | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Assumed centre of gravity above keel used for cross curves of stability |  | 1 |
| Ao | AO | (ships, propulsor performance, propulsor geometry) Propeller disc area | $\pi D^{2} / 4$ | $\mathrm{m}^{2}$ |
| $A_{n}, A_{6}$ |  | (ships, propulsor geometry, water jets) Nozzle discharge area |  | $\mathrm{m}^{2}$ |
| $\overline{A B}$ | XAB | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of buoyancy from aft perpendicular | Distance of centre of buoyancy from aft perpendicular | m |
| $A_{\text {BL }}$ | ABL | (ships, hull geometry) Area of bulbous bow in longitudinal plane | The area of the ram projected on the middle line plane forward of the fore perpendicular | $\mathrm{m}^{2}$ |
| $A_{\text {BT }}$ | ABT | (ships, hull geometry) Area of transverse cross-section of a bulbous bow (full area port and star-board) | The cross sectional area at the fore perpendicular. Where the water lines are rounded so as to terminate on the forward perpendicular $\mathrm{A}_{\mathrm{BT}}$ is measured by continuing the area curve forward to the perpendicular, ignoring the final rounding; | $\mathrm{m}^{2}$ |
| $A_{\mathrm{C}}$ | AC | (ships, appendage geometry) Area under cut-up |  | $\mathrm{m}^{2}$ |
| $A_{\text {c }}$ | CUA | (ACV and SES) Cushion area | Projected area of ACV or SES cushion on water surface | $\mathrm{m}^{2}$ |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $A_{\text {c }}$ |  | (seakeeping, large amplitude motions capsizing) Area of deck available to crew |  | $\mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{\text {D }}$ | AD | (ships, propulsor geometry) <br> Developed blade area | D eveloped blade area of a screw propeller outside the boss or hub | $\mathrm{m}^{2}$ |
| $A_{\text {Den }}$ | ADEN | (ships, propulsor geometry) Duct entry area |  | $\mathrm{m}^{2}$ |
| $A_{\text {Dex }}$ | ADEX | (ships, propulsor geometry) Duct exit area |  | $\mathrm{m}^{2}$ |
| $A_{\text {E }}$ | AE | (ships, propulsor geometry) <br> Expanded blade area | Expanded blade area of a screw propeller outside the boss or hub | $\mathrm{m}^{2}$ |
| $\overline{A F}$ | XAF | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Distance of the centre of flotation from aft perpendicular |  | m |
| $A_{\text {F }}$ | AFO | (hydrofoil boats) Foil area (general) | Foil area in horizontal plane | $\mathrm{m}^{2}$ |
| $A_{\text {Fb }}$ | AFB, AFB0 | (ships, appendage geometry, ships, manoeuvrability) Projected area of bow fins |  | $\mathrm{m}^{2}$ |
| $A_{\text {fE }}$ | AFE | (hydrofoil boats) Emerged area of foil |  | $\mathrm{m}^{2}$ |
| $A_{\text {fF }}$ | ASFF | (hydrofoil boats) Submerged area of front foil |  | $\mathrm{m}^{2}$ |
| $A_{\text {FR }}$ | AFR | (ships, appendage geometry) Frontal area | Projected frontal area of an appendage | $\mathrm{m}^{2}$ |
| $A_{\text {FS }}$ | AFS, AFST | (ships, appendage geometry, seakeeping) Projected area of stern fins |  | $\mathrm{m}^{2}$ |
| $A_{\text {FS }}$ | AFS | (hydrofoil boats) Submerged foil area |  | $\mathrm{m}^{2}$ |
| $A_{\text {fSto }}$ | AFSTO | (hydrofoil boats) Submerged foil plan area at take-off speed |  | $\mathrm{m}^{2}$ |
| $A_{\text {FT }}$ | AFT | (hydrofoil boats) Total foil plan area |  | $\mathrm{m}^{2}$ |
| $\overline{A G}_{\mathrm{L}}$ | XAG | (seakeeping, large amplitude motions capsizing) Longitudinal centre of gravity from aft perpendicular | Distance of centre of gravity from aft perpendicular | m |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $\overline{A G}_{\text {T }}$ | YAG | (seakeeping, large amplitude motions capsizing) Transverse distance from assumed centre of gravity A, to actual centre of gravity G |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $\overline{A G}^{\mathrm{V}}$ | ZAG | (seakeeping, large amplitude motions capsizing) Vertical distance from assumed centre of gravity A, to actual centre of gravity G |  | m |
| $A_{\text {HL }}$ | AHLT | (ships, manoeuvrability) <br> Lateral area of the hull | The area of the profile of the underwater hull of a ship when projected normally upon the longitudinal centre plane | $\mathrm{m}^{2}$ |
| $A_{\text {I }}$ | AIA | (multi-hull vessels) Struthull intersection area |  | $\mathrm{m}^{2}$ |
| $A_{i j}$ | AM(I,J) | (solid body mechanics, inertial and hydro properties) Added mass coefficient in $i^{\text {th }}$ mode due to $j^{\text {th }}$ motion |  | 1 |
| $A_{\text {J }}$ | ASJ | (sailing vessels) Area of jib or genoa |  | $\mathrm{m}^{2}$ |
| $A_{\text {LK }}$ | ALK | (sailing vessels) Lateral area of keel |  | $\mathrm{m}^{2}$ |
| $A_{\text {LT }}$ | ALT | (sailing vessels) Total lateral area of yacht |  | $\mathrm{m}^{2}$ |
| $A_{\text {LV }}$ | AHLV | (ships, manoeuvrability, seakeeping, large amplitude motions capsizing)) Lateral area of hull above water |  | $\mathrm{m}^{2}$ |
| $A_{\text {M }}$ | AM | (ships, hull geometry) Area of midship section | Midway between fore and aft perpendiculars | $\mathrm{m}^{2}$ |
| $A_{\mathrm{m}}$ | ASM | (sailing vessels) Area of mainsail |  | $\mathrm{m}^{2}$ |
| $A_{N}$ | ASN | (sailing vessels) Normalized sail area |  | $\mathrm{m}^{2}$ |
| $A_{n}$ |  | (ships, propulsor geometry, water jets)Nozzle discharge area |  | $\mathrm{m}^{2}$ |
| $A_{\text {P }}$ | AP | (ships, propulsor geometry) Projected blade area | Projected blade area of a screw propeller outside the boss or hub | $\mathrm{m}^{2}$ |
| А $_{\text {pB }}$ | APB | Wetted Surface Area of Pod Main Body |  | $\mathrm{m}^{2}$ |

## ITTC Symbols

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $A_{\text {PBF }}$ | APBF | Wetted Surface Area of Bottom Fin |  | $\mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{\text {ps }}$ | APS | Wetted Surface Area of Strut |  | $\mathrm{m}^{2}$ |
| $A_{\text {R }}$ | ARU | (ships, manoeuvrability) To- <br> tal lateral area of rudder |  | $\mathrm{m}^{2}$ |
| $A_{\text {RF }}$ | AF | (ships, appendage geometry) Lateral area of rudder flap |  | $\mathrm{m}^{2}$ |
| $A_{\text {RL }}$ |  | (seakeeping, large amplitude motions capsizing) Positive area under righting lever curve |  | $\mathrm{m}^{2}$ |
| $A_{\text {Rmov }}$ | ARMV | (ships, manoeuvrability) <br> Lateral area of the movable <br> part of rudder |  | $\mathrm{m}^{2}$ |
| $A_{\text {RN }}$ | ARNO | (ships, manoeuvrability) Nominal lateral area of rudder | $\left(A_{\mathrm{R}}+A_{\mathrm{Rmov}}\right) / 2$ | $\mathrm{m}^{2}$ |
| $A_{\text {RP }}$ | ARP | (ships, appendage geometry)Lateral area of rudder in the propeller race |  | $\mathrm{m}^{2}$ |
| $A_{\text {RT }}$ | ART | (ships, appendage geometry) Total lateral area of rudder | $A_{\mathrm{RX}}+A_{\mathrm{Rmov}}$ | $\mathrm{m}^{2}$ |
| $A_{\text {RX }}$ | ARX | (ships, appendage geometry) Lateral area of the fixed part of rudder |  | $\mathrm{m}^{2}$ |
| As | AS | (seakeeping, large amplitude motions capsizing, sailing vessels) Sail area in general, Area of sails in profile according to ISO 8666 | $(P E+I J) / 2$ | $\mathrm{m}^{2}$ |
| $A_{5}$ |  | (ships, propulsor geometry, water jets) Cross sectional area at station $s$ |  | $\mathrm{m}^{2}$ |
| $A_{\text {SFR }}$ | ASFR | (hydrofoil boats) Submerged area of rear foil |  | $\mathrm{m}^{2}$ |
| Asi | ASI | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Attained subdivision index |  | 1 |
| Ask | ASK | (ships, appendage geometry) Projected skeg area |  | $\mathrm{m}^{2}$ |


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| $A_{\text {SP }}$ | ASSP | (sailing vessels) Area of spinnaker |  | $\mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| Ass | ASS | (hydrofoil boats) Submerged strut area |  | $\mathrm{m}^{2}$ |
| $A_{\text {T }}$ | ATR | (ships, hull geometry) Area of transom (full area port and starboard) | Cross-sectional area of transom stern below the load waterline | $\mathrm{m}^{2}$ |
| $A_{v}$ | AV | (ships, hull geometry, seakeeping, large amplitude motions capsizing) Projected lateral area of the portion of the ship and deck cargo above the waterline (IMO/IS, IMO/HSC'2000) Area exposed to wind | Area of portion of ship above waterline projected normally to the direction of relative wind | $\mathrm{m}^{2}$ |
| $A_{\text {w }}$ | AW | (ships, hull geometry) Area of water-plane |  | $\mathrm{m}^{2}$ |
| $A_{\text {Wa }}$ | AWA | (ships, hull geometry) Area of water-plane aft of midship |  | $\mathrm{m}_{2}$ |
| $A_{\text {wf }}$ | AWF | (ships, hull geometry) Area of water-plane forward of midship |  | $\mathrm{m}^{2}$ |
| $A_{\mathrm{X}}$ | AX | (ships, hull geometry) Area of maximum transverse section |  | $\mathrm{m}^{2}$ |
| $A_{\mathrm{XV}}$ | AXV | (ships,hull geometry, ship performance) Transverse projected area above the waterline including superstructures | Projected area of the ship above the waterline projected on a transversal plane | $\mathrm{m}^{2}$ |
| $\overline{A Z}$ | YAZ | (seakeeping, large amplitude motions, capsizing ships, hydrostatics, stability) Righting arm based on horizontal distance from assumed centre of gravity A, to Z | Generally tabulated in cross curves of stability | m |
| $A_{z \bar{\prime}}(\omega)$ |  | (ships, seakeeping) Amplitude of frequency response function for translatory motions | $\begin{aligned} & z_{a}(\omega) / \zeta_{a}(\omega) \text { or } \\ & z_{a}(\omega) / \eta_{a}(\omega) \end{aligned}$ | 1 |
| $A_{\theta s!}(\omega)$ |  | (ships, seakeeping) Amplitude of frequency response function for rotary motions | $\begin{aligned} & \Theta_{a}(\omega) / \zeta_{a}(\omega) \text { or } \\ & \Theta_{a}(\omega) /\left(\omega^{2} /\left(g \zeta_{a}(\omega)\right)\right) \end{aligned}$ | 1 |

## ITTC Symbols

Version 2021

| ITTC | Computer | Name |
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| Symbol | Symbol |  |

Definition or
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| a, $a^{1}$ | AC, A1 | (ships, basic quantities) Linear or translatory acceleration | $d v / d t$ | $\mathrm{m} / \mathrm{s}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $a$ | ADMP | (fundamental, time and frequency domain quantity) Damping | $s^{r}$, in Laplace variable | 1/s |
| $a$ | RAUG | (ships, performance) Resistance augment fraction | $\left(T-R_{\mathrm{T}}\right) / R_{\mathrm{T}}$ | 1 |
| $a$ | ATT | (ships, unsteady propeller forces) Cylindrical coordinates | Cylindrical system with origin $O$ and longitudinal $x$ axis as defined before; angular $a$-(attitude)-coordinate , zero at 12 o'clock position, positive clockwise looking forward, $r$ distance measured from the $x$-axis |  |
| $a$ |  | Half-width of a rectangular distribution | Half-width of a rectangular distribution of possible values of input quantity $X_{i}$ : $a=\left(a_{+}-a_{-}\right) / 2$ |  |
| $a_{\text {D }}$ | ADR | (ships, propulsor geometry) Developed blade area ratio | $A_{\mathrm{D}} / A_{0}$ | 1 |
| $a_{\text {E }}$ | ADE | (ships, propulsor geometry) Expanded blade area ratio | $A_{\mathrm{E}} / A_{0}$ | 1 |
| $a_{i}$ | AT(I) | (ships, seakeeping) Attitudes of the floating system | $i=1,2$, 3, e.g. Euler angles of roll, pitch, and yaw, respectively | rad |
| $a_{\text {P }}$ | ADP | (ships, propulsor geometry) Projected blade area ratio | $A_{\mathrm{P}} / A_{0}$ | 1 |
| $a_{+}$ |  | Upper bound | Upper bound, or upper limit, of input quantity $X_{i}$ : |  |
| $a$ - |  | Lower bound | Lower bound, or lower limit, of input quantity $X_{i}$ : |  |


| ITTC | Computer |
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| B | B, BR | (ships, basic quantities, hull geometry) Breadth, moulded, of ships hull |  | m |
| :---: | :---: | :---: | :---: | :---: |
| B |  | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Centre of buoyancy | Centroid of the underwater volume |  |
| $B_{B}$ | BB | (multi-hull vessels) Box breadth | Breadth of main deck | m |
| $B_{C}$ | BCU | (ACV and SES) Cushion breadth | SES cushion breadth measured between the side walls | m |
| $B^{\text {C }}$ | CIRCB | (ships, hull geometry) R.E. Froude's breadth coefficient | $B / \nabla^{1 / 3}$ | 1 |
| $B_{\text {cb }}$ |  | (seakeeping, large amplitude motions capsizing) Breadth between centres of buoyancy of side hulls |  | m |
| $B_{\mathrm{f}}$ | BF | (ships, ship performance) Bluntness coefficient | See 7.5-04-01-01.1 | 1 |
| $B_{\text {FOA }}$ | BFOA | (hydrofoil boats) Maximum vessel breadth including foils |  | m |
| $B_{i j}$ | DA(I,J) | (solid body mechanics, inertial and hydro properties) Damping coefficient in ith mode due to $j$ th motion |  |  |
| $B_{\text {LCG }}$ | BLCG | (planing, semi-displacement vessels) Breadth at longitudinal position of the centre of gravity | Breadth over spray strips measured at transverse section containing centre of gravity | m |
| $B_{M}$ | BM | (ships, hull geometry) Breadth, moulded of midship section at design water line |  | m |
| $\overline{B M}$ | ZBM | (seakeeping, large amplitude motions capsizing) Transverse metacentre above centre of buoyancy | Distance from the centre of buoyancy B to transverse metacentre M $\overline{B M}=\frac{I_{\mathrm{T}}}{\nabla}=\overline{K M}-\overline{K B}$ | m |
| $\overline{B M}_{L}$ | ZBML | (seakeeping, large amplitude motions capsizing) Longitudinal metacentre above centre of buoyancy | $\overline{B M}_{L}=\overline{K M}_{L}-\overline{K B}$ | m |
| Bo | BN | (fluid mechanics, flow parameter) Boussinesq number | $V /\left(g R_{H}\right)^{1 / 2}$ | 1 |

Version 2021
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| $B_{\text {OA }}$ | BOA | (sailing vessels) Breadth, overall |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $B_{P}$ | BP | (ships, propulsor performance) Taylor's propeller coefficient based on delivered horsepower (obsolete) | $n P_{\mathrm{D}}{ }^{1 / 2} / V_{\mathrm{A}}{ }^{2.5}$ <br> with $n$ in revs $/ \mathrm{min}$, $P_{\mathrm{D}}$ in horsepower, and $V_{\mathrm{A}}$ in kn | 1 |
| $B_{\text {PA }}$ | BPA | (planing, semi-displacement vessels) Mean breadth over chines | $A_{P} / L_{\text {P }}$ | m |
| $B_{\text {PC }}$ | BPC | (planing, semi-displacement vessels) Breadth over chines | Breadth over chines, excluding external spray strips | m |
| $B_{\text {pt }}$ | BPT | (planing, semi-displacement vessels) Transom breadth | Breadth over chines at transom, excluding external spray strips | m |
| $B_{\text {PX }}$ | BPX | (planing, semi-displacement vessels) Maximum breadth over chines | Maximum breadth over chines, excluding external spray strips | m |
| $B$ s | BS | (multi-hull vessels) Hull spacing | Distance between hull centre lines | m |
| $B_{\text {T }}$ | BTR | (ships, hull geometry) Breadth, moulded of transom at design water line |  | m |
| $B_{\text {TV }}$ | BTUN | (multi-hull vessels) Tunnel width | Minimal distance of the demihulls at the waterline | m |
| $B_{U}$ | BU | (ships, propulsor performance) Taylor's propeller coefficient based on thrust horsepower (obsolete) | $n P_{T}^{1 / 2} / V_{\mathrm{A}}{ }^{2.5}$ with $n$ in revs/min, $P_{\mathrm{T}}$ in horsepower, and $V_{\mathrm{A}}$ in kn | 1 |
| $B_{\text {WL }}$ | BWL | (ships, hull geometry) Maximum moulded breadth at design water line |  | m |
| $B_{\text {WLT }}$ | BWLT | (ACV and SES) Total waterline breadth of SES | At the water line | m |
| $B_{\mathrm{X}}$ | BX | (ships, hull geometry) Breadth, moulded of maximum section area at design water line |  | m |
| $\overline{B M}$ | ZBM | (ships, hydrostatics, stability) Transverse metacentre above centre of buoyancy | Distance from the centre of buoyancy B to the transverse metacentre M. $\overline{B M}=I_{\mathrm{T}} / \nabla=\overline{K M}-\overline{K B}$ | m |
| $\overline{B M_{\mathrm{L}}}$ | ZBML | (ships, hydrostatics, stability) Longitudinal metacentre above centre of buoyancy | $\overline{\mathrm{KM}_{\mathrm{L}}}-\overline{\mathrm{KB}}$ |  |

Version 2021
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|  | Computer Symbol | Name | Definition or | SI- |
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| Symbol | Symbol | Name | Explanation | Unit |


| b |  | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Centre of flotation of added buoyancy layer or centre of lost buoyancy of the flooded volume |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $b$ |  | (seakeeping, large amplitude motions capsizing) Maximum tank breadth |  | m |
| $b$ | B | (environmental mechanics, waves) Bandwidth of spectral resolution | Sampling frequency divided by the number of transform points | Hz |
| $b$ | SP | (fluid mechanics, lifting surfaces) Wing or foil span |  | m |
| $b_{\text {F }}$ | BSPF | (fluid mechanics, lifting surfaces) Flap span |  | m |
| $b_{\text {R }}$ | SPRU | (ships, manoeuvrability) <br> Rudder span | Maximum distance from root to tip | m |
| $b_{\text {RM }}$ | SPRUME | (ships, manoeuvrability) <br> Mean span of rudder |  | m |
| $b_{\text {s }}$ | BST | (hydrofoil boats) Span of struts |  | m |
| $b_{\text {ST }}$ | BSTT | (hydrofoil boats) Transverse horizontal distance of struts |  | m |
| $b_{\text {w }}$ | BSPW | (hydrofoil boats) Foil span wetted |  | m |
| $b_{+}$ |  | Upper bound of the deviation | Upper bound, or upper limit, of the deviation of input quantity $X_{i}$ from its estimate $x_{i:} \quad b_{+}=a_{+}-x_{i}$ |  |
| $b$. |  | Lower bound of the deviation | Lower bound, or lower limit, of the deviation of input quantity $X_{i}$ from its estimate $x_{i:} \quad b_{-}=x_{i}-a_{-}$ |  |

Version 2021
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| C | CR | (fundamental, statistical, stochastic) Population covariance |  |  |
| :---: | :---: | :---: | :---: | :---: |
| C | FF(2) | (ships, basic quantities) Cross force | Force normal to lift and drag (forces) | N |
| $C_{10}$ | C10M | (environmental mechanics, wind) Surface drag coefficient | $\left(0.08+0.065 U_{10}\right) 10^{-3}$ |  |
| $C_{\text {A }}$ | CA | (ships, hull resistance) Incremental resistance coefficient for model ship correlation | $R_{\text {A }} /(S q)$ | 1 |
| $C_{\text {AA }}$ | CAA | (ships, hull resistance) Air or wind resistance coefficient | $\begin{aligned} & R_{\mathrm{AA}} /(S q) \\ & =C_{D A} \frac{\rho_{\mathrm{A}}}{\rho_{\mathrm{S}}} \frac{A_{\mathrm{v}}}{S_{\mathrm{S}}}=-C_{\mathrm{x}} \frac{\rho_{\mathrm{A}}}{\rho_{\mathrm{S}}} \frac{A_{\mathrm{v}}}{S_{\mathrm{S}}} \end{aligned}$ | 1 |
| $C_{\text {ADM }}$ | CADM | (ships, performance) Admiralty coefficient | $U^{2 / 3} V^{3} / P_{\text {S }}$ | 1 |
| $C_{\text {AL }}$ | CAHL | (ships, manoeuvrability) Coefficient of lateral area of ship | $A_{\text {HL }} /(L T)$ | 1 |
| $C_{\text {APP }}$ | CAPP | (ships, hull resistance) Appendage resistance coefficient | $R_{\text {APP }} /(S q)$ | 1 |
| С | CB | (ships, hull geometry) Block coefficient | $\nabla /(L B T)$ | 1 |
| $C_{\text {BFTC }}$ | CBFTC | Thickness Cord Ratio of Bottom Fin |  | 1 |
| Cc | CC | (ships, basic quantities) Cross force coefficient | $C_{\mathrm{C}}=\frac{C}{q A}$ | 1 |
| $C^{\text {C }}$ | CIRCC | (ships, hull resistance) R.E. Froude's resistance coefficient | $1000 R_{\mathrm{T}} /\left(4\left(K^{\mathrm{C}}\right)^{2}\right)$ | 1 |
| $C_{D}$ | CDSE | (fluid mechanics, lifting surfaces) Section drag coefficient |  | 1 |
| $C_{D}$ | CD | (ships, hull resistance) Drag coefficient | D / (Sq) | 1 |
| $C_{\text {D }}$ |  | (seakeeping, large amplitude motions capsizing) Crew density | Proportion of boat plan needed for crew |  |


| ITTC | Computer |
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| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
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| $C_{\text {DA }}$ | CDA | (ships, Resistance and Propulsion, Hull resistance) Air or wind resistance coefficient, from wind tunnel tests | $=\frac{R_{\mathrm{AA}}}{A_{V \frac{1}{2} \rho_{\mathrm{A}} V^{2}}}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $C_{\text {DF }}$ | CDF | (hydrofoil boats) Drag coefficient of foil | $D_{\mathrm{F}} /\left(A_{\mathrm{FS}} q\right)$ | 1 |
| $C_{\text {DI }}$ | CDSI | (fluid mechanics, lifting surfaces) Section induced drag coefficient |  | 1 |
| $C_{\text {DI }}$ | CDI | (hydrofoil boats) Induced drag coefficient | $D_{\mathrm{I}} /\left(A_{\text {FS }} q\right)$ | 1 |
| $C_{\text {DINT }}$ | CDINT | (hydrofoil boats) Interference drag coefficient | $D_{\text {INT }} /\left(A_{\text {FS }} q\right)$ | 1 |
| $C_{\text {D0 }}$ | CD0 | (hydrofoil boats) Section drag coefficient for angle of attack equal to zero | $D_{\mathrm{P}} /\left(A_{\text {FS }} q\right)$ | 1 |
| $C_{\text {DS }}$ | CDSP | (hydrofoil boats) Spray drag coefficient | $D_{\text {S }} /\left(A_{\text {FS }} q\right)$ | 1 |
| $C_{\text {DVENT }}$ | CDVENT | (hydrofoil boats) Ventilation drag coefficient | $D_{\mathrm{V}} /\left(A_{\mathrm{Fs}} q\right)$ | 1 |
| $C_{\text {DW }}$ | CDW | (hydrofoil boats) Wave drag coefficient | $D_{\mathrm{W}} /\left(A_{\mathrm{FS}} q\right)$ | 1 |
| $C_{D}$ V | CDVOL | (ships, performance) <br> Power-displacement coefficient | $P_{\mathrm{D}} /\left(\rho V^{3} \nabla^{2 / 3} / 2\right)$ | 1 |
| $C_{\text {F }}$ | CF | (ships, hull resistance) Frictional resistance coefficient of a body | $R_{\mathrm{F}} /(S q)$ | 1 |
| $C_{f}$ | CFL | (fluid mechanics, boundary layers) Skin friction coefficient | $\tau /\left(\rho U_{\mathrm{e}}^{2} / 2\right)$ | 1 |
| $C_{\text {F0 }}$ | CF0 | (ships, hull resistance) Frictional resistance coefficient of a corresponding plate | $R_{\text {F0 }} /(S q)$ | 1 |
| $C_{\text {Fu }}$ | CFU | (sailing vessels) Frictional resistance coefficient (upright) | $R_{\text {FU }} /(S q)$ | 1 |
| $C_{\text {Gm }}$ | CGM | (ships, Geometry and Hydrostatics, Hull Geometry) Dimensionless $\overline{G M}$ coefficient | $\overline{G M} / \nabla^{1 / 3}$ | 1 |

Version 2021
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| CGz | CGZ | (ships, Geometry and Hydrostatics, Hull Geometry)Dimensionless $\overline{G Z}$ coefficient | $\overline{G Z} / \nabla^{1 / 3}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| СкG $^{\text {¢ }}$ | CKG | (ships, Geometry and Hydrostatics, Hull Geometry)Dimensionless $\overline{K G}$ coefficient | $\overline{K G} / T$ | 1 |
| $C_{\text {H }}$ |  | (seakeeping, large amplitude motions capsizing) Height coefficient, depending on the height above sea level of the structural member exposed to the wind |  | 1 |
| $C_{\text {I }}$ |  | (sailing vessels) Induced resistance coefficient |  | 1 |
| $C_{\text {I }}$ | CI | (ice going vessels) Coefficient of net ice resistance | $R_{\mathrm{I}} /\left(\rho_{\mathrm{I}} g h^{2} B\right)$ | 1 |
| $C_{i j}$ | RF(I, J) | (solid body mechanics, inertial and hydro properties) Restoring force coefficient in $i^{\text {th }}$ mode due to $j^{\text {th }}$ motion |  |  |
| $C_{\text {IL }}$ | CWIL | (ships, hull geometry) Coefficient of inertia of water plane, longitudinal | $12 I_{\mathrm{L}} /\left(\mathrm{BL}^{3}\right)$ | 1 |
| $C_{\text {IT }}$ | CWIT | (ships, hull geometry) Coefficient of inertia of water plane, transverse | $12 I_{\mathrm{T}} /\left(B^{3} L\right)$ | 1 |
| $C_{\text {IW }}$ | CIW | (ice going vessels) Coefficient of water resistance in the presence of ice | $R_{\text {IW }} /\left(S q_{\text {IW }}\right)$ | 1 |
| $C_{\text {L }}$ |  | (seakeeping, large amplitude motions capsizing) Crew limit | Maximum number of persons on board |  |
| $C_{L}$ | CLSE | (fluid mechanics, lifting surfaces) Section lift coefficient |  | 1 |
| $C_{L F}$ | CLF | (hydrofoil boats) Foil lift coefficient | $L_{\mathrm{F}} /\left(A_{\mathrm{FS}} q\right)$ | 1 |
| $C_{L 0}$ | CL0 | (hydrofoil boats) Profile lift coefficient for angle of attack equal to zero | $L_{0} /\left(A_{\text {FS }} q\right)$ | 1 |
| $C_{L 0}$ | CL0D | (planing, semi-displacement vessels) Lift coefficient for zero deadrise | $\Delta /\left(B_{\mathrm{CG}^{2}}{ }^{2}\right)$ | 1 |

Version 2021
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| С $_{\text {Lто }}$ | CLTO | (hydrofoil boats) Lift coefficient at take-off condition | $L_{\text {TO }} /\left(A_{\mathrm{FS}} q\right)$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $C_{L X}$ | CLA | (hydrofoil boats) Slope of lift curve | $d C_{L} / d \alpha$ | 1 |
| $C_{L \beta}$ | CLBET | (planing, semi-displacement vessels) Lift coefficient for dead rise surface | $\Delta /\left(B_{\mathrm{CG}^{2}} \mathrm{q}^{\prime}\right)$ | 1 |
| $C_{M}$ | CMSE | (fluid mechanics, lifting surfaces) Section moment coefficient |  | 1 |
| $C_{\text {m }}$ | CMS | (ships, hull geometry) Midship section coefficient (midway between forward and aft perpendiculars) | $A_{M} /(B T)$ | 1 |
| $C_{M}$ | CM | (hydrofoil boats) Pitching moment coefficient | $M /\left(\left(A_{\text {FF }}+A_{\text {FR }}\right)\left(l_{\mathrm{F}}-l_{\mathrm{R}}\right) q\right)$ | 1 |
| CmtL | CMTL | Longitudinal trimming coefficient | Trimming moment divided by change in trim which approximately equals $\overline{B M}_{L} / L$ | 1 |
| $C_{N}$ | CN | (ships, performance) Trial correction for propeller rate of revolution at speed identity | $n_{\mathrm{T}} / n_{\text {S }}$ | 1 |
| $C_{N P}$ | CNP | (ships, performance) Trial correction for propeller rate of revolution at power identity | $P_{\text {DT }} / P_{\text {DS }}$ | 1 |
| $C_{\text {P }}$ | CPL | (ships, hull geometry) Longitudinal prismatic coefficient | $\nabla /\left(A_{\mathrm{X}} L\right)$ or $\nabla /\left(A_{\mathrm{M}} L\right)$ | 1 |
| $C_{P}$ | CDP | (ships, performance) Trial correction for delivered power |  | 1 |
| $C_{P}$ | CPD | (ships, propulsor performance) Power loading coefficient | $P_{\mathrm{D}} /\left(A_{\mathrm{P}} q_{\mathrm{A}} V_{\mathrm{A}}\right)$ | 1 |
| $C_{p}$ | CP | (ships, hull resistance, water jets) Local pressure coefficient | $\left(p-p_{0}\right) /\left(\rho V^{2} / 2\right)$ | 1 |
| $C_{\text {PA }}$ | CPA | (ships, hull geometry) Prismatic coefficient, after body | $\begin{aligned} & \nabla_{\mathrm{A}} /\left(A_{\mathrm{X}} L / 2\right) \text { or } \\ & \nabla_{\mathrm{A}} /\left(A_{\mathrm{M}} L / 2\right) \\ & \hline \end{aligned}$ | 1 |
| CPE | CPE | (ships, hull geometry) Prismatic coefficient, entrance | $\begin{aligned} & \nabla_{\mathrm{E}} /\left(A_{\mathrm{X}} L_{\mathrm{E}}\right) \text { or } \\ & \nabla_{\mathrm{E}} /\left(A_{\mathrm{M}} L_{\mathrm{E}}\right) \\ & \hline \end{aligned}$ | 1 |

Version 2021
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| $C_{\text {PF }}$ | CPF | (ships, hull geometry) Prismatic coefficient fore body | $\begin{aligned} & \nabla_{\mathrm{F}} /\left(A_{\mathrm{X}} L / 2\right) \text { or } \\ & \nabla_{\mathrm{F}} /\left(A_{\mathrm{M}} L / 2\right) \end{aligned}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $C_{p i}$ | CPI | (sailing vessels) Center of pressure for $\mathrm{A}_{\mathrm{i}}$ |  | 1 |
| $C_{\text {PR }}$ | CPR | (ships, hull resistance) Pressure resistance coefficient, including wave effect | $R_{P} /(S q)$ | 1 |
| $C_{\text {PR }}$ | CPR | (ships, hull geometry) Prismatic coefficient, run | $\begin{aligned} & \nabla_{\mathrm{R}} /\left(A_{\mathrm{x}} L_{\mathrm{R}}\right) \text { or } \\ & \nabla_{\mathrm{R}} /\left(A_{\mathrm{M}} L_{\mathrm{R}}\right) \end{aligned}$ | 1 |
| $C_{\text {PR }}$ | CPR | (ACV and SES) Aerodynamic profile drag coefficient | $R_{0} /\left(\rho_{\mathrm{A}} V_{\mathrm{R}}{ }^{2} A_{\mathrm{C}} / 2\right)$ | 1 |
| $C_{P \mathrm{~V}}$ | CPV | (ships, hull resistance) Viscous pressure resistance coefficient | $R_{P V} /(S q)$ | 1 |
| $C^{*}{ }^{*}$ | CQS | (ships, propulsor performance) Torque index | $Q /\left(A_{\mathrm{P}} q_{\mathrm{s}} D\right)$ | 1 |
| CR | CR | (fundamental, statistical, stochastic) Population covariance |  |  |
| $C_{\text {R }}$ | CR | (ships, hull resistance) Residuary resistance coefficient | $R_{\mathrm{R}} /(S q)$ | 1 |
| $C_{r}$ | CRA | (environmental mechanics, waves) Average reflection coefficient |  | 1 |
| $C_{r}$ | CRDS | (ships, manoeuvrability, seakeeping) Directional stability criterion | $Y_{v}\left(N_{r}-m u x_{G}\right)-N_{v}\left(Y_{r}-m u\right)$ | $\mathrm{N}^{2} \mathrm{~s}^{2}$ |
| $C_{\mathrm{r}}(f)$ | CRF | (environmental mechanics, waves) Reflection coefficient amplitude function |  | 1 |
| $C_{\text {RU }}$ | CRU | (sailing vessels) Residuary resistance coefficient (upright) | $R_{\text {RU }} /(S q)$ | 1 |
| CS | CS | (fundamental, statistical, stochastic) Sample covariance |  |  |
| Cs | CSR | (ships, hull resistance) Spray resistance coefficient | $R_{\text {S }} /(S q)$ | 1 |
| Cs | CS | (ships, hull geometry) Wetted surface coefficient | $S /(\nabla L)^{1 / 2}$ | 1 |
| $C_{\text {s }}$ |  | (seakeeping, large amplitude motions capsizing) Shape coefficient, depending on the shape of the structural member exposed to the wind |  | 1 |

ITTC Symbols

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| $C_{\text {STC }}$ | CSTC | Thickness Cord Ratio of Strut |  | 1 |
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| $C_{\text {T }}$ | CT | (ships, hull resistance) Total resistance coefficient | $R_{\mathrm{T}} /(S q)$ | 1 |
| $C_{T}{ }^{*}$ | CTHS | (ships, propulsor performance) Thrust index | $T /\left(A_{\mathrm{P}} q_{S}\right)$ | 1 |
| $C_{\text {Th }}$ | CTH | (ships, propulsor performance) Thrust loading coefficient, energy loading coefficient | $T /\left(A_{\mathrm{P}} q_{A}\right)=\left(T_{\mathrm{P}} / A_{\mathrm{P}}\right) / q_{\mathrm{A}}$ | 1 |
| $C_{\text {TL }}$ | CTLT | (ships, hull resistance) Telfer's resistance coefficient | $g R L /\left(\Delta V^{2}\right)$ | 1 |
| $C_{\text {Tn }}$ |  | (ships, hull resistance, water jets) Thrust loading coefficient: | $\frac{T_{\text {net }}}{\frac{1}{2} \rho U_{0}^{2} A_{\mathrm{n}}}$ | 1 |
| $C_{\text {TQ }}$ | CTQ | (ships, hull resistance) Quali fied resistance coefficient | $C_{T \nabla /}\left(\eta_{\mathrm{H}} \eta_{\mathrm{R}}\right)$ | 1 |
| $C_{\text {TU }}$ | CTU | (sailing vessels) Total resistance coefficient (upright) | $R_{\text {TU }} /(S q)$ | 1 |
| $C_{\text {TV }}$ | CTVOL | (ships, hull resistance) Resistance displacement | $R_{\mathrm{T}} /\left(\nabla^{2 / 3} q\right)$ | 1 |
| $C_{\text {T } \varphi}$ | CTPHI | (sailing vessels) Total resistance coefficient with heel and leeway | $R_{\text {T } \varphi} /(S q)$ | 1 |
| Cuv | SI(U,V) | (ships, unsteady propeller forces) Generalized stiffness |  |  |
| $C_{\mathrm{V}}$ | CV | (ships, hull resistance) Total viscous resistance coefficient | $R_{\mathrm{V}} /(\mathrm{S} q)$ | 1 |
| $C_{\mathrm{v}}$ | CSP | (planing, semi-displacement vessels) Froude number based on breadth | $V /\left(B_{\text {CG }} g\right)^{1 / 2}$ | 1 |
| $C_{\text {VP }}$ | CVP | (ships, hull geometry) Prismatic coefficient vertical | $\nabla /\left(A_{w} T\right)$ | 1 |
| $C_{\text {w }}$ | CW | (ships, hull resistance) Wave making resistance coefficient | $R_{\mathrm{W}} /(\mathrm{Sq}$ ) | 1 |
| $C_{\text {WA }}$ | CWA | (ships, hull geometry) Water plane area coefficient, aft | $A_{\mathrm{WA}} /(B L / 2)$ | 1 |
| Cwc | CWC | (ACV and SES) Cushion wave making coefficient |  | 1 |
| $C_{\text {WF }}$ | CWF | (ships, hull geometry) Water plane area coefficient, forward | $A_{\text {wF }} /(B L / 2)$ | 1 |
| CWp | CW | (ships, hull geometry) Water plane area coefficient | Awp /(L B) | 1 |

Version 2021

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| $C_{\text {WP }}$ | CWP | (ships, hull resistance) Wave pattern resistance coefficient, by wave analysis |  | 1 |
| :---: | :---: | :---: | :---: | :---: |
| Cwu | CWU | (sailing vessels) Wave resistance coefficient (upright) |  | 1 |
| $C_{\mathrm{X}}$ | CX | (ships, hull geometry) Maximum transverse section coefficient | $A_{\mathrm{X}} /(B T)$, where B and T are measured at the position of maximum area | 1 |
| Cx | CXA | (ships, hull resistance) Air or wind resistance coefficient, usually from wind tunnel tests | $-R_{\mathrm{AA}} /\left(A_{\mathrm{v}} q_{\mathrm{R}}\right)$ | 1 |
| $C^{1}$ |  | (sailing vessels) Force coefficients |  | 1 |
| $C_{x x}$ | XXCR | (fundamental, statistical, stochastic) Auto-covariance of a stationary stochastic process | $\left(x(t)-x^{E}\right)\left(x(t+\tau)-x^{E}\right)^{E}$ |  |
| $C_{x y}$ | XYCR | (fundamental, statistical, stochastic) Cross-covariance of two stationary stochastic processes | $\left(x(t)-x^{E}\right)\left(y(t+\tau)-y^{E}\right)^{E}$ |  |
| Cy |  | (sailing vessels) Force coefficients |  | 1 |
| $C_{z}$ |  | (sailing vessels) Force coefficients |  | 1 |
| C ${ }^{\text {r }}$ | CVOL | (ships, hull geometry) Volumetric coefficient | $\nabla / L^{3}$ | 1 |
| $C_{\Delta}$ | CDL | (planing, semi-displacement vessels) Load coefficient | $\Delta /\left(B_{C G}{ }^{3} \rho g\right)$ | 1 |
| $C_{4}$ | CLOAD | (ACV and SES) Cushion loading coefficient | $\Delta /\left(g \rho_{\mathrm{A}} A_{\mathrm{C}}{ }^{3 / 2}\right)$ | 1 |
| c | CS | (fluid mechanics, flow parameter) Velocity of sound | $(E / \rho)^{1 / 2}$ | m/s |
| $C_{0.7}$ | C07 | (ships, propulsor geometry, appendage geometry)Chord length | Chord length at $\mathrm{r} / \mathrm{R}=0.7$ | m |
| c | CH, LCH | (ships, propulsor geometry, appendage geometry) Chord length, chord length of a foil section |  | m |
| cc | CHC | (hydrofoil boats) Chord length at centre plane |  | m |
| $c_{\text {F }}$ | CFL | (hydrofoil boats) Chord length of flap |  | m |

Version 2021

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| $C_{\text {es }}$ |  | (ships, hull resistance, water jets) Energy velocity coefficient at station $s$ |  | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{\mathrm{FT}}$ | CHTI | (hydrofoil boats) Chord length at foil tips |  | m |
| $C_{G}$ | VG | (environmental mechanics, waves) Wave group velocity or celerity | The average :rate of advance of the energy in a finite train of gravity waves | m/s |
| $c_{i}$ |  | (uncertainty) Sensitivity coefficient | $c_{i}=\partial f / \partial x_{i}$. | 1 |
| $c_{\text {LE }}$ | CHLE | (ships, geometry and hydrostatics, propulsor geometry) Chord, leading part | The part of the Chord delimited by the Leading Edge and the intersection between the Generator Line and the pitch helix at the considered radius | m |
| $c_{\mathrm{M}}$ | CHM, CHME | (ships, appendage geometry, propulsor geometry, fluid mechanics, lifting surfaces hydrofoil boats) <br> Mean chord length | The expanded or developed area of a propeller blade divided by the span from the hub to the tip, $A_{\text {RT }} / S$ | m |
| $c_{\text {ms }}$ |  | (ships, hull resistance, water jets) Momentum velocity coefficient at station $s$ |  | 1 |
| $C_{\text {PF }}$ | CPFL | (hydrofoil boats) Distance of centre of pressure on a foil or flap from leading edge |  | m |
| $c_{\text {R }}$ | CHRT | (fluid mechanics, lifting surfaces, ships, appendage geometry) Chord length at the root |  | m |
| cs | CS | (ships, propulsor geometry) <br> Skew displacement | The displacement between middle of chord and the blade reference line. Positive when middle chord is at the trailing side regarding the blade reference line | m |
| Cs | CSTR | (hydrofoil boats) Chord length of a strut |  | m |
| CSF | CHSF | (hydrofoil boats) Chord length of strut at intersection with foil |  | m |
| $c_{\text {T }}$ | CHTP | (ships, appendage geometry) Chord length at the tip |  | m |


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|  |  |  | The part of the Chord de- <br> limited by the Trailing Edge <br> and the intersection between <br> the Generator Line and the <br> pitch helix at the considered <br> radius |
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ITTC Symbols
Version 2021
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| Explanation |


| D | DR | (fundamental, statistical, stochastic) Population deviation |  |  |
| :---: | :---: | :---: | :---: | :---: |
| D | DEP | (ships, hull geometry) Depth, moulded, of a ship hull |  | m |
| D | D, DI | (ships, basic quantities) Diameter |  | m |
| D | DP | (ships, propulsor geometry, propulsor performance) Propeller diameter |  | m |
| D | FF(1) | (ships, basic quantities) <br> Drag (force) | Force opposing translatory velocity, generally for a completely immersed body | N |
| D |  | (ships, propulsor geometry, water jets) Impeller diameter (maximum) |  | m |
| $D_{0}$ | DC0 | (ships, manoeuvrability, turning circles) Inherent steady turning diameter $\delta_{\mathrm{R}}=\delta_{0}$ |  | m |
| $D_{0}{ }^{\prime}$ | DC0N | (ships, manoeuvrability, turning circles) Non-dimensional inherent steady turning diameter | $D_{0} / L_{\text {PP }}$ | 1 |
| $D_{\text {c }}$ | DC | (ships, manoeuvrability, turning circles) Steady turning diameter |  | m |
| $D_{\text {c }}{ }^{\prime}$ | DCNO | (ships, manoeuvrability, turning circles) Non-dimensional steady turning diameter | $D_{\text {C }} / L_{\text {PP }}$ | 1 |
| $D_{\text {c }}$ | DC | (fluid mechanics, cavitation) Cavity drag |  | N |
| $D_{\text {F }}$ | DRF | (fluid mechanics, lifting surfaces, hydrofoil boats) Foil drag | Force in the direction of motion of an immersed foil | N |
| $D_{\text {fF }}$ | DFF | (hydrofoil boats) Drag force on front foil | $C_{\text {DF }} A_{\text {FF }} q$ | N |
| $D_{\text {FR }}$ | DFA | (hydrofoil boats) Drag force on rear foil | $C_{\text {DF }} A_{\text {FR }} q$ | N |
| $D_{\text {H }}$ | DHUL | (multi-hull vessels) Hull diameter | Diameter of axis symmetric submerged hulls | m |
| $D^{\mathrm{h}}{ }_{u v}$ | DH(U,V) | (ships, basic quantities), Generalized hydrodynamic damping | $\partial F^{\mathrm{h}}{ }_{u} / \partial V_{v}$ |  |

## ITTC Symbols

Version 2021
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| $D_{\text {I }}$ | DRIND | (fluid mechanics, lifting surfaces, hydrofoil boats) Induced drag | For finite span foil, the component of lift in the direction of motion | N |
| :---: | :---: | :---: | :---: | :---: |
| $D_{\text {INT }}$ | DRINT | (fluid mechanics, lifting surfaces, hydrofoil boats) Interference drag | Due to mutual interaction of the boundary layers of intersecting foil | N |
| $D_{\text {n }}$ |  | (ships, propulsor geometry, water jets) Nozzle discharge diameter |  | m |
| $D_{\text {P }}$ | DRSE | (fluid mechanics, lifting surfaces) Section or profile drag at zero lift | Streamline drag | N |
| Dp |  | Pressure differential of flow rate transducer |  | Pa |
| $D_{\text {P0 }}$ | DRF0 | (hydrofoil boats) Profile drag for angle of attack equal to zero lift | Streamline drag | N |
| $D_{\text {Pb }}$ | DPB | Maximum Diameter of Pod Body |  | m |
| DR | DR | (fundamental, statistical, stochastic) Population deviation |  |  |
| DS | DS | (fundamental, statistical, stochastic) Sample deviation |  |  |
| $D_{\text {SP }}$ | DRSP | (hydrofoil boats) Spray drag | Due to spray generation | N |
| $D_{\text {ST }}$ | DRST | (hydrofoil boats) Strut drag |  | N |
| $D_{u v}$ | DA(U,V) | (ships, unsteady propeller forces) Generalized damping |  |  |
| $D_{\mathrm{V}}$ | DRVNT | (hydrofoil boats) Ventilation drag | Due to reduced pressure at the rear side of the strut base | N |
| $\mathrm{D}_{\mathrm{w}}$ | DRWA | (hydrofoil boats) Wave drag | Due to propagation of surface waves | N |
| $D_{\text {x }}$ | DX | (multi-hull vessels) Hull diameter at the longitudinal position "X" |  | m |
| $D_{\mathrm{x}}(f, \theta)$, <br> $D_{\mathrm{X}}(\omega, \mu)$, | DIRSF | (environmental mechanics, waves) Directional spreading function | $S(f, \theta)=S(f) D_{\mathrm{x}}(f, \theta)$ where $\int_{0}^{2 \pi} D_{\mathrm{x}}(f, \theta) d \theta=1$ | rad |
| d | D, DI | (ships, basic quantities) <br> Diameter |  | m |
| d | DIDR | (underwater noise) Distance hydrophone to acoustic centre |  | m |

## ITTC Symbols

Version 2021
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| d | T | (ships, hull geometry seakeeping, large amplitude motions capsizing)) Draught, moulded, of ship hull |  | m |
| :---: | :---: | :---: | :---: | :---: |
| d |  | (seakeeping, large amplitude motions capsizing) Density coefficient for submerged test weights |  | 1 |
| $d_{\text {A }}$ | TA, TAP | (ships, hull geometry) <br> Draught at aft perpendicular |  | m |
| $d_{\text {D }}$ | CLEARD | (ships, propulsor geometry) Propeller tip clearance | Clearance between propeller tip and inner surface of duct | m |
| $d_{\text {F }}$ | TF, TFP | (ships, hull geometry) Draught at forward perpendicular |  | m |
| $d_{\text {h }}$ | DH | (ships, propulsor geometry) Boss or hub diameter | $2 r_{h}$ | m |
| $d_{\text {ha }}$ | DHA | Hub diameter, aft | Aft diameter of the hub, not considering any shoulder | m |
| $d_{\text {hf }}$ | DHF | Hub diameter, fore | Fore diameter of the hub, not considering any shoulder | m |
| $d_{\text {KL }}$ | KDROP | (ships, hull geometry) Design drop of the keel line | $T_{\text {AD }}-T_{\text {FD }}$ alias "keel drag" | m |
| $d_{\text {M }}$ | TM, TMS | (ships, hull geometry) Draught at midship | $\left(T_{\mathrm{A}}+T_{\mathrm{F}}\right) / 2$ for rigid bodies with straight keel | m |
| $d_{\text {TR }}$ | DTRA | (planing, semi-displacement vessels) Immersion of transom, underway | Vertical depth of trailing edge of boat at keel below water surface level | m |
| $d_{t \psi}$ | YART | (ships, manoeuvrability) Rate of change of course | $d \psi / d t$ | rad/s |

Version 2021

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| $E$ | EL | (fluid mechanics, flow parameter) Modulus of elasticity |  | Pa |
| :---: | :---: | :---: | :---: | :---: |
| E | EM | Mainsail base |  | m |
| $E$ | MR | (fundamental, statistical, stochastic) Expectation, population mean |  |  |
| $E$ | E, EN | (ships, basic quantities) Energy |  | J |
| E | EM | (sailing vessels) Mainsail base |  | m |
| $E_{\text {I }}$ | MEI | (environmental mechanics, ice) Modulus of elasticity of ice |  | Pa |
| $E_{\text {s }}$ |  | (ships, hull resistance, water jets) Total energy flux at station s (kinetic + potential + pressure) | $\iint_{A_{j}} \rho\left(\frac{1}{2} \boldsymbol{u}^{2}+\frac{p}{\rho}-g_{j} x_{j}\right) u_{i} n_{i} d A$ | W |
| $E_{s \xi}$ |  | (ships, hull resistance, water jets) Total axial (in $\xi$ direction) energy flux at station s | $\iint_{A_{j}} \rho\left(\frac{1}{2} u_{\xi}^{2}+\frac{p}{\rho}-g_{j} x_{j}\right) u_{i} n_{i} d A$ | W |
| $e$ | ED | (fluid mechanics, flow fields) Density of total flow energy | $\rho V^{2} / 2+p+\rho g h$ | Pa |
| $e_{\text {A }}$ | ENAPP | (planing, semi-displacement vessels) Lever of appendage lift force $N_{\mathrm{A}}$ | Distance between $N_{\mathrm{A}}$ and centre of gravity (measured normally to $N_{\mathrm{A}}$ ) | m |
| $e_{B}$ | ENBOT | (planing, semi-displacement vessels) Lever of bottom normal force $N_{\mathrm{B}}$ | Distance between $N_{\mathrm{B}}$ and centre of gravity (measured normally to $N_{\mathrm{B}}$ ) | m |
| $e_{\text {PN }}$ | ENPN | (planing, semi-displacement vessels) Lever of propeller normal force $N_{\text {PN }}$ | Distance between propeller centreline and centre of gravity (measured along shaft line) | m |
| $e_{\text {PP }}$ | ENPP | (planing, semi-displacement vessels) Lever of resultant of propeller pressure forces $N_{\text {PP }}$ | Distance between $N_{\mathrm{PP}}$ and centre of gravity (measured normally to $N_{\mathrm{PP}}$ ) | m |
| $e_{\text {PS }}$ | ENPS | (planing, semi-displacement vessels) Lever of resultant propeller suction forces $N_{\text {PS }}$ | Distance between $N_{P S}$ and centre of gravity (measured normal to $N_{\mathrm{PS}}$ ) | m |
| $e_{\text {R } P}$ | ENRP | (planing, semi-displacement vessels) Lever of resultant of rudder pressure forces $N_{\mathrm{R} P}$ | Distance between $N_{\mathrm{R} P}$ and centre of gravity (measured normal to $N_{\mathrm{R} P}$ ) | m |


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| $F$ | CQF | (fluid mechanics, boundary layers) Entrainment factor | $1 /\left(U_{\mathrm{e}} d Q / d x\right)$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $F$ | FB | (hull geometry) Fore body |  |  |
| $F$ | FETCH | (environmental mechanics, wind) Fetch length | Distance over water the wind blows | m |
| $F$ | F, F0 | (ships, basic quantities) Force |  | N |
| $F$ |  | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Centre of flotation of the water plane |  |  |
| $F$ |  | (seakeeping, large amplitude motions capsizing) Wind force - IMO/IS |  |  |
| $F^{0}$ | F, F0 | (ships, basic quantities) Force |  | N |
| $F^{0}{ }_{1}$ | $\begin{aligned} & \hline F X, \\ & F 0(1), F(1) \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis $x$ |  | N |
| $F^{0}{ }_{2}$ | $\begin{aligned} & \mathrm{FY}, \\ & \mathrm{FO}(2), \mathrm{F}(2) \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis y |  | N |
| $F^{0}{ }_{3}$ | $\begin{aligned} & \mathrm{FZ}, \\ & \mathrm{FO}(3), \mathrm{F}(3) \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis z |  | N |
| $F_{1}$ | $\begin{aligned} & \text { FX, } \\ & \text { F0(1), F(1) } \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis $x$ |  | N |
| $F^{1}$ | F1 | (ships, basic quantities) Moment of forces | First order moment of a force distribution | Nm |
| $F^{1}{ }_{1}$ | F1(1), F(4) | (solid body mechanics, loads) Moment around body axis $x$ |  | Nm |
| $F^{1}{ }_{2}$ | F1(2), F(5) | (solid body mechanics, loads) Moment around body axis y |  | Nm |
| $F^{1}{ }_{3}$ | F1(3), F(6) | (solid body mechanics, loads) Moment around body axis z |  | Nm |
| $F_{2}$ | $\begin{aligned} & \text { FY, } \\ & \text { FO(2), F(2) } \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis y |  | Nm |
| $F_{3}$ | $\begin{aligned} & \mathrm{FZ}, \\ & \mathrm{FO}(3), \mathrm{F}(3) \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis z |  | Nm |


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| Symbol | Symbol | Name | Definition or <br> Explanation | SI- |
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| $F_{4}$ | F1(1), F(4) | (solid body mechanics, loads) Moment around body axis $X$ |  | Nm |
| :---: | :---: | :---: | :---: | :---: |
| $F_{5}$ | F1(2), F(5) | (solid body mechanics, loads) Moment around body axis y |  | Nm |
| $F_{6}$ | F1(3), F(6) | (solid body mechanics, loads) Moment around body axis z |  | Nm |
| $F B$ | XFB | (seakeeping, large amplitude motions capsizing) Longitudinal centre of buoyancy, $L_{\text {CB }}$, from forward perpendicular | Distance of centre of buoyancy from forward perpendicular | m |
| $F^{C}$ | CIRCF | (ships, hull resistance) R.E. Froude's frictional resistance coefficient | $1000 R_{\mathrm{F}} /\left(4\left(K^{C}\right)^{2}\right)$ | 1 |
| $F_{\text {D }}$ | SFC | Friction deduction force in self-propulsion test. Skin friction correction in a selfpropulsion test carried out at the ship self-propulsion point | Towing force applied to a model to correct the model resistance for different $R e$ between model and full scale. | N |
| $\overline{F F}$ | XFF | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of floatation, $L_{\text {CF, }}$ from forward perpendicular | Distance of centre of flotation from forward perpendicular | m |
| $F^{F}{ }_{1}$ | FF(1) | (ships, basic quantities) Resistance, Drag (force) | Force opposing translatory velocity, generally for a completely immersed body | N |
| $F^{F}{ }_{2}$ | FF(2) | (ships, basic quantities) Cross force | Force normal to lift and drag (forces) | N |
| $F^{F}{ }_{3}$ | FF(3) | (ships, basic quantities) Lift (force) | Force perpendicular to translatory velocity | N |
| $\overline{F G}$ | XFG | (ships, hydrostatics, stability) Longitudinal centre of gravity from forward perpendicular | Distance of centre of gravity from forward perpendicular | m |
| $\overline{F G}$ | XFG | (seakeeping, large amplitude motions capsizing) Longitudinal centre of gravity, from forward perpendicular | Distance of centre of gravity from forward perpendicular | m |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $F_{\text {H }}$ |  | (sailing vessels) Heeling force of sails |  | N |
| :---: | :---: | :---: | :---: | :---: |
| $F^{\mathrm{h}}$ | FH(U) | (solid body mechanics, inertial and hydro properties) Generalized hydrodynamic force |  | N |
| $F_{\text {IN }}$ | FNIC | (ice going vessels) Normal ice force on a body | Projection of hull - ice interaction force on the external normal | N |
| $F_{\text {IT }}$ | FTIC | (ice going vessels) Tangential ice force on a body | Projection of the hull - ice interaction force on the direction of motion | N |
| $F_{i}$ | F(I) | (ships, unsteady propeller forces) Vibratory force | $i=1,2,3$ | N |
| $F_{\mathrm{L}}$ | FS(2) | (ships, seakeeping) Wave excited lateral shear force | Alias horizontal! | N |
| $F_{\mathrm{N}}$ | FS(3) | (ships, seakeeping) Wave excited normal shear force | Alias vertical!Remark2419 | N |
| FP | FP | (hull geometry) Fore perpendicular |  |  |
| $F_{\text {P }}$ | FP | (ships, performance) Force pulling or towing a ship |  | N |
| $F_{\text {P0 }}$ | FP0 | (ships, performance) Pull during bollard test |  | N |
| Fr | FN | (fluid mechanics, flow parameter) Froude number | $V /(g L)^{1 / 2}$ | 1 |
| $F_{\text {R }}$ |  | (sailing vessels) Driving force of sails |  | N |
| Fr ${ }_{\text {c }}$ | FNC | (hydrofoil boats) Froude number based on chord length | $V /\left(g c_{M}\right)^{1 / 2}$ | 1 |
| $F r_{h}$ | FH | (fluid mechanics, flow parameter) Froude depth number | $V /(g h)^{1 / 2}$ | 1 |
| $F r_{\text {I }}$ | FNIC | (ice going vessels) Froude number based on ice thickness | $V /\left(g h_{\mathrm{I}}\right)^{1 / 2}$ | 1 |
| $F r_{L}$ | FNFD | (hydrofoil boats) Froude number based on foil distance | $V /\left(g L_{F}\right)^{1 / 2}$ | 1 |
| Fr ${ }^{\text {r }}$ | FV | (fluid mechanics, flow parameter) Froude displacement number | $V /\left(g \nabla^{1 / 3}\right)^{1 / 2}$ | 1 |
| $F^{\text {S }}$ | FS(I) | (solid body mechanics, loads) Shearing force | $F^{S 0}{ }_{2}, F^{S 0}{ }_{3}$ | N |


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| Symbol | Name | Definition or <br> Explanation | SI- <br> Symbol |  |


| $F^{\text {S }}{ }_{u}$ | FS(U) | (solid body mechanics, loads) Force or load acting at a given planar cross-section of the body, generalized, in section coordinates! | $\left\lvert\, \begin{aligned} & F_{i}^{S}=F^{S 0}{ }_{i} \\ & F^{S_{3+i}}=F^{S 1}{ }_{i}=M^{B}{ }_{i} \end{aligned}\right.$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{Nm} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| $F^{\mathrm{T}}$ | $\begin{array}{\|l} \hline \text { FT, } \\ \text { FS(1) } \end{array}$ | (solid body mechanics, loads) Tensioning or normal force | $F^{S 0}{ }_{1}$ | N |
| $F_{\text {TA }}$ | FTAPP | (planing, semi-displacement vessels) Appendage drag force (parallel to reference line) | Drag forces arising from appendages inclined to flow, assumed to act parallel to the reference line | N |
| $F_{\text {TB }}$ | FTBOT | (planing, semi-displacement vessels) Bottom frictional force (parallel to reference line) | Viscous component of bottom drag forces assumed acting parallel to the reference line | N |
| $F_{\text {TK }}$ | FTKL | (planing, semi-displacement vessels) Keel or skeg drag force (parallel to reference line) | Drag forces arising from keel or skeg, assumed to act parallel to the reference line | N |
| $F_{\text {TRP }}$ | FTRP | (planing, semi-displacement vessels) Additional rudder drag force (parallel to reference line) | Drag forces arising from influence of propeller wake on the rudder assumed to act parallel to the reference line | N |
| $F_{u}$ | F(U) | (solid body mechanics, loads) Force, generalized, load, in body coordinates | $\begin{aligned} & M^{F}{ }_{u}=M^{M}{ }_{u} \\ & F_{i}=F^{0}{ }_{i} \\ & F_{3+i}=F_{i}^{1} \\ & \hline \end{aligned}$ | N |
| $F u$ | FG(I) | (ships, unsteady propeller forces) Generalized vibratory force | $\begin{aligned} & u=1, . ., 6 \\ & u=1,2,3: \text { force } \\ & u=4,5,6: \text { moment } \end{aligned}$ | $\begin{array}{\|l\|} \hline \mathrm{N} \\ \mathrm{~N} \\ \mathrm{Nm} \end{array}$ |
| $F_{\mathrm{V}}$ |  | (sailing vessels) Vertical force of sails |  | N |
| $F_{\text {XI }}$ | FXIC | (ice going vessels) Components of the local ice force |  | N |
| $F_{x}$ | XPF | (fundamental, statistical) Probability function (distribution) of a random quantity |  | 1 |
| $F_{X}$ | $\begin{aligned} & \text { FX, } \\ & \text { FO(1), F(1) } \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis $x$ |  | Nm |
| $F_{x y}$ | XYPF | (fundamental, statistical) Joint probability function (distribution) function of two random quantities |  | 1 |
| $F_{\text {YI }}$ | FYIC | (ice going vessels) Components of the local ice force |  | N |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $F_{y}$ | $\begin{aligned} & \text { FY, } \\ & \text { F0(2), F(2) } \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis y |  | N |
| :---: | :---: | :---: | :---: | :---: |
| $F_{\text {ZI }}$ | FZIC | (ice going vessels) Components of the local ice force |  | N |
| $F_{z}$ | $\begin{aligned} & \mathrm{FZ}, \\ & \mathrm{FO}(3), \mathrm{F}(3) \end{aligned}$ | (solid body mechanics, loads) Force in direction of body axis z |  | N |
| $f$ |  | (uncertainty) Function | Functional relationship between measurand $Y$ and input quantities $X_{i}$ on which $Y$ depends, and between output estimate $y$ and input estimates $x_{i}$ on which $y$ depends. | 1 |
| $f$ | FR | (fundamental, time and frequency domain quantity, ships, seakeeping, environmental mechanics, wave, ships, basic quantities) Frequency | $2 \pi \omega=1 / T$ | Hz |
| $f$ | FREB | (ships, hull geometry, hydrostatics, stability, seakeeping, large amplitude motions, capsizing) <br> Freeboard | From the freeboard markings to the freeboard deck, according to official rules | m |
| $f$ | FBP | (ships, propulsor geometry) Camber of a foil section |  | m |
| $f$ | FM | (ships, appendage geometry) Camber of an aerofoil or a hydrofoil | Maximum separation of median and nose-tail line | m |
| $f$ | FC | (ships, hull resistance) Friction coefficient | Ratio of tangential force to normal force between two sliding bodies | 1 |
| $f_{\text {AA }}$ | FRAA | (planing, semi-displacement vessels) <br> Lever of wind resistance $R_{\text {AA }}$ | Distance between $R_{\mathrm{AA}}$ and centre of gravity (measured normal to $R_{\mathrm{AA}}$ ) | m |
| $f_{\text {AP }}$ | FRAP | (planing, semi-displacement vessels) Lever of appendage drag $R_{A \mathrm{P}}$ | Distance between $R_{\text {AP }}$ and centre of gravity (measured normal to $R_{\mathrm{AP}}$ ) | m |
| $f_{\text {BL }}$ | CABL | (ships, hull geometry) Area coefficient for bulbous bow | $A_{\text {BL }} /(L T)$ | 1 |
| $f_{\text {BT }}$ | CABT | (ships, hull geometry) Taylor sectional area coefficient for bulbous bow | $A_{\text {Bt }} / A_{\mathrm{X}}$ | 1 |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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|  | FC | (fundamental, time and fre- <br> quency domain quantity) <br> Basic frequency in repeating <br> functions | $1 / T_{\mathrm{C}}$ | Hz |
| :--- | :--- | :--- | :--- | :--- |
| $f_{\mathrm{C}}$ | FD | (ships, propulsor geometry) <br> Camber of duct profile |  | m |
| $f_{\mathrm{E}}$ | FE | (ships, seakeeping) Fre- <br> quency of wave encounter | $1 / T_{\mathrm{E}}$ | Hz |
| $f_{\mathrm{F}}$ | CFR | (planing, semi-displacement <br> vessels) Lever of frictional <br> resistance $R_{\mathrm{F}}$ | Distance between $R_{\mathrm{F}}$ and <br> centre of gravity (measured <br> normal to $\left.R_{\mathrm{F}}\right)$ | m |
| $f_{\mathrm{ID}}$ | (ice going vessels) Coeffi- <br> cient of friction between sur- <br> face of body and ice (dy- <br> namic) | Ratio of tangential force to <br> normal force between two <br> bodies (dynamic condition) | 1 |  |
| $f_{\mathrm{IS}}$ | FFRS | (ice going vessels) Coeffi- <br> cient of friction between sur- <br> face of body and ice (static | The same as above (static <br> condition) | 1 |
| $f_{i}$ | (fluid mechanics, flow fields) <br> Mass specific force | Strength of force fields, usu- <br> ally only gravity field gi | $\mathrm{m} / \mathrm{s}^{2}$ |  |
| $f_{\mathrm{K}}$ | FRK | (planing, semi-displacement <br> vessels) Lever of skeg or <br> keel resistance $R_{\mathrm{K}}$ | Distance between $R_{\mathrm{K}}$ and <br> centre of gravity (measured <br> normal to $\left.R_{\mathrm{K}}\right)$ | m |
| $f_{\mathrm{L}}$ | FRL | (fluid mechanics, lifting sur- <br> faces) Camber of lower side <br> (general) | FR |  |

## ITTC Symbols

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $f_{\text {T }}$ | ATR | (ships, hull geometry) Sectional area coefficient for transom stern | $A_{\mathrm{T}} / A_{\mathrm{X}}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $f$ u | FMU | (fluid mechanics, lifting surfaces) Camber of upper side |  | m |
| $f_{\text {w }}$ | FW | (environmental mechanics, waves) Basic wave frequency | $1 / T_{\mathrm{W}}$ | Hz |
| $f_{w}$ | FWE | (ships,performance) Weather factor, a non-dimensional coefficient indicating the decrease of speed in representative sea conditions | $\left\{\begin{array}{l} f_{\mathrm{w}} \\ =\frac{\text { speed in wind and waves }}{\text { speed in calm water }} \\ =\frac{V_{\mathrm{w}}}{V_{\text {ref }}} \end{array}\right.$ | 1 |
| $f_{\text {wi }}$ | FW(I) | (environmental mechanics, waves) Frequencies of harmonic components of a periodic wave | $i f_{W}$ | Hz |
| $f_{x}$ | XPD | (fundamental, statistical) Probability density of a random quantity | $d F_{x} / d x$ |  |
| $f_{x y}$ | XYPD | (fundamental, statistical) Joint probability density of two random quantities | $\partial^{2} F_{x y} /(\partial x \partial y)$ |  |
| $f_{z}$ |  | (ships, seakeeping) Natural frequency of heave | $1 / T_{z}$ | Hz |
| $f_{\theta}$ |  | (ships, seakeeping) Natural frequency of pitch | $1 / T_{\theta}$ | Hz |
| $f_{\varphi}$ |  | (ships, seakeeping) Natural frequency of roll | $1 / T_{\varphi}$ | Hz |

## ITTC Symbols

Version 2021

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$| Nefinition or |
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| G |  | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Centre of gravity of a vessel |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $G^{0}{ }_{i}, G_{i}$ | G0(I) | (solid body mechanics, loads) Gravity or weight force in body coordinates! | $\begin{aligned} G_{i}=G_{i}^{0} & =m^{0}{ }_{i j} g_{j} \\ & =m g_{i} \end{aligned}$ | N |
| $G^{1}{ }_{i}$ | G1(I) | (solid body mechanics, loads) Gravity or weight moment in body coordinates! | $\begin{aligned} G_{3+i}=G^{1}{ }_{i} & =\varepsilon_{i k j} x_{k} G^{0}{ }_{j} \\ & =m^{1}{ }_{i j} g_{j} \end{aligned}$ | Nm |
| $\overline{G G}_{1}$ | GGV | (seakeeping, large amplitude motions capsizing) Vertical stability lever caused by a weight shift or weight addition | $\overline{K G}_{1}=\overline{K G}_{0}+\overline{G G}_{1}$ | m |
| $\overline{G G}_{\mathrm{H}}$ | GGH | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Horizontal stability lever caused by a weight shift or weight addition |  | m |
| $\overline{G G_{L}}$ | GGL | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Longitudinal stability lever caused by a weight shift or weight addition |  | m |
| $\overline{G G}_{\mathrm{V}}$ | GG1 | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Vertical stability lever caused by a weight shift or weight addition | $\overline{K G_{1}}=\overline{K G_{0}}+\overline{\mathrm{GG}}_{1}$ | m |
| $\overline{G M}$ | GM | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Transverse metacentric height | Distance of centre of gravity to the metacentre $\overline{G M}=\overline{K M}-\overline{K G}$ <br> (not corrected for free surface effect) | m |
| $\overline{G M}_{\text {EFF }}$ | GMEFF | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Effective transverse metacentric height | GM Corrected for free surface and/or free communication effects | m |

## ITTC Symbols

Version 2021
G, g

| ITTC | Computer |  |  |  |
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| Symbol | Name | Definition or <br> Explanation | SI- <br> Symbol |  |


| $\overline{G M_{L}}$ | GML | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Longitudinal metacentric height | Distance from the centre of gravity G to the longitudinal metacentre $\mathrm{M}_{L}$ $\overline{G M_{L}}=\overline{K M_{L}}-\overline{K G}$ | m |
| :---: | :---: | :---: | :---: | :---: |
| $G_{u}$ | G(U) | (solid body mechanics, loads) Gravity or weight force, generalized, in body coordinates! | $G_{u}=m_{u v} g_{v}$ | N |
| GZ |  | (seakeeping, large amplitude motions capsizing) Arm of static stability corrected for free surfaces - IMO/table |  | m |
| $\overline{G Z}$ | GZ | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Righting arm or lever | $\begin{aligned} & \overline{G Z}^{=} \overline{A Z}-\overline{A G}_{\mathrm{V}} \sin \varphi- \\ & \overline{A G}_{\mathrm{T}} \cos \varphi \end{aligned}$ | m |
| $\overline{G Z}_{\text {MAX }}$ | GZMAX | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Maximum righting arm or lever |  | m |
| $G_{\mathrm{z}}$ | GAP | (ships, propulsor geometry) Gap between the propeller blades | $2 \pi r \sin (\varphi) / \mathrm{z}$ | m |
| $g$ | G, GR | (ships, basic quantities) Acceleration of gravity | Weight force / mass, strength of the earth gravity field | $\mathrm{m} / \mathrm{s}^{2}$ |
| g |  | (seakeeping, large amplitude motions capsizing, ships, hydrostatics, stability) Centre of gravity of an added or removed weight (mass) |  | 1 |
| $g^{E}$ | GMR | (fundamental, statistical) Expected value of a function of a random quantity | $\begin{array}{r} E(g)=\int_{x} g(x) f_{x}(x) d x \\ x=-\infty \ldots \infty \end{array}$ |  |
| $g_{i}$ | G1(I) | (solid body mechanics, loads) Gravity field strength, in body coordinates! |  | $\mathrm{m} / \mathrm{s}^{2}$ |
| $g^{M}$ | GMR | (fundamental, statistical) <br> Expected value of a function of a random quantity | $\begin{array}{r} E(g)=\int \\ x=-\infty \ldots \infty \end{array}$ |  |
| $g^{M R}$ | GMR | (fundamental, statistical) <br> Expected value of a function of a random quantity | $\begin{array}{r} E(g)=\int g(x) f_{x}(x) d x \\ x=-\infty \ldots \infty \end{array}$ |  |

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Computer <br>
Symbol

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| $g^{M R}$ | $G M R$ | (fundamental, statistical, <br> stochastic) Mean of a func- <br> tion of a random quantity | $M(g(t))=\lim \left(1 / T \int g(t) d t\right)$ <br> $t=-T / 2 \ldots+T / 2$ <br> $T=-\infty \ldots+\infty$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $g^{M \mathrm{~S}}$ | $G M S$ | (fundamental, statistical, <br> stochastic) Average or sam- <br> ple mean of a function of a | $A(g(t))=1 / T \int g(t) d t$ <br> random quantity | t=0 $\ldots+T$ |
| $g_{\mathrm{u}}$ | G(U) | solid body mechanics, <br> loads) Gravity field strength, <br> generalized, in body coordi- <br> nates | $g_{i}=g^{1}{ }_{i}$ <br> $g_{3+i}=0$ | $\mathrm{~m} / \mathrm{s}^{2}$ |

Version 2021

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Symbol |  | SI- |


| H | HT | (fluid mechanics, flow fields) Total head | $e / w=h+p / w+q / w$ | m |
| :---: | :---: | :---: | :---: | :---: |
| H | HT | (ships, basic quantities) <br> Height |  | m |
| H | HBL | (fluid mechanics, boundary layers) Boundary layer shape parameter | $\delta^{*} / \Theta$ | 1 |
| H |  | (sailing vessels) Side force |  | N |
| $H_{1}$ | HT1 | (ships, hull resistance, water jets) Local total head at station 1 |  | m |
| $H_{35}$ | H35 | (ships, hull resistance, water jets) Mean increase of total head across pump and stator or several pump stages |  | m |
| $H_{\text {CG }}$ | HVCG | (ACV and SES) Height of centre of gravity above mean water plane beneath craft |  | m |
| $H_{\text {DK }}$ | HCLDK | (multi-hull vessels) Deck clearance | Minimum clearance of wet deck from water surface at rest | m |
| $H_{\text {d }}$ | HD | (environmental mechanics, waves) Wave height by zero down-crossing | The vertical distance between a crest and a successive trough. | m |
| $H_{\text {E }}$ | HQF | (fluid mechanics, boundary layers) Entrainment shape parameter | $\left(\delta-\delta^{*}\right) / \Theta$ | 1 |
| $H_{H}$ | HH | (ACV and SES) Vertical spacing between inner and outer side skirt hinges or attachment points to structure | needs clarification | m |
| $H_{i j}$ |  | (ships, propulsor geometry, water jets) Head between station $i$ and $j$ |  | m |
| $H_{\text {JS }}$ |  | (ships, propulsor geometry, water jets) Jet System Head | $\frac{P_{\mathrm{JSE}}}{Q_{\mathrm{J}}}$ | m |
| HL |  | (seakeeping, large amplitude motions capsizing) Heeling lever (due to various reasons) - IMO/HSC'2000 |  |  |
| $H_{\text {mo }}$ | HMO | (environmental mechanics, waves) Significant wave height based on zeroth moment for narrow banded spectrum | $4\left(m_{0}\right)^{1 / 2}$ | m |

Version 2021
H, h

| ITTC | Computer |  |  |  |
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| Symbol | Name | Definition or <br> Symbol |  | SI- |


| $H_{\mathrm{N}}$ | HTNT | (fluid mechanics, cavitation) Net useful head of turbo-engines |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $H_{\text {SK }}$ | HSK | (ACV and SES) Skirt depth |  | m |
| $H_{\text {ss }}$ | HSS | (multi-hull vessels) Strut submerged depth | Depth of strut from still water line to strut-hull intersection | m |
| $H_{\text {TC }}$ | HTC | (ships, propulsor geometry) <br> Hull tip clearance | Distance between the propeller sweep circle and the hull | m |
| $H_{U}$ | HTUS | (fluid mechanics, cavitation) Total head upstream of turbo-engines |  | m |
| $\mathrm{Hu}_{\mathrm{u}}$ | HU | (environmental mechanics, waves) Wave height by zero up-crossing | The vertical distance between a trough and a successive crest | m |
| $H_{\text {w }}$ | HW | (environmental mechanics, waves) Wave height | The vertical distance from wave crest to wave trough, or twice the wave amplitude of a harmonic wave. $\eta_{\mathrm{C}}-\eta_{\mathrm{T}}$ | m |
| $H_{w 1 / 3}$ | HW13 | (environmental mechanics, waves) Significant wave height. Sum of significant wave height of swell and wind waves | Average of the highest one third wave heights | m |
| $H_{1 / 3 S}$ | H13S | (environmental mechanics, waves) Significant wave height of swell | Average of the highest one third wave heights of the swell. | m |
| $H_{1 / 3 W}$ | H13W | (environmental mechanics, waves) Significant wave height of wind waves. | Average of the highest one third wave heights of the wind waves. | m |
| $H_{w v}$ | HWV | (environmental mechanics, waves) Wave height estimated from visual observation |  | m |
| $H_{\sigma}$ | HWDS | (environmental mechanics, waves) Estimate of significant wave height from sample deviation of wave elevation record |  | m |
| $h$ | HS | (fluid mechanics, flow fields) Static pressure head | $\Delta z_{0}$, <br> $z_{0}$-axis positive vertical up! | m |
| $h$ | DE | (ships, basic quantities, ships, manoeuvrability) Depth, Water depth |  | m |

Version 2021
H, h

| ITTC | Computer |  |  |  |
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| Symbol | Name | Definition or <br> Symbol |  | SI- |


| $h$ |  | (seakeeping, large amplitude motions capsizing) Maximum tank height |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $h$ |  | (seakeeping, large amplitude motions capsizing) Vertical distance from the centre of A to the waterline |  | m |
| $h_{0}$ | H0 | (ships, propulsor geometry) Immersion | The depth of submergence of the propeller measured vertically from the propeller centre to the free surface | m |
| $h_{1 \mathrm{~A}}$ |  | (ships, propulsor geometry, water jets) maximum height of cross sectional area of stream tube at station 1A |  | m |
| $h_{\text {BS }}$ | HBS | (ACV and SES) Bow seal height | Distance from side wall keel to lower edge of bow seal | m |
| $h_{\text {CE }}$ |  | (seakeeping, large amplitude motions capsizing) Height of centre of area of Asp above waterline at SSM |  | m |
| $h_{\text {CG }}$ | HVCG | (hydrofoil boats) Height of centre of gravity foil borne | Distance of centre of gravity above mean water surface | m |
| $h_{\text {F }}$ | HFL | (hydrofoil boats) Flight height | Height of foil chord at foil borne mode above position at rest | m |
| $h_{\text {I }}$ | HTIC | (ice going vessels) Thickness of ice |  | m |
| $h_{\text {J }}$ | HJ | (ships, propulsor geometry, water jets) Height of jet centreline above undisturbed water surface |  | m |
| $h_{\mathrm{K}}$ | HKE | (hydrofoil boats) Keel clearance | Distance between keel and mean water surface foil borne | m |
| $h_{\text {LP }}$ |  | (seakeeping, large amplitude motions capsizing) Height of waterline above centre of area of immersed profile |  | m |
| $h_{M}$ | DEME | (ships, manoeuvrability) <br> Mean water depth |  | m |
| $h_{\text {P }}$ | HSP | (planing, semi-displacement vessels) Wetted height of strut palms (flange mounting) |  | m |

## ITTC Symbols

Version 2021
H, h

| ITTC <br> Symbol | Computer <br> Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |
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| $h_{\mathrm{R}}$ | HRU | (planing, semi-displacement <br> vessels) Wetted height of <br> rudders |  | m |
| :--- | :--- | :--- | :--- | :--- |
| $h_{\mathrm{SN}}$ | HTSN | (ice going vessels) Thickness <br> of snow cover | m |  |
| $h_{\mathrm{SS}}$ | HSS | (ACV and SES) Stern seal <br> height | Distance from side wall keel <br> to lower edge of stern seal | m |
| $h_{\mathrm{R}}$ | HRU | (planing, semi-displacement <br> vessels) Wetted height of <br> rudders |  | m |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| I | IM | (fundamental, time and frequency domain quantity) Imaginary variable |  | 1 |
| :---: | :---: | :---: | :---: | :---: |
| I | ID | (fluid mechanics, flow fields) Induction factor | Ratio between velocities induced by helicoidal and by straight line vortices | 1 |
| I | I, IN | (ships, basic quantities) Moment of inertia | Second order moment of a mass distribution | kg m ${ }^{2}$ |
| I | I | (sailing vessels) Fore triangle height |  | m |
| $\left\lvert\, \begin{aligned} & I_{12} \\ & I_{23} \\ & I_{31} \end{aligned}\right.$ | $\begin{aligned} & \mathrm{I} 2(1,2) \\ & \mathrm{I} 2(2,3) \\ & \mathrm{I} 2(3,1) \end{aligned}$ | (solid body mechanics, inertial and hydro properties) Real products of inertia in case of non-principal axes |  | $\mathrm{kg} \mathrm{m}{ }^{2}$ |
| $I^{\text {l }}{ }_{\nu v}$ | IH(U,V) | (solid body mechanics, inertial and hydro properties) Generalized hydrodynamic inertia | $\partial F_{u}^{h} / \partial \dot{\mathrm{V}}_{v}$ |  |
| $I_{i j}$ | IN(I,J) | (solid body mechanics, inertial and hydro properties) Second moments of mass, i.e. inertia distribution | Alias mass moments of inertia | $\mathrm{kg} \mathrm{m}{ }^{2}$ |
| $I_{\text {AS }}$ | ASI | (seakeeping, large amplitude motions capsizing) Attained subdivision index |  | 1 |
| $I_{\text {L }}$ | IL | (solid body mechanics, inertial and hydro properties) Longitudinal second moment of water-plane area | About transverse axis through centre of floatation | $\mathrm{m}^{4}$ |
| $I_{\text {T }}$ | IT | (solid body mechanics, inertial and hydro properties) Transverse second moment of water-plane area | About longitudinal axis through centre of floatation | $\mathrm{m}^{4}$ |
| $I_{V R}$ | IVR | (ships, hull resistance, water jets) Intake velocity ratio | $V_{V} / V$ | 1 |
| $I_{x y}$ | IXY | (solid body mechanics, inertial and hydro properties) Real products of inertia in case of non-principal axes |  | kg m ${ }^{2}$ |
| $I_{y}, I_{y y}$, | IY, IYY, | (solid body mechanics, inertial and hydro properties) Pitch moment of inertia around the principal axis $y$ |  | kg m ${ }^{2}$ |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $I_{y z}$ | IYZ | (solid body mechanics, inertial and hydro properties) Real products of inertia in case of non-principal axes |  | $\mathrm{kg} \mathrm{m}{ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $I_{z}, I_{z z}$ | IZ, IZZ, | (solid body mechanics, inertial and hydro properties) Yaw moment of inertia around the principal axis $z$ |  | $\mathrm{kg} \mathrm{m}{ }^{2}$ |
| $I_{z x}$ | IZX | (solid body mechanics, inertial and hydro properties) Real products of inertia in case of non-principal axes |  | $\mathrm{kg} \mathrm{m}{ }^{2}$ |
| i | I | (fundamental, time and frequency domain quantity) Imaginary unit | $\sqrt{-1}$ | 1 |
| $i_{\text {EI }}$ | ANENIN | (multi-hull vessels) Half angle of entrance at tunnel (inner) side | Angle of inner water line with reference to centre line of demihull | rad |
| $i_{\text {EO }}$ | ANENOU | (multi-hull vessels) Half angle of entrance at outer side | Angle of outer water line with reference to centre line of demihull | rad |
| $i_{\text {E }}$ | ANEN | (ships, hull geometry) Angle of entrance, half | Angle of waterline at the bow with reference to centre plane, neglecting local shape at stem | rad |
| $i_{G}$ | RK | (ships, propulsor geometry) <br> Rake <br> ISO symbol: Rk | The distance between the propeller plane and the generator line in the direction of the shaft axis. Aft displacement is positive rake. | m |
| $i_{\text {R }}$ | ANRU | (ships, hull geometry) Angle of run, half | Angle of waterline at the stern with reference to the centre-plane, neglecting local shape of stern frame | rad |
| is | RAKS | (ships, propulsor geometry) <br> Rake, skew-induced | The axial displacement of a blade section which occurs when the propeller is skewed. Aft displacement is positive rake | m |
| $i_{\text {T }}$ | RAKT | (ships, propulsor geometry) <br> Rake, total | The axial displacement of the blade reference line from the propeller plane $i_{\mathrm{G}}+i_{\mathrm{S}}=C_{\mathrm{S}} \sin \varphi$ Positive direction is aft. | m |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| J | JEI | (ships, propulsor performance) Propeller advance ratio | $V_{\text {A }} /(D n)$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| J | J | (sailing vessels) Fore triangle base |  | m |
| $J_{\text {A }}$ | JA | (ships, propulsor performance) Apparent or hull advance ratio | $V /(D n)=V_{H} /(D n)$ | 1 |
| $J_{\mathrm{H}}$ | JH | (ships, propulsor performance) Apparent or hull advance ratio | $V /(D n)=V_{H} /(D n)$ | 1 |
| $J_{\mathrm{P}}$ | JP | (ships, propulsor performance) Propeller advance ratio for ducted propeller | $V_{\mathrm{P}} /$ ( $\mathrm{D} n$ ) | 1 |
| $J_{\text {PQ }}$ | JPQ | (ships, propulsor performance) Advance ratio of propeller determined from torque identity |  | 1 |
| $J_{\text {PT }}$ | JPT | (ships, propulsor performance) Advance ratio of propeller determined from thrust identity |  | 1 |
| $J_{Q}$ | JQ | (ships, propulsor performance) Advance ratio of propeller determined from torque identity |  | 1 |
| $J_{T}$ | JT | (ships, propulsor performance) Advance ratio of propeller determined from thrust identity |  | 1 |
| $J_{\text {VR }}$ | JVR | (ships, hull resistance, water jets)) Jet velocity ratio | $V_{J} / V$ | 1 |
| j | J | (fundamental, time and frequency domain quantity) Integer values | $-\infty \ldots$ | s |

## ITTC Symbols

Version 2021

| ITTC | Computer |  | Definition or | SI- |
| :---: | :---: | :---: | :---: | :---: |
| Symbol | Symbol |  | Explanation | Unit |


| K |  | (ships, hydrostatics, stability seakeeping, large amplitude motions capsizing) Keel reference |  |  |
| :---: | :---: | :---: | :---: | :---: |
| K | MX | (ships, manoeuvrability, seakeeping, solid body mechanics, loads) Roll moment on body, moment about body $x$ axis |  | Nm |
| K | KS | (ships, manoeuvrability, seakeeping) Gain factor in linear manoeuvring equation |  | 1/s |
| K | K | (solid body mechanics, loads) Moment around body axis $x$ |  | Nm |
| $K_{1}$ | C1 | (ships, performance) Ship model correlation factor for propulsive efficiency | $\eta_{\text {DS }} / \eta_{\text {DM }}$ | 1 |
| $K_{2}$ | C2 | (ships, performance) Ship model correlation factor for propeller rate revolution | $n_{\text {S }} / n_{M}$ | 1 |
| $\overline{K A}$ | ZKA | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Assumed centre of gravity above moulded base or keel | Distance from the assumed centre of gravity A to the moulded base or keel K | m |
| $K_{\text {APP }}$ | KAP | (ships, performance) Appendage correction factor | Scale effect correction factor for model appendage drag applied at the towing force in a self-propulsion test | 1 |
| $\overline{K B}$ | ZKB | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Centre of buoyancy above moulded base or keel | Distance from the centre of buoyancy B to the moulded base or keel K | m |
| $K^{C}$ | CIRCK | (ships, hull resistance) R.E. Froude's speed displacement coefficient | $\begin{aligned} & (4 \pi)^{1 / 2} F r_{\nabla} \text { or } \\ & (4 \pi / g)^{1 / 2} V_{K} / \nabla^{1 / 6} \end{aligned}$ | 1 |
| $K_{F i}$ | KF(I) | (ships, unsteady propeller forces) Vibratory force coefficients | $F_{i} /\left(\rho n^{2} D^{4}\right)$ | 1 |
| $K_{F u}$ | KF(U) | (ships, unsteady propeller forces) Generalized vibratory force coefficients | According to definitions of $K_{F i}$ and $K_{M \mathrm{i}}$ | 1 |

Version 2021

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or |
| :--- |
| Explanation |


| KG | ZKG | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Centre of gravity above moulded base or keel | Distance from centre of gravity G to the moulded base or keel K | m |
| :---: | :---: | :---: | :---: | :---: |
| Kg | ZKAG | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Vertical centre of gravity of added or removed weight above moulded base or keel | Distance from centre of gravity, g, to the moulded base or keel K | m |
| $K_{H}$ |  | (ships, propulsor geometry, water jets) Head coefficient: | $\frac{g H}{n^{2} D^{5}}$ |  |
| KM | ZKM | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Transverse metacentre above moulded base or keel | Distance from the transverse metacentre M to the moulded base or keel K | m |
| Kıi $^{\text {l }}$ | KM(I) | (ships, unsteady propeller forces) Vibratory moment coefficients | $M_{i} /\left(\rho n^{2} D^{5}\right)$ | 1 |
| $\overline{K M}_{L}$ | ZKML | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal metacentre above moulded base or keel | Distance from the longitudinal metacentre $\mathrm{M}_{L}$ to the moulded base or keel K | m |
| $K_{P}$ | KP | (ships, propulsor performance) Delivered power coefficient | $P_{\mathrm{D}} /\left(\rho n^{3} D^{5}\right)=2 \pi K_{Q}$ | 1 |
| $K_{p}$ | KPR | (ships, unsteady propeller forces) Pressure coefficient | $p /\left(\rho n^{2} D^{2}\right)$ | 1 |
| $K_{Q}$ | KQ | (ships, propulsor performance, hull resistance, water jets)) Torque coefficient | $Q /\left(\rho n^{2} D^{5}\right)$ | 1 |
| $K_{\text {QJ }}$ |  | (ships, hull resistance, water jets) Flow rate coefficient: | $\frac{Q_{\mathrm{J}}}{n D^{3}}$ | 1 |
| $K_{Q 0}$ | KQ0 | (ships, propulsor performance) Torque coefficient of propeller converted from behind to open water condition | $K_{Q} \cdot \eta_{\mathrm{R}}$ | 1 |
| $K_{Q T}$ | KQT | (ships, propulsor performance) Torque coefficient of propeller determined from thrust coefficient identity |  | 1 |
| $K_{\text {QIA }}$ | KQICMS | (ice going vessels) Average coefficient of torque in ice | $Q_{\mathrm{IA}} /\left(\rho_{\mathrm{W}} n_{\mathrm{IA}}{ }^{2} D^{5}\right)$ | 1 |

ITTC Symbols
Version 2021


| Ksc | KSC | (ships, propulsor performance) Centrifugal spindle torque coefficient | $Q_{\text {sc }} /\left(\rho n^{2} D^{5}\right)$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| Ksh | KSH | (ships, propulsor performance) Hydrodynamic spindle torque coefficient | $Q_{\text {sh }} /\left(\rho n^{2} D^{5}\right)$ | 1 |
| $K_{R}$ | KR | (ships, hull resistance) Resistance coefficient corresponding to $K_{Q}, K_{T}$ | $R /\left(\rho D^{4} n^{2}\right)$ | 1 |
| $K_{T}$ | KT | (ships, propulsor performance) Thrust coefficient | $T /\left(\rho n^{2} D^{4}\right)$ | 1 |
| $K_{\text {TD }}$ | KTD | (ships, propulsor performance) Duct thrust coefficient for a ducted propeller unit | $T_{\mathrm{D}} /\left(\rho n^{2} D^{4}\right)$ | 1 |
| $K_{\text {TIA }}$ | KTICMS | (ice going vessels) Average coefficient of thrust in ice | $T_{\mathrm{IA}} /\left(\rho_{\mathrm{W}} n_{\mathrm{IA}}{ }^{2} D^{4}\right)$ | 1 |
| $K_{\text {TP }}$ | KTP | (ships, propulsor performance) Propeller thrust coefficient for a ducted propeller unit | $T_{\mathrm{P}} /\left(\rho n^{2} D^{4}\right)$ | 1 |
| $K_{T Q}$ | KTQ | (ships, propulsor performance) Thrust coefficient achieved by torque identity |  | 1 |
| $K_{\text {TT }}$ | KTT | (ships, propulsor performance) Total thrust coefficient for a ducted propeller unit | $K_{\text {TP }}+K_{\text {TD }}$ | 1 |
| k |  | (uncertainty) Coverage factor | For calculation of expanded $k$ uncertainty $U=k u_{c}(y)$ | 1 |
| k | HK | (fluid mechanics, flow parameter) Roughness height or magnitude | Roughness height, usually in terms of some average | m |
| k | WN | (environmental mechanics, waves) Wave number | $2 \pi / L_{\mathrm{W}}=\omega^{2} / g$ | 1/m |
| k | K | (ships, hull resistance) Three dimensional form factor on flat plate friction | $\left(C_{V}-C_{\text {F0 }}\right) / C_{\text {F0 }}$ | 1 |
| $k$ | RDGX | (solid body mechanics, inertial and hydro properties) Roll radius of gyration around the principal axis $x$ | $\left(I_{x x} / m\right)^{1 / 2}$ | m |
| k |  | (seakeeping, large amplitude motions capsizing) Roll damping coefficient expressing the effect of bilge keels |  | 1 |

## ITTC Symbols

Version 2021

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $k_{p}$ |  | (uncertainty) Coverage factor for probability $p$ | For calculation of expanded uncertainty $U_{p}=k_{p} u_{c}(y)$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $k_{\text {P }}$ | KP | (ships, resistance and propulsion, propulsor performance) Roughness height of Propeller blade surface |  | m |
| $k_{\text {s }}$ | SK | (fluid mechanics, flow parameter) Sand roughness | Mean diameter of the equivalent sand grains covering a surface | m |
| ks | KHS | (ships, resistance and propulsion, ship performance) Roughness height of Hull surface |  | m |
| $k_{x}, k_{x x}$ | RDGX | (solid body mechanics, inertial and hydro properties) Roll radius of gyration around the principal axis $x$ | $\left(I_{x x} / m\right)^{1 / 2}$ | m |
| $k_{y}, k_{y y}$ | RDGY | (solid body mechanics, inertial and hydro properties) Pitch radius of gyration around the principal axis $y$ | $\left(I_{y y} / m\right)^{1 / 2}$ | m |
| $k_{z}, k_{z z}$ | RDGZ | (solid body mechanics, inertial and hydro properties) Yaw radius of gyration around the principal axis $z$ | $\left(I_{z z} / m\right)^{1 / 2}$ | m |
| $k(\theta)$ | WDC | (ships, hull resistance) Wind direction coefficient | $C_{\text {AA }} / C_{\text {AA0 }}$ | 1 |

ITTC Symbols
Version 2021

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |


| L | L | (ships, hull geometry) <br> Length of ship | Reference length of ship (generally length between the perpendiculars) | m |
| :---: | :---: | :---: | :---: | :---: |
| $L$ | L, LE | (ships, basic quantities) Length |  | m |
| L | FF(3) | (ships, basic quantities) Lift (force) | Force perpendicular to translatory velocity | N |
| $L$ |  | (seakeeping, large amplitude motions capsizing) Length of the vessel on the waterline in maximum load condition IMO/IS |  | m |
| L | L | (mechanics in general, solid body mechanics) Angular momentum | $\boldsymbol{L}=I \boldsymbol{\omega}\left(=r^{2} \mathrm{mv}\right)$ | Kg m s ${ }^{-1}$ |
| $L_{0}$ | LF0 | (fluid mechanics, lifting surfaces) Lift force for angle of attack of zero | $C_{L 0} A_{\text {FT }} q$ | N |
| $L_{0}$ | LF0 | (hydrofoil boats) Profile lift force for angle of attack of zero | $C_{L 0} A_{\text {FT }} q$ | N |
| $L_{B}$ | LB | (ACV and SES) Deformed bag contact length |  | m |
| $L_{\text {b }}$ | LSB | (ships, manoeuvrability, seakeeping) Static stability lever | $N_{v} / Y_{v}$ | m |
| $L_{\text {C }}$ | LC | (planing, semi-displacement vessels) Wetted chine length, underway |  | m |
| $L_{\text {C }}$ | LAC | (ACV and SES) Cushion length |  | m |
| $L_{\text {CB }}$ | XCB | (ships, hydrostatics, stability) Longitudinal centre of buoyancy (LCB) | Longitudinal distance from reference point to the centre of buoyancy, B such as $\mathrm{X}_{\text {MCF }}$ from Midships | m |
| $L_{\text {CF }}$ | XCF | (ships, hydrostatics, stability) Longitudinal centre of flotation (LCF) | Longitudinal distance from reference point to the centre of flotation, F such as $\mathrm{X}_{\mathrm{MCF}}$ from Midships | m |
| $L_{\text {CG }}$ | XCG | (ships, hydrostatics, stability) Longitudinal centre of gravity (LCG) | Longitudinal distance from a reference point to the centre of gravity, G such as XMCG from Midships | m |
| $L_{\text {CH }}$ | LCH | (multi-hull vessels) Length of centre section of hull | Length of prismatic part of hull | m |

## ITTC Symbols

Version 2021

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- |


| $L_{\text {CS }}$ | LCS | (multi-hull vessels) Length of centre section of strut | Length of prismatic part of strut | , |
| :---: | :---: | :---: | :---: | :---: |
| $L_{\text {D }}$ | LD | (ships, propulsor geometry) Duct length |  | m |
| $L_{\text {den }}$ | LDEN | (ships, propulsor geometry) <br> Duct entry part length | Axial distance between leading edge of duct and propeller plane | m |
| $L_{\text {dex }}$ | LDEX | (ships, propulsor geometry) <br> Duct exit length | Axial distance between propeller plane and trailing edge of duct | m |
| $L_{\text {d }}$ | LSR | (ships, manoeuvrability, seakeeping) Damping stability lever | $\left(N_{r}-m u \chi_{G}\right) /\left(Y_{r}-m u\right)$ | m |
| $L_{\mathrm{E}}$ | LEN | (ships, hull geometry) <br> Length of entrance | From the forward perpendicular to the forward end of parallel middle body, or maximum section | m |
| $L_{\mathrm{E}}$ | LACE | (ACV and SES) Effective length of cushion | $A_{\mathrm{C}} / B_{\mathrm{C}}$ | m |
| $L_{\text {Eff }}$ | LEFF | (sailing vessels) Effective length for Reynolds Number |  | m |
| $L_{\text {F }}$ | LF | (ships, appendage geometry) Length of flap or wedge | Measured in direction parallel to keel | m |
| $L_{\mathrm{F}}$ | LF | (hydrofoil boats) Lift force on foil | $C_{L} A_{\text {FT }} q$ | N |
| $L_{\text {fF }}$ | LFF | (hydrofoil boats) Lift force on front foil | $C_{L} A_{\text {fF }} q$ | N |
| $L_{\text {FR }}$ | LFR | (hydrofoil boats) Lift force on rear foil | $C_{L} A_{\text {FR }} q$ | N |
| Lfs | LFS | (ships, hull geometry) <br> Frame spacing | used for structures | m |
| $L_{H}$ | LH | (multi-hull vessels) Box length | Length of main deck | m |
| $L_{H}$ | LH | (ACV and SES) Horizontal spacing between inner and outer side skirt hinges or attachment points to structure | needs clarification | m |
| $L_{\text {HY }}$ |  | (sailing vessels) Hydrodynamic lift force |  | N |
| $L_{K}$ | LK | (planing, semi-displacement vessels) Wetted keel length, underway |  | m |
| $L_{M}$ | LM | (planing, semi-displacement vessels) Mean wetted length, underway | $\left(L_{K}+L_{C}\right) / 2$ | m |

ITTC Symbols
Version 2021

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$ Symbol | Same | Definition or <br> Explanation | SI- <br> Unit |
| :--- | :--- | :--- | :--- |


| $L_{\text {NH }}$ | LNH | (multi-hull vessels) Length of nose section of hull | Length of nose section of hull with variable diameter | m |
| :---: | :---: | :---: | :---: | :---: |
| $L_{\text {NS }}$ | LNS | (multi-hull vessels) Length of nose section of strut | Length of nose section of strut with variable thickness | m |
| $L_{\text {OA }}$ | LOA | (ships, hull geometry) Length, overall |  | m |
| Los | LOS | (ships, hull geometry) <br> Length, overall submerged |  | m |
| $L_{\text {P }}$ | LP | (ships, hull geometry) Length of parallel middle body | Length of constant transverse section | m |
| $L_{p}$ | SPL | (underwater noise) <br> Sound pressure level | $\begin{aligned} & L_{p} \\ & =10 \log _{10}\left(\frac{\bar{p}_{r m s}^{2}}{p_{r e f}^{2}}\right) \mathrm{dB}, p_{\text {ref }} \\ & =1 \mu \mathrm{~Pa} \end{aligned}$ |  |
| Lpb | LPB | (ships, hull geometry) <br> Length of Pod Main Body |  | m |
| $L_{\text {PbF }}$ | LPBF | (ships, hull geometry) Length of Bottom Fin | Code length of bottom fin under pod main body | m |
| $L_{\text {PP }}$ | LPP | (ships, hull geometry) <br> Length between perpendiculars |  | m |
| $L_{\text {Pr }}$ | LPRC | (planing, semi-displacement vessels) Projected chine length | Length of chine projected in a plane parallel to keel | m |
| Lps | LPS | (ships, hull geometry) Length of Upper Strut | Code length of strut between forward edge and aft edge | m |
| $L_{\text {R }}$ | LRU | (ships, hull geometry) <br> Length of run | From section of maximum area or after end of parallel middle body to waterline termination or other designated point of the stern | m |
| Ls | LS | (multi-hull vessels) Strut length | Length of strut from leading to trailing edge | m |
| $L_{\text {s }}$ | LS | (ACV and SES) Distance of leading skirt contact point out-board or outer hinge of attachment point to structure | needs clarification | m |
| $L_{\text {s }}$ | SRNL | (underwater noise) <br> Underwater sound radiated noise level at a reference distance of 1m | $\begin{aligned} & L_{\mathrm{s}} \\ & =L_{\mathrm{p}} \\ & +20 \log _{10}\left[\frac{d}{d_{r e f}}\right] \mathrm{dB}, d_{r e f} \\ & =1 \mathrm{~m} \end{aligned}$ |  |

ITTC Symbols
Version 2021

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Sin |


| $L_{\text {SB }}$ | LSB | (planing, semi-displacement vessels) Total length of shafts and bossings |  | m |
| :---: | :---: | :---: | :---: | :---: |
| LSH | LSH | (multi-hull vessels) Length of submerged hull |  | m |
| Lss | LSS | (ships, hull geometry) Station spacing |  | m |
| $L_{\text {то }}$ | LT0 | (hydrofoil boats) Lift force at take off | $C_{L \text { LO }} A_{\text {FT }} q$ | N |
| $L_{\text {VHD }}$ | LVD | (planing, semi-displacement vessels) Vertical component of hydrodynamic lift |  | N |
| Lvs | LVS | (planing, semi-displacement vessels) Hydrostatic lift | Due to buoyancy | N |
| $L_{\text {W }}$ | LW | (environmental mechanics, waves) Wave length | The horizontal distance between adjacent wave crests in the direction of advance | m |
| $L_{\text {wv }}$ | LWV | (environmental mechanics, waves) Wave length estimated by visual observation | Measured in the direction of wave propagation | m |
| $L_{\text {WL }}$ | LWL | (ships, hull geometry) Length of waterline |  | m |
| $l$ | XTA | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal trimming arm | $X_{\text {CG }}-X_{\text {CB }}$ | m |
| 1 |  | (seakeeping, large amplitude motions capsizing) Arm of dynamic stability corrected for free surfaces - IMO/table |  | m |
| $l$ |  | (seakeeping, large amplitude motions capsizing) Maximum tank length |  | m |
| $l_{\text {b }}$ | LSB | (ships, manoeuvrability, seakeeping) Static stability lever | $N_{v} / Y_{v}$ | m |
| $l_{\text {c }}$ | LC | (fluid mechanics, cavitation) Cavity length | Streamwise dimension of a fully-developed cavitating region | m |
| $l_{\text {CP }}$ | LCP | (planing, semi-displacement vessels) Lever of resultant of pressure forces, underway | Distance between centre of pressure and aft end of planing surface | m |
| $l_{\text {d }}$ | LSR | (ships, manoeuvrability, seakeeping) Damping stability lever | $\left(N_{r}-\right.$ mux $\left._{G}\right) /\left(Y_{r}-m u\right)$ | m |

## ITTC Symbols

Version 2021
L, I

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- |


| $l_{\text {F }}$ | LEFF | (hydrofoil boats) Horizontal distance of centre of pressure of front foil to centre of gravity |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $l_{\text {FR }}$ | LEFR | (hydrofoil boats) Horizontal distance between centres of pressure of front and rear foils | $l_{\text {F }}+l_{\text {R }}$ | m |
| $l_{\text {h }}$ | LH | Hub length | The length of the hub, including any fore and aft shoulder | m |
| $l_{\text {ha }}$ | LHA | Hub length, aft | Length of the hub taken from the propeller plane to the aft end of the hub including aft shoulder | m |
| $l_{\text {hf }}$ | LHF | Hub length, fore | Length of the hub taken from the propeller plane to the fore end of the hub including fore shoulder | m |
| $l_{\text {R }}$ | LERF | (hydrofoil boats) Horizontal distance of centre of pressure of rear foil to centre of gravity |  | m |
| $l_{r}$ | LHRD | (ships, manoeuvrability, turning circles) Loop height of $r-\delta$ curve for unstable ship |  | rad/s |
| $l_{\text {s }}$ |  | (seakeeping, large amplitude motions capsizing) Actual length of enclosed superstructure extending from side to side of the vessel |  | m |
| $l_{\text {w }}$ |  | (seakeeping, large amplitude motions capsizing) Wind heeling lever |  | m |
| $l_{\delta}$ | LWRD | (ships, manoeuvrability, turning circles) Loop width of $r-\delta$ curve for unstable ship |  | rad |

ITTC Symbols
Version 2021
M, m

| ITTC <br> Symbol | Computer <br> Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |
| :--- | :--- | :--- | :--- | :--- |


| M | M1, F1 | (ships, basic quantities) Moment of forces | First order moment of a force distribution | Nm |
| :---: | :---: | :---: | :---: | :---: |
| M | MO | (ships, basic quantities) Momentum |  | Ns |
| M | MR | (fundamental, statistical, stochastic) Expectation, population mean |  |  |
| M |  | (ships, hydrostatics, stability) (seakeeping, large amplitude motions capsizing) <br> Metacentre of a vessel | See subscripts for qualification | Nm |
| M, | M, | (solid body mechanics, loads) Moment around body axis y |  |  |
| M | MY | (ships, manoeuvrability, seakeeping) Pitch moment on body, moment about body $y$ axis |  | Nm |
| M | MSP | (hydrofoil boats) Vessel pitching moment |  | Nm |
| M | MS | (hull geometry) Midships |  |  |
| Ma | MN | (fluid mechanics, flow parameter) Mach number | V/c | 1 |
| $M^{\text {B }}{ }_{i}$ | MB(I) | (solid body mechanics, loads) Bending moment | $F^{\text {S1 }}{ }_{2}, F^{\text {S1 }}{ }_{3}$ | Nm |
| $M^{\text {C }}$ | CIRCM | (ships, hull geometry) R.E. Froude's length coefficient, or length-displacement ratio | $L / \nabla^{1 / 3}$ | 1 |
| $M_{\text {c }}$ |  | (seakeeping, large amplitude motions capsizing) Maximum offset load moment due to crew |  | Nm |
| $M_{\text {c }}$ |  | (seakeeping, large amplitude motions capsizing) Minimum capsizing moment as determined when account is taken of rolling |  |  |
| $M_{\mathrm{F}}$ | MLF | (hydrofoil boats) Load factor of front foil | $L_{\text {FF }} / 4$ | 1 |
| $M_{\text {FS }}$ |  | (seakeeping, large amplitude motions capsizing) Free surface moment at any inclination |  | Nm |
| $M_{i}$ | M(I) | (ships, unsteady propeller forces) Vibratory moment | $i=1,2,3$ | Nm |

ITTC Symbols
Version 2021
M, m

| ITTC <br> Symbol | Computer <br> Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |
| :--- | :--- | :--- | :--- | :--- |


| $M_{\text {L }}$ | $\begin{array}{\|l} \mathrm{MB}(3), \\ \mathrm{FS}(6) \end{array}$ | (ships, seakeeping) Wave excited lateral bending moment | Alias horizontal! | Nm |
| :---: | :---: | :---: | :---: | :---: |
| $\bar{M}_{\text {is }}$ |  | (ships, hull resistance, water jets) Momentum flux at station $s$ in $i$ direction | $\iint_{A_{j}} \rho u_{i}\left(u_{j} n_{j}\right) d A$ | W |
| $M_{N}$ | $\begin{array}{\|l} \mathrm{MB}(2), \\ \mathrm{FS}(5) \end{array}$ | (ships, seakeeping) Wave excited normal bending moment | Alias vertical! | Nm |
| M, MR | MR | (fundamental, statistical, stochastic) Expectation, population mean |  |  |
| $M_{\mathrm{R}}$ | MLR | (hydrofoil boats) Load factor of rear foil | $L_{\text {FR }} / 4$ | 1 |
| $M_{\mathrm{R}}$ |  | (seakeeping, large amplitude motions capsizing) Heeling moment due to turning |  | Nm |
| $M_{\text {S }}$ | MS | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Moment of ship stability in general | $\Delta \overline{G Z}$ Other moments such as those of capsizing, heeling, etc. will be represented by $M_{\mathrm{s}}$ with additional subscripts as appropriate | Nm |
| MS | MS | (fundamental, statistical, stochastic) Average, sample mean |  | 1 |
| $M_{\text {T }}$ | $\begin{aligned} & \hline \text { MT(1), } \\ & \text { FS(4) } \end{aligned}$ | (ships, seakeeping) Wave excited torsional moment |  | Nm |
| $M^{\text {T }}$ | MT, <br> MB(1) | (solid body mechanics, loads) Twisting or torsional moment | $F^{\text {S1 }}{ }_{1}$ | Nm |
| $M_{\text {TC }}$ | MTC | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Moment to change trim by one centimetre |  | Nm/cm |
| $M_{\text {TM }}$ | MTM | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Moment to change trim by one meter | $\Delta C_{\text {MTL }}$ | Nm/m |

Version 2021


| $M_{u v}$ | MA(U,V) | (ships, unsteady propeller forces, solid body mechanics, inertial and hydro properties) Generalized mass, i. <br> e. generalized inertia tensor of a (rigid) body referred to a body fixed coordinate system | $\left\lvert\, \begin{aligned} & M_{i j}=M^{0}{ }_{i j} \\ & M_{i, 3+j}=M^{1 \mathrm{~T}}{ }_{i j} \\ & M_{3+i, j}=M^{1}{ }^{i j} \\ & M_{3+i, 3+j}=M^{2}{ }_{i j} \end{aligned}\right.$ | kg |
| :---: | :---: | :---: | :---: | :---: |
| $M_{\text {W }}$ |  | (seakeeping, large amplitude motions capsizing) Maximum heeling moment due to wind |  | Nm |
| $M_{\mathrm{v}}$ |  | (seakeeping, large amplitude motions capsizing) Dynamically applied heeling moment due to wind pressure |  | Nm |
| $M_{\mathrm{x}}$, | $\mathrm{M}(1)$, | (solid body mechanics, loads) Moment around body axis $x$ |  | Nm |
| $M_{y}$, | $\mathrm{M}, \mathrm{M}(2)$, | (solid body mechanics, loads) Moment around body axis y |  | Nm |
| $M_{\mathrm{z}}$, | M(3) | (solid body mechanics, loads) Moment around body axis z |  | Nm |
| m | M, MA, MASS | (ships, basic quantities, solid body mechanics, inertial and hydro properties) Mass |  | kg |
| m | ХАСВ | (ships, hydrostatics, stability) Longitudinal centre of floatation of added buoyant layer | Longitudinal distance from reference point to the centre of the added buoyant layer, b | m |
| m | SHIPMA | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) <br> Ship mass | $W / g$ | kg |
| $m$ | BLCK | (ships, hull resistance) <br> Blockage parameter | Maximum transverse area of model ship divided by tank cross section area | 1 |
| $\begin{aligned} & m^{0}{ }_{i j}, \\ & m_{i j} \end{aligned}$ | $\begin{aligned} & \text { M0(I,J), } \\ & \text { MA(I,J) } \end{aligned}$ | (solid body mechanics, inertial and hydro properties) Zeroth moments of mass, i.e. inertia distribution, mass tensor | $m_{i j}=m \delta_{i j}$ | kg |

## ITTC Symbols

Version 2021
M, m

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $m^{1}{ }_{i j}$ | M1(I,J) | (solid body mechanics, inertial and hydro properties) First moments of mass, i.e. inertia distribution | Alias static moments of mass | kg m |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & m_{22}^{2}, \\ & m_{55} \end{aligned}$ | $\begin{aligned} & \mathrm{M} 2(2,2), \\ & \mathrm{MA}(5,5) \end{aligned}$ | (solid body mechanics, inertial and hydro properties) Pitch moment of inertia around the principal axis y |  | kg m ${ }^{2}$ |
| $\begin{aligned} & m_{33}^{2}, \\ & m_{66} \end{aligned}$ | $\begin{aligned} & \mathrm{M} 2(3,3), \\ & \mathrm{MA}(6,6) \end{aligned}$ | (solid body mechanics, inertial and hydro properties) Yaw moment of inertia around the principal axis z |  | kg m ${ }^{2}$ |
| $m^{2}{ }_{i j}$, | M2(I,J), | (solid body mechanics, inertial and hydro properties) Second moments of mass, i.e. inertia distribution | Alias mass moments of inertia | kg m ${ }^{2}$ |
| $m_{\text {LCC }}$ |  | (seakeeping, large amplitude motions capsizing) Mass in light craft condition |  | kg |
| $m_{\text {LDC }}$ |  | (seakeeping, large amplitude motions capsizing) Mass in loaded displacement condition according to ... |  | kg |
| $m_{\text {MTL }}$ |  | (seakeeping, large amplitude motions capsizing) Maximum total load (mass) |  | kg |
| $m_{n}$ | MN | (environmental mechanics, waves) n-th moment of wave power spectral density | $\int f^{n} S(f) d f$ | $\mathrm{m}^{2} / \mathrm{s}^{n}$ |
| $m_{\text {SSC }}$ |  | (seakeeping, large amplitude motions capsizing) Mass in standard sailing conditions according to ... |  | kg |
| $m_{x}$ | XMS | (fundamental, statistical) Average or sample mean of a random quantity | $1 / n \sum x_{i}, i=1 \ldots n$ unbiased random estimate of the expectation with $\begin{aligned} & x^{\mathrm{AE}}=x^{\mathrm{E}} \\ & x^{\mathrm{VSE}}=x^{\mathrm{V}} / n \end{aligned}$ |  |

ITTC Symbols
Version 2021
N, n

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $N$ | FR, N | (ships, basic quantities) Frequency or rate of revolution | Alias RPS (RPM in some propulsor applications) | Hz |
| :---: | :---: | :---: | :---: | :---: |
| $N$ |  | (uncertainty) Number of input quantities | Number of input quantities $X_{i}$ on which the measurand $Y$ depends | 1 |
| $N$ | MZ | (ships, manoeuvrability, seakeeping) Yaw moment on body, moment about body zaxis |  | Nm |
| $N$ | $\begin{aligned} & \mathrm{N}, \mathrm{M}(3), \\ & \mathrm{F} 1(3), \mathrm{F}(6) \end{aligned}$ | (solid body mechanics, loads) Moment around body axis z |  | Nm |
| $N_{\text {A }}$ | NAPP | (planing, semi-displacement vessels) Appendage lift force (normal to reference line) | Lift forces arising from appendages inclined to flow, assumed to act normally to reference line | N |
| $N_{\text {B }}$ | NBOT | (planing, semi-displacement vessels) Bottom normal force (normal to reference line) | Resultant of pressure and buoyant forces assumed acting normally to the reference line | N |
| $N_{\text {P }}$ | NPR | (ships, propulsor geometry) Number of propellers |  | 1 |
| $N_{\text {PP }}$ | NPP | (planing, semi-displacement vessels) Propeller pressure force (normal to reference line) | Resultant of propeller pressure forces acting normally to the reference line | N |
| $N_{\text {PS }}$ | NPS | (planing, semi-displacement vessels) Propeller suction force (normal to reference line) | Resultant of propeller suction forces acting normally to the reference line | N |
| $N_{r}$ | NR | (ships, manoeuvrability, seakeeping) Derivative of yaw moment with respect to yaw velocity | $\partial N / \partial r$ | Nms |
| $N_{\text {RP }}$ | NRP | (planing, semi-displacement vessels) Rudder pressure force (normal to reference line) | Resultant of rudder pressure forces acting normally to the reference line | N |
| $N_{r}$ | NRRT | (ships, manoeuvrability, seakeeping) Derivative of yaw moment with respect to yaw acceleration | $\partial N / \partial \dot{r}$ | Nms ${ }^{2}$ |
| $N V R$ |  | (ships, hull resistance, water jets) Nozzle velocity ratio: | $\frac{\overline{u_{6 \xi}}}{U_{0}}$ | 1 |

## ITTC Symbols

Version 2021
N, n

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $N_{v}$ | NV | (ships, manoeuvrability, seakeeping) Derivative of yaw moment with respect to sway velocity | $\partial N / \partial v$ | Ns |
| :---: | :---: | :---: | :---: | :---: |
| $N_{\dot{v}}$ | NVRT | (ships, manoeuvrability, seakeeping) Derivative of yaw moment with respect to sway acceleration | $\partial N / \partial \dot{v}$ | Nms ${ }^{2}$ |
| $N_{\delta}$ | ND | (ships, manoeuvrability, seakeeping) Derivative of yaw moment with respect to rudder angle | $\partial N / \partial \delta$ | Nm |
| $n$ |  | Number of repeated observations |  | 1 |
| $n$ | FR, N | (ships, basic quantities, performance, propulsor performance) Frequency or rate of revolution | Alias RPS (RPM in some propulsor applications) | Hz |
| $n$ |  | (ships, hull resistance, water jets) Impeller rotation rate |  | Hz |
| $n_{\text {aw }}$ | NAW | (ships, seakeeping) Mean increased rate of revolution in waves |  | $1 / \mathrm{s}^{2}$ |
| $n_{i}$ |  | (ships, hull resistance, water jets) Unit normal vector in $i$ direction |  | 1 |
| $n_{\text {IA }}$ | FRICMS | (ice going vessels) Average rate of propeller revolution in ice |  | Hz |
| $n_{\text {T }}$ |  | (ships, propulsor performance) Propeller rate of revolution, corrected using correlation factor | $n_{\mathrm{T}}=C_{N} \cdot n_{\mathrm{S}}$ | 1 |

## ITTC Symbols

| Version 2021 |  |  | O, 0 |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |


| $\overline{O G}$ | (seakeeping, large amplitude <br> motions capsizing) Height of <br> centre of gravity above wa- <br> terline | m |
| :--- | :--- | :--- | :--- |

ITTC Symbols

| Version 2021 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or | SI- |
| Symbol | Symbol |  | Explanation | Unit |


| $P$ | P, PO | (ships, basic quantities) Power |  | W |
| :---: | :---: | :---: | :---: | :---: |
| $P$ | PT | (fluid mechanics, boundary layers) Total pressure |  | Pa |
| $P$ | PITCH | (ships, propulsor geometry) Propeller pitch in general |  | m |
| $P$ | P | (sailing vessels) Mainsail height |  | m |
| $P$ | P | (mechanics in general, solid body mechanics) Linear momentum | $\boldsymbol{P}=m \boldsymbol{v}$ | Kg m s ${ }^{-1}$ |
| $P_{\text {AW }}$ | PAW | (ships, seakeeping) Mean power increased in waves |  | W |
| $P_{\text {B }}$ | PB | (ships, performance) Brake power | Power delivered by prime mover | W |
| $P_{\text {BW }}$ | PBW | (ships, ship performance) Brake power in representative sea condition |  | W |
| $P D$ | PD | (fundamental, statistical, stochastic) Probability density |  | 1 |
| $P_{\text {D }}$ | PD, PP | (ships, performance) Delivered power, propeller power | $Q \omega$ | W |
| $P_{\text {D }}$ |  | (ships, hull resistance, water jets) Delivered Power to pump impeller |  | W |
| $P_{\text {DI }}$ | PDI | (ice going vessels) Delivered power at propeller in ice | $2 \pi Q_{\text {IA }} n_{\text {IA }}$ | W |
| $P_{\text {DT }}$ | PDT | (ships, ship performance) Delivered Power, corrected using correlation factor | $P_{\text {DT }}=C_{P} \cdot P_{\mathrm{DS}}$ | W |
| $P_{\text {E }}$ | PE, PR | (ships, performance) Effective power, resistance power | $R$ V | W |
| $P_{\text {E }}$ |  | (ships, hull resistance, water jets) Effective power: | $R_{\text {твн }} U_{0}$ | W |
| $\mathrm{P}_{\mathrm{F}}$ | PF | (fundamental, statistical, stochastic) Probability function |  | 1 |
| $P_{\text {FCU }}$ | PFCU | (ACV and SES) Power of lift fan |  | W |
| $P_{\text {FSK }}$ | PFSK | (ACV and SES) Power of skirt fan |  | W |
| $P_{\text {I }}$ | PI | (ships, performance) Indicated power | Determined from pressure measured by indicator | W |
| $P_{\text {J }}$ | PJ | (ships, propulsor performance) Propeller jet power | $\eta_{\text {TJ }} T V_{\text {A }}$ | W |

## ITTC Symbols

Version 2021
P, p

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name $\quad$| Definition or |
| :--- |
| Explanation |


| $P_{\text {JSE }}$ |  | (ships, hull resistance, water jets) Effective Jet System Power | $Q_{\mathrm{J}} \mathrm{H}_{1 \mathrm{~A} 7}$ | W |
| :---: | :---: | :---: | :---: | :---: |
| $P_{m}$ | PM | (propulsion, propulsor) Propeller mean pitch |  | m |
| $P_{\text {MB }}$ | PMB | (propulsion, propulsor) Blade mean pitch |  | m |
| $P_{n}$ | PN | (ships, manoeuvrability, seakeeping) P-number, heading change per unit rudder angle in one ship length |  | 1 |
| $P_{\text {P }}$ | PD, PP | (ships, performance) Delivered power, propeller power | $Q \omega$ | W |
| $P_{\text {PE }}$ |  | (ships, hull resistance, water jets) Pump effective power: | $Q_{J} H_{35}$ | W |
| $P_{R}$ | PE, PR | (ships, performance) Effective power, resistance power | $R$ V | W |
| $P_{\text {s }}$ | PS | (ships, performance) Shaft power | Power measured on the shaft | W |
| $P_{T}$ | PTH | (ships, performance) Thrust power | $T V_{\text {A }}$ | W |
| $P_{\text {TE }}$ |  | (ships, hull resistance, water jets) Effective thrust power |  | W |
| $P_{\mathrm{V}}$ |  | (seakeeping, large amplitude motions capsizing) Wind pressure |  | Pa |
| $p$ |  | (uncertainty) Probability | Level of confidence: $0 \leq p \leq$ 1.0 | 1 |
| $p$ | P | (solid body mechanics, rigid body motions) Rotational velocity around body axis $x$ |  | rad/s |
| $p$ | PR, ES | (fluid mechanics, flow fields) Pressure, density of static flow energy |  | Pa |
| $p$ | PR | (fluid mechanics, boundary layers) Static pressure |  | Pa |
| $p$ | PDR | (ships, propulsor geometry) Pitch ratio ISO Symbol: P/D | $P / D$ | 1 |
| $p$ | PR | (ships, unsteady propeller forces) Pressure |  | Pa |
| $p$ | OX, P | (ships, manoeuvrability) Roll velocity, rotational velocity about body $x$-axis |  | 1/s |

ITTC Symbols

| Version 2021 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |


| $p_{0}$ | P0 | (fluid mechanics, flow fields) <br> Ambient pressure in undis- <br> turbed flow |  | Pa |
| :--- | :--- | :--- | :--- | :--- |
| $p_{0}$ | PR0 | (ships, hull resistance, water <br> jets) Ambient pressure in un- <br> disturbed flow | $\mathrm{N} / \mathrm{m}^{2}$ |  |
| $p_{\mathrm{A}}$ | PA | (fluid mechanics, cavitation) <br> Ambient pressure |  | Pa |
| $p_{\mathrm{AC}}$ | PACO | (fluid mechanics, cavitation) <br> Collapse pressure | Absolute ambient pressure at <br> which cavities collapse | Pa |
| $p_{\mathrm{AI}}$ | PBIC | (fluid mechanics, cavitation) <br> Critical pressure | Absolute ambient pressure at <br> which cavitation inception <br> takes place | Pa |
| $p_{\mathrm{B}}$ | PBS | (ACV and SES) Mean bag <br> pressure | (ACV and SES) Bow seal <br> pressure | Pressure in the bow seal bag | Pa | $p_{\mathrm{BS}}$ |
| :--- |

## ITTC Symbols

| Version 2021 |  | P, P |  |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC <br> Symbol | Computer <br> Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |
| $\dot{p}$ | OXRT, PR | (ships, manoeuvrability) <br> Roll acceleration, angular <br> acceleration about body x- <br> axis | $d p / d t$ | $1 / \mathrm{s}^{2}$ |

## ITTC Symbols

Version 2021
Q, q

| ITTC | Computer | Name | Definition or | SI- |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |  | Explanation | Unit |


| Q | Q | (ships, performance) Torque | $P_{\mathrm{D}} / \omega$ | Nm |
| :---: | :---: | :---: | :---: | :---: |
| Q |  | (fundamental, balances and system related) Quantity under consideration |  | $Q^{\mathrm{U} / \mathrm{s}}$ |
| Q | QF, QFLOW | (fluid mechanics, flow fields) Rate of flow | Volume passing across a control surface in time unit | $\mathrm{m}^{3} / \mathrm{s}$ |
| Q | QF | (fluid mechanics, boundary layers) Entrainment | $\begin{aligned} & b \\ & f U d y \\ & a \\ & \hline \end{aligned}$ | $\mathrm{m}^{2} / \mathrm{s}$ |
| Q |  | (ships, hull resistance, water jets) Impeller torque |  | Nm |
| $Q_{\text {AW }}$ | QAW | (ships, seakeeping) Mean torque increased in waves |  | Nm |
| $Q_{\text {BS }}$ | QBS | (ACV and SES) Bow seal air flow rate | Air flow rate to the bow seal | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q_{\mathrm{bl}}$ |  | (ships, hull resistance, water jets) Volume flow rate inside boundary layer |  | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q^{\text {C }}$ | QCF | (fundamental, balances and system related) Convective flux |  | $Q^{\mathrm{U} / \mathrm{s}}$ |
| $Q \mathrm{cu}$ | QCU | (ACV and SES) Cushion air flow rate | Air flow rate to cushion | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q^{\text {D }}$ | QDF | (fundamental, balances and system related) Diffusive flux |  | $Q^{\mathrm{U} / \mathrm{s}}$ |
| $Q^{\text {F }}$ | QFL | (fundamental, balances and system related) Total flux across the surface of the control volume | Inward positive! | $Q^{\mathrm{U}} / \mathrm{s}$ |
| $Q_{\text {FB }}$ | QFB | (ships, manoeuvrability, seakeeping) Torque of bow fin |  | Nm |
| $Q_{\text {FS }}$ | QFS | (ships, manoeuvrability, seakeeping) Torque of stern fin |  | Nm |
| $Q_{\text {IA }}$ | QIMS | (ice going vessels) Average torque in ice |  | Nm |
| $Q_{\text {J }}$ |  | (ships, hull resistance, water jets) Volume flow rate through water jet system |  | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q^{\mathrm{M}}$ | QDM | (fundamental, balances and system related) Molecular diffusion |  | $Q^{\mathrm{U}} / \mathrm{s}$ |
| $Q^{\text {P }}$ | QPN | (fundamental, balances and system related) Production of sources in the control volume |  | $Q^{\mathrm{U}} / \mathrm{s}$ |

## ITTC Symbols

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $Q_{R}$ | QRU | (ships, manoeuvrability, seakeeping) Torque about rudder stock |  | Nm |
| :---: | :---: | :---: | :---: | :---: |
| Qs | QSP | (ships, propulsor performance) Spindle torque | About spindle axis of controllable pitch propeller $Q_{\mathrm{S}}=Q_{\mathrm{SC}}+Q_{\mathrm{SH}}$ positive if it increases pitch | Nm |
| $Q^{\text {S }}$ | QRT | (fundamental, balances and system related) Storage in the control volume, rate of change of the quantity stored | $d q / d t$ | $Q^{\mathrm{U} / \mathrm{s}}$ |
| Qsc | QSPC | (ships, propulsor performance) Centrifugal spindle torque |  | Nm |
| $Q_{\text {sH }}$ | QSPH | (ships, propulsor performance) Hydrodynamic spindle torque |  | Nm |
| Qss | QSS | (ACV and SES) Stern seal air flow rate | Air flow rate to the stern seal | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q_{\text {T }}$ | QT | (ACV and SES) Total air volume flow |  | $\mathrm{m}^{3} / \mathrm{s}$ |
| $Q^{\text {T }}$ | QDT | (fundamental, balances and system related) Turbulent diffusion |  | $Q^{\mathrm{U} / \mathrm{s}}$ |
| $Q_{\text {TS }}$ | QTS | (ACV and SES) Total air volume flow of skirt |  | $\mathrm{m}^{3} / \mathrm{s}$ |
| $q$ |  | (uncertainty) Random quantity |  | 1 |
| $\bar{q}$ |  | (uncertainty) Arithmetic mean or average |  | 1 |
| $q$ | QQ | (fundamental, balances and system related) Quantity of the quality under consideration stored in a control volume |  | $Q^{\mathrm{U}}$ |
| $q$ | UNQ | (solid body mechanics, loads) Load per unit length |  | N/m |
| $q$ | Q | (solid body mechanics, rigid body motions) Rotational velocity around body axis $y$ |  | rad/s |
| $q$ | PD, EK | (fluid mechanics, flow fields) Dynamic pressure, density of kinetic flow energy, | $\rho V^{2} / 2$ | Pa |
| $q$ | PD, EK | (ships, hull resistance) Dynamic pressure, density of kinetic flow energy, | $\begin{array}{\|l} \rho V^{2} / 2 \\ \text { see 3.3.2 } \end{array}$ | Pa |

## ITTC Symbols

Version 2021
Q, q

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $q$ | OY, Q | (ships, manoeuvrability) <br> Pitch velocity, rotational ve- <br> locity about body $y$-axis |  | $1 / \mathrm{s}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\dot{q}$ | QR | Rates of change of compo- <br> nents of rotational velocity <br> relative to body axes |  | $\mathrm{rad} / \mathrm{s}^{2}$ |
| $q_{\mathrm{A}}$ | QA | (ships, propulsor perfor- <br> mance) Dynamic pressure <br> based on advance speed | $\rho V_{\mathrm{A}}^{2} / 2$ | Pa |
| $q_{k}$ | PDWR, <br> EKWR | (uncertainty) kth observation <br> of $q$ | (ships, hull resistance) Dy- <br> (independent repeated ob- <br> namic pressure based on ap- <br> parent wind | $\rho V_{\mathrm{WR}}{ }^{2} / 2$ <br> ing quantity $q$ |
| $q_{\mathrm{R}}$ | Qsee 3.4 .2 |  |  |  |

## ITTC Symbols

Version 2021
R, r

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $R$ | R | (fundamental, time and frequency domain quantity) Complex variable | $\exp \left(s T_{s}\right)$ Laurent transform |  |
| :---: | :---: | :---: | :---: | :---: |
| $R$ | R, RE | (ships, basic quantities) Resistance (force) | Force opposing translatory velocity | N |
| $R$ | RD | (ships, basic quantities) Radius |  | m |
| $R$ | RDP | (ships, propulsor geometry) <br> Propeller radius |  | m |
| $R_{0}$ | R0 | (ships, ship performance) <br> Full scale resistance without overload |  | N |
| $R_{\text {A }}$ | RA | (ships, hull resistance) Model-ship correlation allowance | Incremental resistance to be added to the smooth ship resistance to complete the model-ship prediction | N |
| $R_{\text {AA }}$ | RAA | (ships, hull resistance) Air or wind resistance |  | N |
| $R_{\text {APP }}$ | RAP | (ships, hull resistance) Appendage resistance |  | N |
| $R_{\text {AR }}$ | RAR | (ships, hull resistance) <br> Roughness resistance |  | N |
| $R_{\text {ASK }}$ | RASK | (ACV and SES) Intake momentum resistance of skirt | $\rho_{\text {A }} Q_{\text {TS }} V_{\text {A }}$ | N |
| $R_{\text {AW }}$ | RAW | (ships, seakeeping, sailing vessels) Mean added resistance in waves |  | N |
| $R_{\text {At }}$ | RAT | (ACV and SES) Total aerodynamic resistance | $R_{M}+R_{0}$ | N |
| $R_{\text {C }}$ | RC | (ships, hull resistance) Resistance corrected for difference in temperature between resistance and self-propulsion tests | $\begin{aligned} & R_{\mathrm{TM}}\left[(1+k) C_{\mathrm{FMC}}+C_{\mathrm{R}}\right] / \\ & {\left[(1+k) C_{\mathrm{FM}}+C_{\mathrm{R}}\right]} \end{aligned}$ <br> where $\mathrm{C}_{\text {fм }}$ is the frictional coefficient at the temperature of the self-propulsion test | N |
| $R_{\text {C }}$ | RCS | (ships, manoeuvrability, turning circles) Steady turning radius |  | m |
| $R e$ | RN | (fluid mechanics, flow parameter) Reynolds number | $V L / v$ | 1 |
| $R e_{0.7}$ | RN07 | (fluid mechanics, flow parameter) Propeller Reynolds number at 0.7 R | $R e_{0.7}=\frac{c_{0.7} \sqrt{V_{A}^{2}+(0.7 \pi n D)^{2}}}{v}$ | 1 |
| $R e_{\delta^{*}}$ | RDELS | (fluid mechanics, boundary layers) Reynolds number based on displacement thickness | $U_{\infty} \delta^{*} / v$ or $U_{\mathrm{e}} \delta^{*} / v$ | 1 |

## ITTC Symbols

Version 2021
R, r

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $R e_{\theta}$ | RTHETA | (fluid mechanics, boundary layers) Reynolds number based on momentum thickness | $U_{\infty} \Theta / v$ or $U_{\mathrm{e}} \Theta / v$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\text {F }}$ | RF | (ships, hull resistance) Frictional resistance of a body | Due to fluid friction on the surface of the body | N |
| $R_{\text {F0 }}$ | RF0 | (ships, hull resistance) Frictional resistance of a flat plate |  | N |
| $R_{\text {Fint }}$ | RFINT | (multi-hull vessels) Frictional resistance interference correction | $R_{\text {FMH }}-\Sigma R_{\text {F }}$ | N |
| $R_{\text {FMH }}$ | RFMH | (multi-hull vessels) Frictional resistance of multihull vessel |  | N |
| $R_{\text {FU }}$ |  | (sailing vessels) Friction resistance (upright) |  | N |
| $R_{\text {H }}$ | RH | (ACV and SES) Hydrodynamic resistance | $R_{\mathrm{W}}+R_{\text {WET }}$ | N |
| $R_{\text {H }}$ | RH | (fluid mechanics, flow parameter) Hydraulic radius | Area of section divided by wetted perimeter | m |
| $R_{\mathrm{H}}$ | RTUHA | (sailing vessels) Resistance increase due to heel (with zero side force) |  | N |
| $R_{\mathrm{I}}$ |  | (sailing vessels) Resistance increase due to side (induced resistance) |  | N |
| $R_{\text {I }}$ | RI | (ice going vessels) Net ice resistance | $R_{\text {IT }}-R_{\text {IW }}$ | N |
| $R_{\text {IT }}$ | RIT | (ice going vessels) Total resistance in ice | Ship towing resistance in ice | N |
| $R_{\text {IW }}$ | RIW | (ice going vessels) Hydrodynamic resistance in presence of ice | Total water resistance of ship in ice | N |
| $R_{\mathrm{k}}$ | RAKG | (ships, propulsor geometry) <br> Rake | The displacement from the propeller plane to the generator line in the direction of the shaft axis. Aft displacement is positive rake. | m |
| $R_{\mathrm{K}}$ | RKEEL | (planing, semi-displacement vessels) Keel drag |  | N |
| $R_{M}$ | RM | (ACV and SES) Intake momentum resistance in general | $\rho_{\text {A }} Q_{\text {T }} V_{\text {A }}$ | N |
| $R_{\text {MCU }}$ | RMCU | (ACV and SES) Intake momentum resistance of cushion | $\rho_{\mathrm{A}} Q_{\mathrm{cu}} V_{\mathrm{A}}$ | N |

## ITTC Symbols

Version 2021
R, r

| ITTC | Computer | Name | Definition or | SI- |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |  | Explanation | Unit |


| $R_{P}$ | RP | (ships, hull resistance) Pres- <br> sure resistance | Due to the normal stresses <br> over the surface of a body | N |
| :--- | :--- | :--- | :--- | :--- |
| $R_{\mathrm{PAR}}$ | RPAR | (planing, semi-displacement <br> vessels) Parasitic drag | Drag due to inlet and outlet <br> openings | N |
| $R_{P \mathrm{~S}}$ | RSP | (planing, semi-displacement <br> vessels) Pressure component <br> of spray drag | N |  |
| $R_{P \mathrm{~V}}$ | RPV | (ships, hull resistance) Vis- <br> cous pressure resistance | Due to normal stress related <br> to viscosity and turbulence | N |
| $R R_{\mathrm{R}}$ | RR | (fundamental, statistical, <br> stochastic) Population corre- <br> lation | (ships, hull resistance) Re- <br> siduary resistance | $R_{\mathrm{T}}-R_{\mathrm{F}}$ or $R_{\mathrm{T}}-R_{\mathrm{Fo}}$ |

## ITTC Symbols

Version 2021
R, r

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $R_{\text {TU }}$ | RTU | (sailing vessels) Total resistance (upright) |  | N |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\text {Tw }}$ | RTW | (ships, ship performance) <br> Total resistance in wind and waves |  | N |
| $R_{\text {T } \varphi}$ | RTUH | (sailing vessels) Total resistance when heeled | $R_{\text {TU }}+R_{\varphi}$ | N |
| $R_{\mathrm{U}}$ | RU | (ships, propulsor performance) Pod unit resistance | Resistance of a podded drive unit | N |
| $R_{u}$ | R(U) | (ships, unsteady propeller forces) Generalized vibratory bearing reaction | $\begin{aligned} & u=1, . ., 6 \\ & u=1,2,3: \text { force } \\ & u=4,5,6: \text { moment } \end{aligned}$ | $\begin{aligned} & \hline \mathrm{N} \\ & \mathrm{~N} \\ & \mathrm{Nm} \\ & \hline \end{aligned}$ |
| $R_{V}$ | RV | (ships, hull resistance) Total viscous resistance | $R_{\mathrm{F}}+R_{P V}$ | N |
| $R \mathrm{vs}$ | RSV | (planing, semi-displacement vessels) Viscous component of spray drag | $C_{\text {F }} S_{\text {ws }} q_{\text {S }}$ | N |
| $R_{\text {W }}$ | RW | (ships, hull resistance) Wave making resistance | Due to formation of surface waves | N |
| $R_{\text {wb }}$ | RWB | (ships, hull resistance) Wave breaking resistance | Associated with the break down of the bow wave | N |
| $R_{\text {WET }}$ | RWET | (ACV and SES) Resistance due to wetting |  | N |
| $R_{\text {WP }}$ | RWP | (ships, hull resistance) Wave pattern resistance |  | N |
| $R_{\text {xX }}$ | XXRR | (fundamental, statistical, stochastic) Auto-correlation of a stationary stochastic process | $\begin{aligned} & x(t) x(t+\tau)^{\mathrm{E}}=R_{x x}(\tau) \\ & R_{x x}(\tau)=R_{x x}(-\tau) \end{aligned}$ <br> if $x$ is ergodic: $\begin{aligned} & R_{x x}(\tau)=x(t) x(t+\tau)^{\mathrm{MR}} \\ & R_{x x}(\tau)=\int S_{x x}(\omega) \cos (\omega \tau) d \tau \\ & \tau=0 \ldots \infty \end{aligned}$ | $\begin{aligned} & x x^{R}, x x^{R R}, \\ & R_{x x} \end{aligned}$ |
| $R_{X x}$ | XXMR | (fundamental, statistical) Auto-correlation of a random quantity | $x x^{\mathrm{E}}$ |  |
| $R_{x y}$ | XYRR | (fundamental, statistical, stochastic) Cross-correlation of two stationary stochastic processes | $\begin{aligned} & x(t) y(t+\tau)^{\mathrm{E}}=R_{x y}(\tau) \\ & R_{y x}(\tau)=R_{x y}(-\tau) \end{aligned}$ <br> if $x$, $y$ are ergodic: $R_{x y}(\tau)=x(t) y(t+\tau)^{M R}$ | $x y^{R}, R_{x y}$ |
| $R_{x y}$ | XYMR | (fundamental, statistical) Cross-correlation of two random quantities | $x y^{E}$ |  |
| $R_{\pi}$ | RPI | (planing, semi-displacement vessels) Induced drag | $g \rho \nabla \operatorname{tg} \tau$ | N |
| $R_{\varphi}$ | RTUHA | (sailing vessels) Resistance increase due to heel (with zero side force) |  | N |

## ITTC Symbols

Version 2021
R, r

| ITTC | Computer | Name | Definition or <br> Explanation | SI- |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |  | Unit |  |


| $r$ | R | (solid body mechanics, rigid body motions) Rotational velocity around body axis z |  | rad/s |
| :---: | :---: | :---: | :---: | :---: |
| $r$ | RD | (ships, basic quantities) Radius |  | m |
| $r$ | LR | (ships, propulsor geometry) Blade section radius |  | m |
| $r$ | OZ, R | (ships, manoeuvrability) Yaw velocity, rotational velocity about body z-axis |  | 1/s |
| $r\left(X_{i}, X_{j}\right)$ |  | (uncertainty) Estimated correlation coefficient | $r\left(x_{i}, x_{j}\right)=u\left(x_{i}, x_{j}\right) /\left(u\left(x_{i}\right) u\left(x_{j}\right)\right)$ | 1 |
| $r$ | R | (ships, unsteady propeller forces) Cylindrical coordinates | Cylindrical system with origin $O$ and longitudinal $x$ axis as defined before; angular a-(attitude)-coordinate , zero at 12 o'clock position, positive clockwise looking forward, $r$ distance measured from the $x$-axis | m |
| $r$ |  | (seakeeping, large amplitude motions capsizing) Effective wave slope coefficient |  | 1 |
| $r_{C}$ | OZCI | (ships, manoeuvrability, turning circles) Steady turning rate |  | 1/s |
| $r_{C}{ }^{\prime}$ | OZCINO | (ships, manoeuvrability, turning circles) Non-dimensional steady turning rate | $r_{\mathrm{C}} L_{\text {PP }} / U_{\mathrm{C}}$ or $2 L_{\mathrm{PP}} / D_{\mathrm{C}}$ | m |
| $r_{\text {h }}$ | RH | (ships, propulsor geometry) <br> Hub radius |  | m |
| $\dot{r}$ | RR | (solid body mechanics, rigid body motions) Rates of change of components of rotational velocity relative to body axes |  | $\mathrm{rad} / \mathrm{s}^{2}$ |
| $\dot{r}$ | OZRT, RR | (ships, manoeuvrability) Yaw acceleration, angular acceleration about body zaxis | $d r / d t$ | $1 / \mathrm{s}^{2}$ |

ITTC Symbols
Version 2021

| ITTC <br> Symbol | Computer <br> Symbol | Name | Definition or <br> Explanation | SI- <br> Unit |
| :--- | :--- | :--- | :--- | :--- |


| S | S, AWS | (ships, hull geometry) Area of wetted surface |  | $\mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| S | S | (ships, hull resistance) Wetted surface area, underway | $S_{\text {BH }}+S_{\text {APP }}$ | $\mathrm{m}^{2}$ |
| $S_{0}$ | S0 | (ships, hull resistance) Wetted surface area, at rest | $S_{\text {BH0 }}+S_{\text {APP0 }}$ | $\mathrm{m}^{2}$ |
| $S^{0}{ }_{i j}$ | SM0(I,J) | Zero ${ }^{\text {th }}$ order moment of a scalar quantity | $\delta_{i j} d s=\delta_{i j} S$ |  |
| $S^{1}{ }_{i j}$ | SM1(I,J) | (fundamental. coordinate and space related) First order moment of a scalar quantity, formerly static moments of a scalar distribution | $\iint_{\mathcal{E}_{i k j} \chi_{k} d s}$ |  |
| $S^{2}{ }_{i j}$ | SM2(I,J) | (fundamental. coordinate and space related) Second moment of a scalar quantity, formerly moments of inertia of a scalar distribution | $\iint_{\text {kli }} \chi_{l \delta_{j k m}} X_{m} d s$ |  |
| $S_{\text {A }}$ | SRA | (ships, propulsor performance) Apparent slip ratio | 1-V/(nP) | 1 |
| $S_{A}$ | AS | (sailing vessels) Sail area in general | $(P E+I J) / 2$ | $\mathrm{m}^{2}$ |
| $S_{\text {APP }}$ | SAP | (ships, hull resistance) Appendage wetted surface area, underway |  | $\mathrm{m}^{2}$ |
| $S_{\text {APP0 }}$ | SAP0 | (ships, hull resistance) Appendage wetted surface area, at rest |  | $\mathrm{m}^{2}$ |
| $S_{\text {BH }}$ | SBH | (ships, hull resistance) Bare Hull wetted surface area, underway |  | $\mathrm{m}^{2}$ |
| $S_{\text {BH0 }}$ | SBH0 | (ships, hull resistance) Bare Hull wetted surface area, at rest |  | $\mathrm{m}^{2}$ |
| $S^{C}$ | CIRCS | (ships, hull geometry, hull resistance) R.E. Froude's wetted surface area coefficient | $S / \nabla^{2 / 3}$ | 1 |
| $S_{\text {c }}$ | SC | (sailing vessels) Wetted surface area of canoe body |  | $\mathrm{m}^{2}$ |
| $S_{\text {H }}$ | THL | (fluid mechanics, flow fields) Total head loss |  | m |
| S\%o | SSH0 | (ACV and SES) Wetted area of side hulls at rest off cushion | Total wetted area of side walls under way on cushion | $\mathrm{m}^{2}$ |

ITTC Symbols

| Version 2021 |  |  | S, S |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or | SI- |
| Symbol | Symbol |  | Explanation | Unit |


| $S_{\text {I }}$ | SAIC | (environmental mechanics, ice) Salinity of ice | Weight of salt per unit weight of ice | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & S_{i}(f), \\ & S_{i}(\omega) \end{aligned}$ | $\begin{aligned} & \text { EISF, } \\ & \text { EISC } \end{aligned}$ | (environmental mechanics, waves) Incident wave power spectral density |  | $\mathrm{m}^{2} / \mathrm{Hz}$ |
| $S_{\mathrm{K}}$ | SK | (sailing vessels) Wetted surface area of keel |  | $\mathrm{m}^{2}$ |
| $\begin{aligned} & S_{\eta}(f), S_{\eta \eta}(f), \\ & S_{\eta}(\omega), S_{\eta \eta}(\omega) \\ & \hline \end{aligned}$ | EWSF, EWSC | (ships, seakeeping) Wave elevation auto spectral density |  | $\mathrm{m}^{2} \mathrm{~s}$ |
| $\begin{aligned} & S_{n}(f), \\ & S_{n}(\omega) \end{aligned}$ | EWSF, EWSC | (environmental mechanics, waves) Wave power spectral density |  | $\mathrm{m}^{2} / \mathrm{Hz}$ |
| $S_{\text {R }}$ | SRR | (ships, propulsor performance) Real slip ratio | $1-V_{A} /(n P)$ | 1 |
| $S_{\text {R }}$ | SR | (sailing vessels) Wetted surface area of rudder |  | $\mathrm{m}^{2}$ |
| $\begin{aligned} & S_{r}(f), \\ & S_{r}(\omega) \end{aligned}$ | ERSF, <br> ERSC | (environmental mechanics, waves) Reflected wave power spectral density |  | $\mathrm{m}^{2} / \mathrm{Hz}$ |
| Ss | SWS | (planing, semi-displacement vessels) Area wetted by spray | Wetted area between design line or stagnation line and spray edge | $\mathrm{m}^{2}$ |
| $S_{\text {SHC }}$ | SSHC | (ACV and SES) Wetted area of side hulls under way on cushion | Total wetted area of side walls under way on cushion | $\mathrm{m}^{2}$ |
| $S_{\text {SH }}$ | SSH | (ACV and SES) Wetted area of side hulls under way off cushion | Total wetted area of side walls under way off cushion | $\mathrm{m}^{2}$ |
| St | SN | (fluid mechanics, flow parameter) Strouhal number | $f L / V$ | 1 |
| STIX | STIX | (seakeeping, large amplitude motions capsizing) Actual stability index value according to ... |  | 1 |
| $\underline{\text { STIX }}$ | STIXR | (seakeeping, large amplitude motions capsizing) Required stability index value, see ... |  | 1 |
| $S_{u v}$ | $S(\mathrm{U}, \mathrm{V})$ | (fundamental. coordinate and space related) Generalized moment of a scalar quantity distributed in space | $\begin{aligned} & S_{i j}=S^{0}{ }_{i j} \\ & S_{i, 3+j}=S^{1}{ }_{i j} \\ & S_{3+i, j}=S^{1}{ }_{i j} \\ & S_{3+i, 3+j}=S^{2}{ }_{i j} \\ & \hline \end{aligned}$ |  |
| $S_{\text {w }}$ | SAWA | (environmental mechanics, ice) Salinity of water | Weight of dissolved salt per unit weight of saline water | 1 |
| $S_{\text {Wb }}$ | SWB | (planing, semi-displacement vessels) Wetted bottom area, underway | Area bounded by stagnation line, chines or water surface underway and transom | $\mathrm{m}^{2}$ |

ITTC Symbols
Version 2021
S, s


| $S_{\text {WBK }}$ | SWBK | Wetted surface area of bilge keels |  | $\mathrm{m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $S_{\text {WHP }}$ | SWHP | (planing, semi-displacement vessels) Wetted area underway of planing hull | Principal wetted area bounded by trailing edge, chines and spray root line | $\mathrm{m}^{2}$ |
| $S_{\text {WHE }}$ | SWHE | (planing, semi-displacement vessels) Wetted hull area, underway | Total wetted surface of hull underway, including spray area and wetted side area, w/o wetted transom area | $\mathrm{m}^{2}$ |
| $S_{\text {whs }}$ | SWSH | (planing, semi-displacement vessels) Area of wetted sides | Wetted area of the hull side above the chine or the design water line | $\mathrm{m}^{2}$ |
| $S_{\text {ws }}$ | SWS | (planing, semi-displacement vessels) Area wetted by spray | Wetted area between design line or stagnation line and spray edge | $\mathrm{m}^{2}$ |
| $S_{x x}$ | XXSR | (fundamental, statistical, stochastic) Power spectrum or autospectral power density of a stochastic process | $x x^{R R S R}$ |  |
| $S_{x y}$ | XYSR | (fundamental, statistical, stochastic) Cross-power spectrum of two stationary stochastic processes | $x y^{R R S R}$ |  |
| $\begin{aligned} & \hline S_{\zeta}(\omega, \mu) \\ & S_{\theta}(\omega, \mu) \\ & \text { etc. } \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { S2ZET } \\ & \text { S2TET } \\ & \text { etc. } \\ & \hline \end{aligned}$ | (environmental mechanics, waves) Two dimensional spectral density |  | 1 |
| $\left\lvert\, \begin{aligned} & S_{\rho}(f, \theta) \\ & S_{\zeta}(\omega, \mu) \end{aligned}\right.$ | STHETA | (environmental mechanics, waves) Directional spectral density |  | $\begin{aligned} & \mathrm{m}^{2} / \mathrm{Hz} / \\ & \mathrm{rad} \end{aligned}$ |
| $s$ | S | (fundamental. coordinate and space related) Any scalar quantity distributed, maybe singularly, in space | $\int d s$ |  |
| s | S | (fundamental, time and frequency domain quantity) Complex variable | $a+2 \pi i f$ <br> Laplace transform | 1/s |
| $s$ | SP | (ships, basic quantities) Distance along path |  | m |
| $s$ |  | (seakeeping, large amplitude motions capsizing) Wave steepness |  | 1 |
| $s_{F}$ | SPF | (ships, manoeuvrability, stopping man.) Distance along track, track reach |  | m |

ITTC Symbols
Version 2021
S, s

|  | Computer Symbol | Name | Definition or | SI- |
| :---: | :---: | :---: | :---: | :---: |
| Symbol | Symbol | Name | Explanation | Unit |


| $s_{i j}$ | ST(I,J) | (fluid mechanics, flow fields) Total stress tensor | Density of total diffusive momentum flux due to molecular and turbulent exchange | Pa |
| :---: | :---: | :---: | :---: | :---: |
| $s^{\text {V }}{ }^{\text {ij }}$ | SV(I,J) | (fluid mechanics, flow fields) <br> Viscous stress |  | Pa |
| $s_{p}$ |  | (uncertainty) Pooled experimental standard deviation | Positive square root of $s_{\mathrm{p}}^{2}$ |  |
| $\mathrm{s}_{\mathrm{p}}^{2}$ |  | (uncertainty) Pooled estimate of variance |  | 1 |
| $s^{2}(\bar{q})$ |  | (uncertainty) Experimental variance of the mean | $s^{2}(\bar{q})=s^{2}\left(q_{k}\right) / n ; \text { estimated }$ <br> variance obtained from a Type A evaluation | 1 |
| $s(\bar{q})$ |  | (uncertainty) Experimental standard deviation of the mean | Positive square root of $s^{2}(\bar{q})$ | 1 |
| $s^{2}\left(q_{k}\right)$ |  | (uncertainty) Experimental variance from repeated observations |  | 1 |
| $s\left(q_{k}\right)$ |  | (uncertainty) Experimental standard deviation of repeated observations | Positive square root of $s^{2}\left(q_{k}\right)$ | 1 |
| $\mathrm{s}^{\mathrm{R}}{ }^{\text {ij }}$ | SR(I,J) | Turbulent or Reynolds stress | $\rho v_{i} v_{j}^{C R}$ | Pa |
| $s^{2}\left(\bar{X}_{i}\right)$ |  | (uncertainty) Experimental variance of input mean | From mean $\bar{X}_{i}$, determined from $n$ independent repeated observations $X_{i, k}$, estimated variance obtained from a Type A evaluation. | 1 |
| $s\left(\bar{X}_{i}\right)$ |  | (uncertainty) Standard deviation of input mean | Positive square root of $s^{2}\left(\bar{X}_{1}\right)$ | 1 |
| $s(\bar{q}, \bar{r})$ |  | (uncertainty) Estimate of covariance of means |  | 1 |
| $s\left(\bar{X}_{i}, \overline{X_{j}}\right)$ |  | (uncertainty) Estimate of covariance of input means |  | 1 |
| $S_{V}$ | SINKV | (ships, performance) Sinkage, dynamic | Change of draft, fore and aft, divided by length | 1 |
| $S_{X}$ | XDS | (fundamental, statistical) Sample deviation of a random quantity | $x^{V S 1 / 2}$, unbiased random estimate of the standard deviation | 1 |

ITTC Symbols
Version 2021
T, t

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or |
| :--- |
| Explanation |


| $T$ | T | (ships, hull geometry, seakeeping, large amplitude motions capsizing) Draught, moulded, of ship hull |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $T$ | TC | (ships, basic quantities, ships, seakeeping) Period, Wave period | Duration of a cycle of a repeating or periodic, not necessarily harmonic process | S |
| $T$ | TIC | (ships, manoeuvrability, seakeeping) Time constant of the 1st order manoeuvring equation |  | s |
| $T$ | TH | (ships, propulsor performance) Propeller thrust |  | N |
| $T$ | YHA | (seakeeping, large amplitude motions capsizing) Equivalent transverse heeling arm | Heeling moment/ $\Delta$ | m |
| $T_{01}$ | T1 | (environmental mechanics, waves) Average period from zeroth and first moment | $m_{0} / m_{1}$ | s |
| $T_{02}$ | T2 | (environmental mechanics, waves) Average period from zeroth and second moment | $\left(m_{0} / m_{2}\right)^{1 / 2}$ | s |
| $T_{1}$ | TIC1 | (ships, manoeuvrability, seakeeping) First time constant of manoeuvring equation |  | s |
| $T_{1 / 3 d}$ | T13D | Significant wave period | By downcrossing analysis | s |
| $T_{1 / 3}$ | T13U | Significant wave period | By upcrossing analysis | s |
| $T_{2}$ | TIC2 | (ships, manoeuvrability, seakeeping) Second time constant of manoeuvring equation |  | s |
| $T_{3}$ | TIC3 | (ships, manoeuvrability, seakeeping) Third time constant of manoeuvring equation |  | s |
| $T_{\text {A }}$ | TA, TAP | (ships, hull geometry) Draught at aft perpendicular |  | m |
| $T_{\text {AD }}$ | TAD, TAPD | (ships, hull geometry) Design draught at aft perpendicular |  | m |
| $T_{\text {AW }}$ | TAW | (ships, seakeeping) Mean thrust increase in waves |  | N |
| $T^{\text {C }}$ | CIRCT | (ships, hull geometry) R.E. Froude's draught coefficient | $T / \nabla^{1 / 3}$ | 1 |
| $T_{\mathrm{C}}$ | TC | (fundamental, time and frequency domain quantity) Pe riod of cycle | $1 / f_{\mathrm{C}}$ <br> duration of cycles in periodic, repeating processes | s |

## ITTC Symbols

Version 2021

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$| Name |
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| Explanation |


| $T_{\text {C }}$ | TC0 | (ACV and SES) Cushion thrust |  | N |
| :---: | :---: | :---: | :---: | :---: |
| $T_{\mathrm{C}}$ | TCAN | (sailing vessels) Draught of canoe body |  | m |
| $T_{\text {D }}$ | THDU | (ships, propulsor performance) Duct thrust of a ducted propeller unit |  | N |
| $T_{\mathrm{P}}$ | THDP | (ships, propulsor performance) Propeller thrust of a ducted propeller unit |  | N |
| $T_{\text {T }}$ | THDT | (ships, propulsor performance) Total thrust of a ducted propeller unit |  | N |
| $T_{\text {d }}$ | TD | (environmental mechanics, waves) Wave periods by zero down-crossing | Time elapsing between two successive downward crossings of zero in a record | s |
| $T_{\text {E }}$ | TE | (ships, seakeeping) <br> Wave encounter period |  | s |
| $T_{\text {EFF }}$ | TEFF | (sailing vessels) Effective draught | $F_{\mathrm{H}} /\left(\rho V_{\mathrm{B}}{ }^{2} R\right)^{5}$ | m |
| $T_{\text {F }}$ | TF, TFP | (ships, hull geometry) Draught at forward perpendicular |  | m |
| $T_{\text {F }}$ | TFO | (hydrofoil boats) Foil immersion | Distance between foil chord and mean water surface | m |
| $T_{\text {FD }}$ | TFPD | (ships, hull geometry) Design draught at forward perpendicular |  | m |
| $T_{\text {FD }}$ | TFD | (hydrofoil boats) Depth of submergence of apex of a dihedral foil | Distance between foil apex and mean water surface | m |
| $T_{\text {FM }}$ | TFOM | (hydrofoil boats) Mean depth of foil submergence |  | m |
| $T_{\text {H }}$ | THUL | (ships, hull geometry) Draught of the hull | Maximum draught of the hull without keel or skeg | m |
| Th | TN | (fluid mechanics, cavitation, fluid mechanics, flow parameter) Thoma number Cavitation number | $\left(\begin{array}{l} \left(H_{\mathrm{U}}-p_{\mathrm{V}} / w\right) / H_{\mathrm{N}} \\ \left(p_{\mathrm{A}}-p_{\mathrm{V}}\right) / q \end{array}\right.$ | 1 |
| $T_{\text {IA }}$ | TIMS | (ice going vessels) Average total thrust in ice |  | N |

## ITTC Symbols

Version 2021
T, t

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
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| Explanation |


| $T_{i j}$ | $T(\mathrm{I}, \mathrm{J})$ | (fundamental. coordinate and space related) Tensor in space referred to an orthogonal system of Cartesian coordinates fixed in the body | $T_{i j}{ }^{s}+T_{i j}{ }^{a}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $T_{i j}{ }^{\text {A }}$ | TAS(I,J) | (fundamental. coordinate and space related) Antisymmetric part of a tensor | $\left(T_{i j}-T_{j i}\right) / 2$ |  |
| $T_{i j}{ }^{\text {S }}$ | TSY(I,J) | (fundamental. coordinate and space related) Symmetric part of a tensor | $\left(T_{i j}+T_{j i}\right) / 2$ |  |
| $T_{i j}{ }^{\text {T }}$ | TTR(I,J) | (fundamental. coordinate and space related) Transposed tensor | $T_{j i}$ |  |
| $T_{i j} v_{j}$ |  | (fundamental. coordinate and space related) Tensor product | $\Sigma T_{i j} V_{j}$ |  |
| $T_{j x}$ | TJX | Jet thrust (can be measured directly in bollard pull condition) |  | N |
| TL |  | (seakeeping, large amplitude motions capsizing) Turning lever |  | 1 |
| $T_{M}$ | TM, TMS | (ships, hull geometry) Draught at midship | $\left(T_{\mathrm{A}}+T_{\mathrm{F}}\right) / 2$ for rigid bodies with straight keel | m |
| $T_{\text {MD }}$ | TMD, TMSD | (ships, hull geometry) Design draught at midship | $\begin{aligned} & \begin{array}{l} \left(T_{\mathrm{AD}}+T_{\mathrm{FD}}\right) / 2 \text { for rigid bod- } \\ \text { ies } \end{array} \\ & \hline \end{aligned}$ | m |
| $T_{\text {net }}$ |  | (ships, hull resistance, water jets) Net thrust exerted by the jet system on the hull |  | N |
| $T_{P}$ | TP | (environmental mechanics, waves) Period with maximum energy | $2 \pi f_{P}$ |  |
| $T_{\text {PBS }}$ | TPBS | Bottom Thickness of Strut |  | m |
| $\mathrm{T}_{\mathrm{R}}$ | TR | (environmental mechanics, waves) Duration of record | $1 / \mathrm{f}_{\mathrm{R}}$ | S |
| $T_{\text {rt }}$ | TRT | (environmental mechanics, waves) Return period | The average interval in years between times that a given design wave is exceeded |  |
| $T_{\text {S }}$ | TS | (fundamental, time and frequency domain quantity, environmental mechanics, waves) Sample interval, Period of sampling | $1 / f_{s}$, time between two successive samples, Duration between samples | S |

ITTC Symbols
Version 2021
T, t

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$| Name |
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| Explanation |$\quad$| SI- |
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| $T_{\text {T }}$ | TTR | (ships, hull geometry) Immersion of transom | Vertical depth of trailing edge of boat at keel below water surface level | m |
| :---: | :---: | :---: | :---: | :---: |
| $T_{\mathrm{U}}$ | TU | (ships, propulsor performance) Pod unit thrust, , | Pod unit resistance subtracted from the propeller thrust | N |
| $T_{\mathrm{u}}$ | TU | (environmental mechanics, waves) Wave periods by zero up-crossing | Time elapsing between two successive upward crossings of zero in a record | S |
| $T_{\text {W }}$ | TW | (environmental mechanics, waves) Basic wave period | Time between the passage of two successive wave crests past a fixed point. $1 / f_{\mathrm{w}}$ | S |
| $T_{\text {wv }}$ | TWV | (environmental mechanics, waves) Wave period estimated from visual observation |  | S |
| $T_{\text {x }}$ | TXP | (ships, propulsor performance) Propeller Thrust along shaft axis |  | N |
| $T_{y \mathrm{P}}$ | TYP | (ships, propulsor performance) Propeller normal force in $y$ direction in propeller axis |  | N |
| $T_{z}$ | TNHE | (ships, seakeeping) Natural period of heave |  | s |
| $T_{\text {zP }}$ | TZP | (ships, propulsor performance) Propeller normal force in $z$ direction in propeller axis |  | N |
| $T_{\theta}$ | TNPI | (ships, seakeeping) Natural period of pitch |  | s |
| $T_{\varphi}$ | TNRO | (ships, seakeeping) Natural period of roll |  | S |
| $t$ | TI | (fundamental, time and frequency domain quantity, ships, basic quantities) Time | $-\infty . . .+\infty$ | s |
| $t$ | TE | (ships, basic quantities) Temperature |  | K |
| t | TT | (ships, hull geometry) Taylor tangent of the area curve | The intercept of the tangent to the sectional area curve at the bow on the midship ordinate | 1 |
| $t$ | TM | (ships, propulsor geometry) Blade section thickness |  | m |

ITTC Symbols
Version 2021
T, t

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$| Name |
| :--- | | Definition or |
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| Explanation |$\quad$| SI- |
| :--- |


| $t$ | TMX | (ships, appendage geometry) Maximum thickness of an aerofoil or a hydrofoil | Measured normal to mean line | m |
| :---: | :---: | :---: | :---: | :---: |
| $t$ | YHA | (ships, hydrostatics, stability) Equivalent transverse heeling arm | Heeling moment / 4 | m |
| $t$ | THDF | (ships, performance) Thrust deduction fraction | $\left(T-R_{\mathrm{T}}\right) / T$ | 1 |
| $t$ |  | (ships, hull resistance, water jets) Thrust deduction fraction | $(1-t)=\frac{R_{\mathrm{TBH}}}{T_{\mathrm{net}}}$ | 1 |
| $t_{p}(v)$ |  | (uncertainty) Inverse Student $t$ | Student $t$-distribution for $v$ degrees of freedom corresponding to a given probability $p$ | 1 |
| $t_{p}\left(V_{\text {eff }}\right)$ |  | (uncertainty) Inverse Student $t$ for effective degrees of freedom | Student $t$-distribution for $v_{\text {eff }}$ degrees of freedom corresponding to a given probability $p$ in calculation of expanded uncertainty $U_{p}$ | 1 |
| $t_{180}$ | TI180 | (ships, manoeuvrability, turning circles) Time to reach 180 degree change of heading |  | s |
| $t_{\text {A }}$ | TEAI | (environmental mechanics, <br> ice) Temperature of air |  | ${ }^{\circ} \mathrm{C}$ |
| $t_{\text {a }}$ | TIA | (ships, manoeuvrability, zigzag man..) Initial turning time |  | s |
| $t_{c 1}$ | TIC1 | (ships, manoeuvrability, zigzag man..) First time to check yaw (starboard) |  | s |
| $t_{\text {c } 2}$ | TIC2 | (ships, manoeuvrability, zigzag man..) Second time to check yaw (port) |  | s |
| $t_{\text {D }}$ | TD | (ships, propulsor geometry) <br> Thickness of duct profile |  | m |
| $t_{\text {d }}$ | DURATN | (environmental mechanics, wind) Wind duration |  | S |
| $t_{\text {F }}$ | TIF | (ships, manoeuvrability, stopping man.) Stopping time |  | s |
| $t_{\text {hc }}$ | TCHC | (ships, manoeuvrability, zigzag man..) Period of changes in heading |  | s |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $t_{\mathrm{I}}$ | TEIC | (environmental mechanics, <br> ice) Local temperature of ice |  | ${ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- | :--- | :--- |
| $t_{\mathrm{J}}$ | TI(J) | (fundamental, time and fre- <br> quency domain quantity) <br> Sample time instances | $j T_{\mathrm{S}}$ |  |
| $t_{\mathrm{KL}}$ | TRIM | (seakeeping, large amplitude <br> motions capsizing ships, hy- <br> drostatics, stability) Static <br> trim | $T_{\mathrm{A}}-T_{\mathrm{F}}-d_{\mathrm{KL}}$ | s |
| $t_{\mathrm{r}}$ | TIR | (ships, manoeuvrability, zig- <br> zag man) Reach time | m |  |
| $t_{\mathrm{s}}$ | TRIM | (ships, hydrostatics, stabil- <br> ity, seakeeping, large ampli- <br> tude motions capsizing) <br> Static trim | $T_{\mathrm{A}}-T_{\mathrm{F}}-d_{\mathrm{KL}}$ | m |
| $t_{\mathrm{S}}$ | TSTR | (multi-hull vessels) Maxi- <br> mum thickness of strut | m |  |
| $t_{\mathrm{V}}$ | TV | (ships, performance) Run- <br> ning trim | ${ }^{\circ} \mathrm{C}$ |  |
| $t_{\mathrm{W}}$ | TEWA | (environmental mechanics, <br> ice) Temperature of water |  | m |

ITTC Symbols
Version 2021
$\mathbf{U}, \mathbf{u}$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Snit |


| $U$ | U, UN | (ships, basic quantities) Undisturbed velocity of a fluid |  | m/s |
| :---: | :---: | :---: | :---: | :---: |
| U |  | Expanded uncertainty | Expanded uncertainty of output estimate $y$ that defines an interval $Y=y \pm U$ having a high level of confidence, equal to coverage factor $k$ times the combined standard uncertainty $u_{c}(y)$ of $y: U=k$ $u_{c}(y)$ |  |
| $U_{0}$ |  | (ships, hull resistance, water jets) Free stream velocity |  | m/s |
| $U_{10}$ | U10M | (environmental mechanics, wind) Reference mean wind speed at elevation 10 meters above sea surface | $U_{10}=(10 / z)^{1 / 7} U_{z}^{A}$ | m/s |
| $U_{\text {A }}$ | UA | (ships, propulsor performance) Axial velocity induced by propeller |  | m/s |
| $U_{\text {A }}$ | USHEAR | (environmental mechanics, wind) Wind shear velocity | $C_{10}{ }^{1 / 2} U_{10}$ or $0.71 U_{10}{ }^{1.23}$ | m/s |
| $U_{\text {AD }}$ | UADU | (ships, propulsor performance) Axial velocity induced by duct of ducted propeller |  | m/s |
| $U_{\text {AP }}$ | UAP | (ships, propulsor performance) Axial velocity induced by propeller of ducted propeller |  | m/s |
| $U_{\text {c }}$ | UC | (ships, manoeuvrability, turning circles) Speed in steady turn |  | m/s |
| $U_{\text {e }}$ | UE | (fluid mechanics, boundary layers) Velocity at the edge of the boundary layer at $y=\delta_{995}$ |  | m/s |
| $U_{\text {I }}$ | UNIN | (fluid mechanics, cavitation) Critical velocity | Free stream velocity at which cavitation inception takes place | m/s |
| $U_{i}$ | UIN | (fluid mechanics, boundary layers) Instantaneous velocity |  | m/s |
| $U_{\text {m }}$ | UMR | (fluid mechanics, boundary layers) Time mean of velocity in boundary layer |  | m/s |

Version 2021
$\mathbf{U}, \mathbf{u}$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Snit |


|  |  |  | Expanded uncertainty of out- <br> put estimate $y$ that defines an <br> interval $Y=y \pm U_{p}$ having a <br> high level of confidence $p$, <br> equal to coverage factor $k_{p}$ <br> times the combined standard <br> uncertainty $u_{c}(y)$ of $y: U_{p}=$ <br> $k_{p} u_{c}(y)$ |  |
| :--- | :--- | :--- | :--- | :--- |
| ciated to concertaintence level as $p$ |  |  |  |  |

ITTC Symbols
Version 2021
$\mathbf{U}, \mathbf{u}$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Sit |


| $u$ | UFL | (fluid mechanics, boundary layers) Velocity fluctuations in boundary layer |  | m/s |
| :---: | :---: | :---: | :---: | :---: |
| $u$ | UX, U | (ships, manoeuvrability) Surge velocity, linear velocity along body $x$ axis |  | m/s |
| $u$ | U | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $x$ |  | m/s |
| $u_{7 \varphi}$ | UJFI | (ships, hull resistance, water jets) Local tangential velocity at station 7 |  | $\mathrm{m} / \mathrm{s}$ |
| $u_{\mathrm{c}}^{2}(y)$ |  | (uncertainty) Combined variance | Combined variance associated with output estimate $y$ | 1 |
| $u_{c}(y)$ |  | (uncertainty) Combined standard uncertainty | Positive square root of $u_{\mathrm{c}}^{2}(y)$ | 1 |
| $u_{c}(y) / / y \mid$ |  | Relative combined standard uncertainty of output estimate $y$ |  |  |
| $u_{\text {cA }}(y)$ |  | (uncertainty) Combined standard uncertainty from Type A | From Type A evaluations alone | 1 |
| $u_{\text {cB }}(y)$ |  | (uncertainty) Combined standard uncertainty from Type B | From Type B evaluations alone | 1 |
| $u_{c}\left(y_{i}\right)$ |  | (uncertainty) Combined standard uncertainty | Combined standard uncertainty of output estimate $y_{i}$ when two or more measurands or output quantities are determined in the same measurement | 1 |
| $u_{i}, v_{i}$ | U(I), V(I) | (basic quantity) Any vector quantities |  |  |
| $u_{i} v_{i}$ | UVPS | (basic quantity) Scalar product | $u_{i} v_{i}$ |  |
| $u_{i} v_{j}$ | UVPD(I,J) | (basic quantity) Diadic product | $u_{i} v_{j}$ |  |
| uxv | UVPV(I) | (basic quantity) Vector product | $\varepsilon_{i j k} u_{j} v_{k}$ |  |
| ${ }_{1} u_{i}^{2}(y)$ |  | (uncertainty) Component of combined variance | $u_{i}^{2}(y) \equiv\left[c_{i} u\left(x_{i}\right)\right]^{2}$ | 1 |
| ${ }_{1} u_{i}(y)$ |  | (uncertainty) Component of combined standard uncertainty | $u_{i}(y) \equiv\left\|c_{i}\right\| u\left(x_{i}\right)$ | 1 |

ITTC Symbols
Version 2021
$\mathbf{U}, \mathbf{u}$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- |


| $u^{s}$ | UFLS | (fluid mechanics, boundary layers) Root mean square value of velocity fluctuations |  | m/s |
| :---: | :---: | :---: | :---: | :---: |
| $u^{2}\left(x_{i}\right)$ |  | (uncertainty) Estimated variance | Associated with input estimate $x_{i}$ that estimates input quantity $X_{i}$ | 1 |
| $u\left(X_{i}\right)$ |  | (uncertainty) Standard deviation | Positive square root of $u^{2}\left(x_{i}\right)$ | 1 |
| $u\left({ }_{i}, \chi_{j}\right)$ |  | (uncertainty) Estimated covariance |  | 1 |
| $u\left(x_{i}\right) /\left\|x_{i}\right\|$ |  | (uncertainty) Relative standard uncertainty |  | 1 |
| $\begin{aligned} & u\left(x_{i}, x_{j}\right) / \mid x_{i} \\ & x_{j} \mid \end{aligned}$ |  | Estimated relative covariance | Estimated relative covariance associated with input estimates $x_{i}$ and $x_{j}$ |  |
| $u_{z}, u_{z i}$ | UFLUCT | (environmental mechanics, wind) Turbulent wind fluctuations |  | m/s |
| $u_{\tau}$ | UTAU | (fluid mechanics, boundary layers) Shear (friction) velocity | $(\tau / \rho)^{1 / 2}$ | m/s |
| $\dot{u}$ | UR | (solid body mechanics, rigid body motions) Rates of change of components of linear velocity relative to body axes |  | $\mathrm{m} / \mathrm{s}^{2}$ |
| $\dot{u}$ | UXRT, UR | (ships, manoeuvrability) Surge acceleration, linear acceleration along body $x$-axis | $d u / d t$ | $\mathrm{m} / \mathrm{s}^{2}$ |
| $u^{+}$ | UPLUS | (fluid mechanics, boundary layers) | $U / u_{\tau}$ | 1 |
| $u \times v$ | UVPV(I) | (fundamental. coordinate and space related) Vector product | $\delta_{i j k} u_{j} v_{k}$ |  |
| $u^{*}$ | USHEAR | (environmental mechanics, wind) Wind shear velocity | $C_{10}{ }^{1 / 2} U_{10}$ or $0.71 U_{10}{ }^{1.23}$ | m/s |
| $\left[u\left(x_{i}\right) /\left[x_{i}\right]\right]^{2}$ |  | Estimated relative variance | Estimated relative variance associated with input estimate $x_{i}$ |  |
| $\left[u_{c}(y) /\|y\|\right]^{2}$ |  | Relative combined variance | Relative combined variance associated with output estimate $y$ |  |

## ITTC Symbols

Version 2021
V, v
ITTC

Symbol $\quad$\begin{tabular}{llll}
Computer <br>
Symbol

$\quad$ Name $\quad$

Definition or <br>
Explanation

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SI- <br>
Unit
\end{tabular}

| V | VA | (fluid mechanics, flow fields, sailing vessels) Velocity of a body | $V=v_{i} v_{i}{ }^{1 / 2}$ | m/s |
| :---: | :---: | :---: | :---: | :---: |
| V | VO | (ships, basic quantities) Volume |  | $\mathrm{m}^{3}$ |
| V | DISPVOL | (ships, hull geometry) Displacement volume | $\Delta /(\rho g)=\nabla_{\mathrm{BH}}+\nabla_{\mathrm{AP}}$ | $\mathrm{m}^{3}$ |
| $V$ | V | (ships, hull resistance, manoeuvrability, sailing vessels) Linear velocity of origin in body axis, Speed of the model or the ship |  | m/s |
| V |  | (seakeeping, large amplitude motions capsizing) Tank total capacity |  | $\mathrm{m}^{3}$ |
| $V^{0}$ | V0, OMN | (ships, basic quantities) Rotational velocity | $2 \pi n$ | rad/s |
| $V^{0}{ }_{i}$ | $V 0(\mathrm{I}), V(\mathrm{I})$ | (fundamental. coordinate and space related) Zeroth order moments of a vector quantity distributed in space, referred to an orthogonal system of Cartesian coordinates fixed in the body | $\int d v_{i}$ |  |
| $V_{0}$ | V0 | (ships, manoeuvrability) Approach speed |  | m/s |
| $V_{0}$ | V0 | (fluid mechanics, flow fields) Velocity of undisturbed flow |  | m/s |
| $V_{0}$ |  | (seakeeping, large amplitude motions capsizing) Speed of craft in the turn - <br> IMO/HSC'2000 <br> Service speed - IMO/IS |  | m/s |
| $V^{1}$ | V, V1 | (ships, basic quantities) Linear or translatory velocity of a body | $d s / d t$ | m/s |
| $V^{1}{ }_{i}$ | V1(I) | (fundamental. coordinate and space related) First order moments of a vector distribution | $\iint_{\varepsilon i j k} \chi_{j} d v_{k}$ |  |
| $V_{\text {A }}$ | VA | $\begin{aligned} & \text { (ships, manoeuvrability) Ap- } \\ & \text { proach speed } \end{aligned}$ |  | m/s |
| $V_{\text {A }}$ | VA | (ships, performance, propulsor performance) Advance speed of propeller | Equivalent propeller open water speed based on thrust or torque identity | m/s |

ITTC Symbols
Version 2021
V, v

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Sir |


| $V_{\text {BM }}$ | VBM | (planing, semi-displacement vessels) Mean bottom velocity | Mean velocity over bottom of the hull | m/s |
| :---: | :---: | :---: | :---: | :---: |
| $V_{F}$ | VF | (ships, manoeuvrability) <br> Flow or current velocity |  | m/s |
| $V_{\text {I }}$ | VI | (fluid mechanics, lifting surfaces) Induced velocity |  | m/s |
| $V_{i}$ | V(I) | (ships, unsteady propeller forces) Velocity field of the wake | $i=1,2,3$ | m/s |
| $V_{i}$ | V0(I), V(I) | (fundamental. coordinate and space related) Zeroth order moments of a vector quantity distributed in space, referred to an orthogonal system of Cartesian coordinates fixed in the body | $\int d v_{i}$ |  |
| $V_{\mathrm{K}}$ | VKN | (ships, hull resistance) Speed in knots |  |  |
| $V_{\mathrm{L}}$ | VOLS | (fluid mechanics, cavitation) Volume loss | $W_{\mathrm{L}} / \mathrm{w}$ | $\mathrm{m}^{3}$ |
| $V_{\text {mc }}$ | VMC | (sailing vessels) Velocity made good on course |  | m/s |
| $V_{\mathrm{mg}}$ | VMG | (sailing vessels) Velocity made good to windward (contrary to wind direction) |  | m/s |
| $V_{\mathrm{P}}$ | VP | (ships, propulsor performance) Mean axial velocity at propeller plane of ducted propeller |  | m/s |
| $V_{\text {ref }}$ | VREF | (ships, ship performance) Design ship speed when the ship is in operation in a calm sea condition (no wind and waves) |  | m/s |
| $V_{\text {s }}$ | VS | (ships, propulsor performance) Section advance speed at $0.7 R$ | $\left(V_{\mathrm{A}}{ }^{2}+(0.7 R \omega)^{2}\right)^{1 / 2}$ | m/s |
| $V_{\text {SP }}$ | VSP | (planing, semi-displacement vessels) Spray velocity | Relative velocity between hull and spray in direction of the spray | m/s |
| $V_{T}$ | VT | (fluid mechanics, lifting surfaces) Resultant velocity of flow approaching a hydrofoil | Taking vortex induced velocities into account | m/s |
| $V_{\text {tw }}$ | VWABS | (sailing vessels) True wind velocity |  | m/s |

## ITTC Symbols

Version 2021
V, v
ITTC

Symbol $\quad$\begin{tabular}{llll}
Computer <br>
Symbol

$\quad$ Name $\quad$

Definition or <br>
Explanation

$\quad$

SI- <br>
Unit
\end{tabular}

| $V_{\mathrm{u}}$ | V(URT) | (ships, manoeuvrability) Generalized velocity |  | m/s |
| :---: | :---: | :---: | :---: | :---: |
| $\dot{V}_{\mathrm{u}}$ | V(URT) | (ships, manoeuvrability) Generalized acceleration |  | $\mathrm{m} / \mathrm{s}^{2}$ |
| $V_{\mathrm{u}}$ | $V(\mathrm{U})$ | (fundamental. coordinate and space related) Generalized vector | $\begin{aligned} & V_{i}=V_{i} \\ & V_{3+i}=V_{i} \end{aligned}$ |  |
| $V_{w}$ | VW | (ships, ship performance) Design ship speed when the ship is in operation under the representative sea condition |  | m/s |
| $V_{\text {WR }}$ | VWREL | (ships, hull resistance, manoeuvrability, environmental mechanics, wind, sailing vessels) <br> Relative wind velocity, apparent wind velocity |  | m/s |
| $V_{\text {WT }}$ | VWABS | (ships, manoeuvrability, environmental mechanics, wind) True wind velocity |  | m/s |
| $v$ | UY, V | (ships, manoeuvrability) Sway velocity, linear velocity along body $y$-axis |  | m/s |
| $v$ | V | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis y |  | m/s |
| $v$ |  | (seakeeping, large amplitude motions capsizing) Tank total capacity |  | $\mathrm{m}^{3}$ |
| v | V | (fluid mechanics, flow fields) Velocity component in direction of $y$ axis |  | m/s |
| $v^{0}{ }_{1}$ | $\begin{aligned} & \text { P, OMX, } \\ & \text { V0(1), V(4) } \end{aligned}$ | (solid body mechanics, rigid body motions) Rotational velocity around body axis $x$ |  | rad/s |
| $v^{0}{ }_{2}$ | $\begin{aligned} & \text { Q, OMY, } \\ & \text { V0(2), V(5) } \end{aligned}$ | (solid body mechanics, rigid body motions) Rotational velocity around body axis $y$ |  | rad/s |
| $v^{0} 3$ | $\begin{aligned} & \text { R, OMZ, } \\ & \text { V0(3), V(6) } \end{aligned}$ | (solid body mechanics, rigid body motions) Rotational velocity around body axis z |  | rad/s |

ITTC Symbols
Version 2021
V, v

| ITTC | Computer |  |  |  |
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| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Sir |


| $v^{1}{ }_{1}$ | $\begin{aligned} & \mathrm{U}, \mathrm{VX}, \\ & \mathrm{~V} 1(1), \mathrm{V}(1) \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $x$ |  | m/s |
| :---: | :---: | :---: | :---: | :---: |
| $v^{1}{ }_{2}$ | $\begin{aligned} & \mathrm{V}, \mathrm{VY}, \\ & \mathrm{~V} 1(2), \mathrm{V}(2) \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $y$ |  | m/s |
| $v^{1}{ }_{3}$ | $\begin{aligned} & \text { W, VZ, } \\ & \text { V1(3), V(3) } \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis z |  | m/s |
| $V_{1}$ | $\begin{aligned} & \mathrm{U}, \mathrm{VX}, \\ & \mathrm{~V} 1(1), \mathrm{V}(1) \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $x$ |  | m/s |
| $v_{1}$ | VX, V1 | (fluid mechanics, flow fields) Velocity component in direction of $x, y, z$ axes |  | m/s |
| $v_{2}$ | V1(2), V(2) | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $y$ |  | m/s |
| $v_{2}$ | VY, V2 | (fluid mechanics, flow fields) Velocity component in direction of $x, y, z$ axes |  | m/s |
| $v_{3}$ | V1(3), V(3) | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis z |  | m/s |
| V3 | VZ, V3 | (fluid mechanics, flow fields) (fluid mechanics, flow fields) Velocity component in direction of $x, y, z$ axes |  | m/s |
| $V_{4}$ | V0(1), V(4) | (solid body mechanics, rigid body motions) Rotational velocity around body axis $x$ |  | rad/s |
| $v_{5}$ | $\begin{aligned} & \text { Q, OMY, } \\ & \text { V0(2), V(5) } \end{aligned}$ | (solid body mechanics, rigid body motions) Rotational velocity around body axis $y$ |  | rad/s |
| V6 | $\begin{aligned} & \text { R, OMZ, } \\ & \text { V0(3), V(6) } \end{aligned}$ | (solid body mechanics, rigid body motions) Rotational velocity around body axis z |  | rad/s |
| $v_{\text {A }}$ | POAI | (environmental mechanics, ice) Relative volume of air | Volume of gas pores per unit volume of ice | 1 |

## ITTC Symbols

Version 2021
V, v

| ITTC | Computer Symbol | Name | Definition or | SI- |
| :---: | :---: | :---: | :---: | :---: |
| Symbol | Symbol | Name | Explanation | Unit |


| $V_{B}$ | POBR | (environmental mechanics, ice) Relative volume of brine | Volume of liquid phase per unit volume of ice | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $V_{0}$ | POIC | (environmental mechanics, ice) Total porosity of ice | $v_{0}=v_{\mathrm{A}}+v_{\mathrm{B}}$ | 1 |
| $v_{i}$ | V(I) | (fluid mechanics, flow fields) Velocity |  | m/s |
| $v_{u}$ | V(U) | (solid body mechanics, rigid body motions) Components of generalized velocity or motion relative to body axes | $\begin{aligned} & v_{i}=v_{i}^{1} \\ & v_{3+i}=v^{0} \end{aligned}$ | m/s <br> rad/s |
| $v_{y}$ | VY, V2 | (fluid mechanics, flow fields) Velocity component in direction of $x, y, z$ axes |  | m/s |
| $V_{\text {w }}$ |  | (seakeeping, large amplitude motions capsizing) Wind speed used in calculation |  | m/s |
| $v_{x}$ | VX, | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $x$ |  | m/s |
| $v_{y}$ | $\begin{aligned} & \text { V, VY, } \\ & \text { V1(2), V(2) } \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis $y$ |  | m/s |
| $v_{z}$ | $\begin{aligned} & \text { W, VZ, } \\ & \text { V1(3), V(3) } \end{aligned}$ | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis z |  | m/s |
| uxv | UVPV(I) | (fundamental. coordinate and space related) Vector product | $\varepsilon_{i j k} u_{j} v_{k}$ |  |
| $\dot{v}$ | VR | (solid body mechanics, rigid body motions) Rates of change of components of linear velocity relative to body axes |  | $\mathrm{m} / \mathrm{s}^{2}$ |
| $\dot{v}$ | UYRT, VR | (ships, manoeuvrability) Sway acceleration, linear acceleration along body $y$-axis | $d v / d t$ | $\mathrm{m} / \mathrm{s}^{2}$ |

ITTC Symbols
Version 2021
W, w
ITTC
Symbo
Computer
Symbol
Name
Definition or
SI-
Explanation
Unit

| W | WT | (ships, basic quantities) Weight (force), gravity force acting on a body |  | N |
| :---: | :---: | :---: | :---: | :---: |
| W | SHIPWT | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Ship weight | $m g$ | N |
| We | WN | (fluid mechanics, flow parameter) Weber number | $V^{2} L / \kappa$ | 1 |
| $W_{\text {F }}$ | WTF | (hydrofoil boats) Weight of foil |  | N |
| $W_{\text {L }}$ | WTLS | (fluid mechanics, cavitation) Weight loss | Weight of material eroded from a specimen during a specified time | N/s |
| w | WD | (ships, basic quantities, fluid mechanics, flow parameter) Weight density, formerly specific weight | $d W / d V=\rho g$ | $\mathrm{N} / \mathrm{m}^{3}$ |
| w | WPUL | (solid body mechanics, loads) Weight per unit length | $d W / d x_{1}$ | $\mathrm{N} / \mathrm{m}$ |
| w | W | (solid body mechanics, rigid body motions) Translatory velocity in the direction of body axis z |  | m/s |
| w | W | (fluid mechanics, flow fields) Velocity component in direction of $z$ axis |  | m/s |
| w | WFT | (ships, performance) Taylor wake fraction in general | $\left(V-V_{\mathrm{A}}\right) / V$ | 1 |
| w | UZ, W | (ships, manoeuvrability) Heave velocity, linear velocity along body $z$-axis |  | m/s |
| w | VZ, V3 | (fluid mechanics, flow fields) Velocity component in direction of $x, y, z$ axes |  | m/s |
| $w_{1}$ |  | (ships, hull resistance, water jets) Geometric intake width at station 1 |  | m |
| $W_{1 \mathrm{~A}}$ |  | (ships, hull resistance, water jets) Width of capture area measured over hull surface at station 1A |  | m |
| $W_{\text {F }}$ | WFF | (ships, performance) Froude wake fraction | $\left(V-V_{\mathrm{A}}\right) / V_{\mathrm{A}}$ | 1 |

## ITTC Symbols

Version 2021
W, w

| ITTC |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |$\quad$| Computer |
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| Symbol |$\quad$ Name $\quad$| Definition or |
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| Explanation |


| $w_{Q}$ | WFTQ | (ships, ship performance) <br> Torque wake fraction | Propeller speed $V_{\mathrm{A}}$ deter- <br> mined from torque identity | 1 |
| :--- | :--- | :--- | :--- | :--- |
| $w_{\mathrm{R}}$ |  | (ships, ship performance) <br> Effect of the rudder(s) on the <br> wake fraction | 1 |  |
| $w_{T}$ | WFTT | (ships, performance) Thrust <br> wake fraction | Propeller speed, $V_{\mathrm{A}}$, deter- <br> mined from thrust identity | 1 |
| $\dot{w}$ | UZRT, WR | (solid body mechanics, rigid <br> body motions, ships, ma- <br> noeuvrability) Heave accel- <br> eration, linear acceleration <br> along body z-axis | $d w / d t$ | $\mathrm{~m} / \mathrm{s}^{2}$ |

ITTC Symbols
Version 2021
X, x


| $X$ |  | (fundamental, time and frequency domain quantity) <br> Real "valued" function |  |  |
| :---: | :---: | :---: | :---: | :---: |
| X | X | (solid body mechanics, loads) Force in direction of body axis $x$ |  | N |
| $X$ | X | (ships, unsteady propeller forces) Cylindrical coordinates | Cylindrical system with origin O and longitudinal $x$ axis as defined before; angular a-(attitude)-coordinate, zero at 12 o'clock position, positive clockwise looking forward, $r$ distance measured from the $x$-axis | m |
| X | FX | (ships, manoeuvrability, seakeeping) Surge force on body, force along body $x$ axis |  | N |
| X |  | (sailing vessels) Components of resultant force along designated axis |  | N |
| $X_{1}$ |  | (seakeeping, large amplitude motions capsizing) Roll damping coefficients |  | 1 |
| $X_{2}$ |  | (seakeeping, large amplitude motions capsizing) Roll damping coefficients |  | 1 |
| $\chi_{\text {Св }}$ | XCB | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of buoyancy (Lcb) | Longitudinal distance from reference point to the centre of buoyancy, B such as X MCF from Midships | m |
| $X_{\text {CF }}$ | XCF | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of flotation ( $\mathrm{L}_{\mathrm{Cf}}$ ) | Longitudinal distance from reference point to the centre of flotation, F such as $\mathrm{X}_{\mathrm{MCF}}$ from Midships | m |
| $X_{\text {CG }}$ | XCG | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of gravity (LCG) | Longitudinal distance from a reference point to the centre of gravity, $G$ such as $X_{M C G}$ from Midships | m |
| $X_{\text {F }}$ | FDIM | (environmental mechanics, wind) Dimensionless Fetch | $g F / U_{19}{ }^{2}$ |  |

ITTC Symbols
Version 2021
X, x

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
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| Explanation |$\quad$| SI- |
| :--- |


| $X_{H}$ | XH | (ACV and SES) Horizontal spacing between inner and outer side skirt hinges or attachment points to structure | needs clarification | m |
| :---: | :---: | :---: | :---: | :---: |
| $X_{\text {R }}$ | XRU | (ships, manoeuvrability, seakeeping) Longitudinal rudder force |  | N |
| $X_{\text {s }}$ | XS | (ACV and SES) Distance of leading skirt contact point out-board or outer hinge of attachment point to structure | needs clarification | m |
| $X_{i}$ |  | $i^{\text {th }}$ input quantity | $i^{\text {th }}$ input quantity on which measurand $Y$ depends NOTE Xi may be the physical quantity or the random variable |  |
| $X_{i, k}$ |  | $k^{\text {th }}$ independent repeated observation of $X_{i}$ |  |  |
| $X_{u}$ | XU | (ships, manoeuvrability, seakeeping) Derivative of surge force with respect to surge velocity | $\partial X / \partial u$ | Ns/m |
| $X_{\text {u }}$ | XURT | (ships, manoeuvrability, seakeeping) Derivative of surge force with respect to surge acceleration | $\partial X / \partial \dot{u}$ | Ns ${ }^{2} / \mathrm{m}$ |
| $\overline{X_{i}}$ |  | Estimate of the value of input quantity $X_{i}$ | Estimate of the value of input quantity $X_{i}$ equal to the arithmetic mean or average of $n$ independent repeated observation $X_{i, k}$ of $X_{i}$ |  |
| $x$ | X | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| $x$ | X, Y | (fundamental, statistical, stochastic) Stationary stochastic process | $x(\zeta, t), y(\zeta, t)$ |  |
| $x$ | $x$ | (fundamental, time and frequency domain quantity) Values of real quantities | $x(t)$ |  |
| $x$ | XLO | (ships, performance) Load fraction in power prediction | $\eta_{\mathrm{D}} P_{\mathrm{D}} / P_{\mathrm{E}}-1$ | 1 |

ITTC Symbols
Version 2021
X, x


| $x$ | X | (ships, unsteady propeller forces) Cylindrical coordinates | Cylindrical system with origin $O$ and longitudinal $x$ axis as defined before; angular a-(attitude)-coordinate, zero at 12 o'clock position, positive clockwise looking forward, $r$ distance measured from the $x$-axis | m |
| :---: | :---: | :---: | :---: | :---: |
| $x$ | X | (ships, unsteady propeller forces) Cartesian coordinates | Origin O coinciding with the centre of the propeller. The longitudinal $x$-axis coincides with the shaft axis, positive forward; the trans-verse $y$ axis, positive to port; the third, $z$-axis, positive upward | m |
| $x$ | X, Y | (fundamental, statistical) Random quantities | $x(\zeta), y(\zeta)$ |  |
| $x_{0}$ | X0 | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space | m |
| $\chi_{01}$ | X0(1) | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space | m |
| $\chi_{02}$ | X0(2) | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space | m |
| $\chi_{03}$ | X0(3) | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space | m |
| X090 | X090 | (ships, manoeuvrability, turning circles) Advance at $90^{\circ}$ change of heading |  | m |
| $\chi_{0180}$ | X0180 | (ships, manoeuvrability, turning circles) Advance at $180^{\circ}$ change of heading |  | m |
| $\chi_{0}$ | X0F | (ships, manoeuvrability, stopping man.) Head reach |  | m |
| $\chi_{0 \text { max }}$ | XMX | (ships, manoeuvrability, turning circles) Maximum advance |  | m |

ITTC Symbols
Version 2021
$\mathbf{X}, \mathrm{x}$


| $X_{1}$ | X(1) | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| :---: | :---: | :---: | :---: | :---: |
| $x_{2}$ | X(2) | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| $x_{3}$ | X(3) | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| $x^{\text {A }}$ | XA | (fundamental, time and frequency domain quantity) Analytic function | $X^{\mathrm{A}}(t)=X(t)+i X^{\mathrm{H}}(t)$ |  |
| $x^{\text {A }}$ | XMS | (fundamental, statistical) Average or sample mean of a random quantity | $1 / n \sum x_{i}, i=1 \ldots n$ <br> unbiased random estimate of the expectation with $\begin{aligned} & x^{\mathrm{AE}}=x^{E} \\ & x^{\mathrm{VSE}}=x^{V} / n \end{aligned}$ |  |
| $\chi_{\text {B }}$ | XBDR | (ships, propulsor geometry) Boss to diameter ratio | $d_{\mathrm{h}} / D$ |  |
| ХСВ | ХАСВ | (ships, hydrostatics, seakeeping, large amplitude motions capsizing) Longitudinal centre of floatation of added buoyant layer | Longitudinal distance from reference point to the centre of the added buoyant layer, $b$ such as $X_{M C}$ from Midships | m |
| $\chi_{\text {CF }}$ | XACF | (ships, hydrostatics, seakeeping, large amplitude motions capsizing) Longitudinal centre of flotation of added buoyant layer | Longitudinal distance from reference point to the centre of flotation of the added buoyant layer, $f$ such as $\mathrm{X}_{\text {MCf }}$ from Midships | m |
| $\chi_{\text {CG }}$ | XACG | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Longitudinal centre of gravity of added weight (mass) | Longitudinal distance from reference to the centre of gravity, $g$, of an added or removed weight (mass) such as $\mathrm{x}_{\mathrm{MCg}}$ from Midships | m |
| $x^{\text {D }}$ | XDR | (fundamental, statistical) Standard deviation of a random quantity | $x^{\mathrm{VR} 1 / 2}$ |  |
| $x_{\text {D }}$ |  | (seakeeping, large amplitude motions capsizing) Distance of down flooding opening from end of boat |  | m |

ITTC Symbols
Version 2021
X, x

| ITTC | Computer |
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| Symbol | Symbol |


| $x^{\text {DF }}$ | XDF | (fundamental, time and frequency domain quantity) Fourier transform of ampled function | $X^{\mathrm{DF}}(f)=\Sigma x_{j} \exp \left(-i 2 \pi f j T_{s}\right)$ <br> i.e. periodically repeating= $X(0) / 2+f_{\mathrm{s}} \Sigma X^{F}\left(f+j f_{\mathrm{s}}\right)$ sample theorem: aliasing! |  |
| :---: | :---: | :---: | :---: | :---: |
| $x^{\text {DL }}$ | XDL | (fundamental, time and frequency domain quantity) Laurent transform Sampled function | $X^{\mathrm{DL}}(\mathrm{s})=\Sigma x_{j} \exp \left(-s j T_{\mathrm{s}}\right)$ |  |
| $x^{D R}$ | XDR | (fundamental, statistical) Standard deviation of a random quantity | $x^{\mathrm{VR} 1 / 2}$ |  |
| $x^{\text {DS }}$ | XDS | (fundamental, statistical) Sample deviation of a random quantity | $x^{V S^{1 / 2}}$, <br> unbiased random estimate of the standard deviation |  |
| $\chi^{E}$ | XMR | (fundamental, statistical) Expectation or population mean of a random quantity | $E(x)$ |  |
| $X_{F}$ | XF | (fundamental. coordinate and space related) Flow axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the flow | m |
| $x^{\mathrm{F}}$ | XFT | (fundamental, time and frequency domain quantity) Fourier transform | $X^{\mathrm{F}}(f)=\int X(t) \exp (-i 2 \pi f t) d t$ <br> inverse form: <br> $=\int X^{\mathrm{F}}(f) \exp (-i 2 \pi f t) d t$ <br> if $X(t)=0$ and $\mathrm{a}=0$ then $X^{\mathrm{F}}(f)=X^{\mathrm{L}}(f)$ |  |
| $\chi_{\text {F1 }}$ | XF(1) | (fundamental. coordinate and space related) Flow axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the flow | m |
| $X_{\text {F2 }}$ | XF(2) | (fundamental. coordinate and space related) Flow axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the flow | m |
| $X_{\text {F3 }}$ | XF(3) | (fundamental. coordinate and space related) Flow axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the flow | m |
| $\chi^{\mathrm{F}}{ }_{j}$ | XFT(J) | (fundamental, time and frequency domain quantity) Fourier transform of periodic function | $\begin{aligned} & 1 / T_{\mathrm{C}} \int X(t) \exp \left(-i 2 \pi j t / T_{\mathrm{C}}\right) d t \\ & t=0 . . T_{\mathrm{C}} \\ & X^{\mathrm{F}}=\Sigma x^{\mathrm{F}} \delta \delta\left(f-j / T_{C}\right) \end{aligned}$ <br> inverse form: $X(t)=\Sigma x^{\mathrm{F}} \operatorname{jexp}\left(-i 2 \pi f j T_{\mathrm{C}}\right)$ |  |

## ITTC Symbols

Version 2021
$\mathbf{X}, \mathrm{x}$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |$\quad$| SI- |
| :--- |


| $x^{\mathrm{H}}$ | XHT | (fundamental, time and frequency domain quantity) Hilbert transform | $X^{\mathrm{H}}(t)=1 / \pi \int X(\tau) /(t-\tau) d \tau$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $x^{\mathrm{HF}}$ | XHF | (fundamental, time and frequency domain quantity) Fourier transform of Hilbert transform | $\begin{aligned} & X^{\mathrm{HF}}(f)=X^{\mathrm{F}}(f)(-i \operatorname{sgn} f) \\ & (1 / t)^{F}=-i \operatorname{sgn} f \end{aligned}$ |  |
| $x_{i}$ | $X(\mathrm{I}), Y(\mathrm{I})$ | (fundamental, statistical) Samples of random quantities | $\begin{aligned} & i=1 \ldots n \\ & \quad n: \text { sample size } \end{aligned}$ |  |
| $x_{i}$ | X(I) | (ships, seakeeping) Absolute displacement of the ship at the reference point | $i=1,2,3$ :surge, sway, and heave respectively | m |
| $x_{i}$ |  | Estimate of input quantity $X_{i}$ | Estimate of input quantity $X_{i}$ NOTE when $x_{i}$ is determined from the arithmetic mean or average of $n$ independent repeated observation $x_{i}=\overline{X_{i}}$ $x_{i}=\bar{X}_{i}$ |  |
| $\chi_{j}$ | $X(\mathrm{~J})$ | (fundamental, time and frequency domain quantity) Variables for samples values of real quantities | $x\left(t_{j}\right)=\int_{x}(t) \delta\left(t-t_{j}\right) d t$ |  |
| $\chi^{\text {L }}$ | XLT | (fundamental, time and frequency domain quantity) Laplace transform | $\begin{aligned} & X^{\mathrm{L}}(s)=\int X(t) \exp (-s t) d t \\ & \text { if } X(t<0)=0 \text { then } \\ & =(X(t) \exp (-a t))^{F} \end{aligned}$ |  |
| $x^{\text {M }}$ | XMR | (fundamental, statistical) Expectation or population mean of a random quantity | $E(x)$ |  |
| $\left(x^{m}\right)^{E}$ | XmMR | (fundamental, statistical) mth moment of a random quantity | $\left(x^{m}\right)^{E}$ |  |
| $x^{\text {MR }}$ | XMR | (fundamental, statistical) Expectation or population mean of a random quantity | $E(x)$ |  |
| $\chi^{\text {MS }}$ | XMS | (fundamental, statistical) Average or sample mean of a random quantity | $1 / n \sum x_{i}, i=1 \ldots n$ <br> unbiased random estimate of the expectation with $\begin{aligned} & x^{A E}=x^{E} \\ & x^{V S E}=x^{V} / n \end{aligned}$ |  |

## ITTC Symbols

Version 2021
X, X


| $x^{\text {PD }}$ | XPD | (fundamental, statistical) Probability density of a random quantity | $d F_{x} / d x$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $x^{\mathrm{PF}}$ | XPF | (fundamental, statistical) Probability function (distribution) of a random quantity |  | 1 |
| $X_{P}$ | XP | (ships, propulsor geometry) Longitudinal propeller position | Distance of propeller centre forward of the after perpendicular | m |
| $x^{R}$ | XRT | (fundamental, time and frequency domain quantity) Laurent transform | $X^{\mathrm{R}}(r)=\Sigma x_{j} r^{-j}=X^{\mathrm{DL}}$ |  |
| $\chi_{\text {R }}$ | XRU | (ships, manoeuvrability) <br> Longitudinal position of rudder axis |  | m |
| $x^{\text {S }}$ | XS | (fundamental, time and frequency domain quantity) Single-sided complex spectra | $\begin{aligned} & X^{\mathrm{S}}(f)=X^{\mathrm{F}}(f)(1+\operatorname{sgn} f) \\ & =X^{\mathrm{AF}} \\ & \text { i.e. }=0 \text { for } f<0 \end{aligned}$ |  |
| $x^{\text {S }}{ }^{\text {b }}$ | XS(J) | (fundamental, time and frequency domain quantity) Single-sided complex Fourier series | $X^{\mathrm{F}}{ }_{j}(1+\operatorname{sgn} j)$ <br> line spectra |  |
| $x_{u}$ | X(U) | (ships, seakeeping) Generalized displacement of a ship at the reference point | $u=1 . . .6$ surge, sway, heave, roll, pitch, yaw | $\begin{aligned} & \mathrm{m} \\ & \mathrm{rad} \end{aligned}$ |
| $x^{V}$ | XVR, XXVR | (fundamental, statistical) Variance of a random quantity | $x^{2 E}-x^{E 2}$ |  |
| $x^{V \mathrm{R}}$ | XVR, XXVR | (fundamental, statistical) Variance of a random quantity | $x^{2 E}-x^{E 2}$ |  |
| $x^{V S}$ | $X \mathrm{VS}, \mathrm{XXVS}$ | (fundamental, statistical) Sample variance of a random quantity | $\begin{aligned} & 1 /(n-1) \sum\left(x_{i}-x^{\mathrm{A}}\right)^{2} \\ & i=1 \ldots . . n \end{aligned}$ <br> unbiased random estimate of the variance $\quad x^{V S E}=x^{V}$ |  |
| $x x^{\mathrm{C}}$ | XXCR | (fundamental, statistical, stochastic) Auto-covariance of a stationary stochastic process | $\left(x(t)-x^{E}\right)\left(x(t+\tau)-x^{E}\right)^{E}$ |  |
| $x x^{\text {CR }}$ | XXCR | (fundamental, statistical, stochastic) Auto-covariance of a stationary stochastic process | $\left(x(t)-x^{E}\right)\left(x(t+\tau)-x^{E}\right)^{E}$ |  |

## ITTC Symbols

Version 2021

| ITTC | Computer |
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| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
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| Explanation |


| $x x^{\text {MR }}$ | XXMR | (fundamental, statistical) Auto-correlation of a random quantity | $x \chi^{E}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $x x^{\mathrm{R}}$ | XXMR | (fundamental, statistical) Auto-correlation of a random quantity | $x \chi^{E}$ |  |
| $x x^{\mathrm{RR}}$ | XXRR | (fundamental, statistical, stochastic) Auto-correlation of a stationary stochastic process | $\begin{aligned} & x(t) x(t+\tau)^{E}=R_{x x}(\tau) \\ & R_{x x}(\tau)=R_{x x}(-\tau) \\ & \text { if } x \text { is ergodic: } \\ & R_{x x}(\tau)=x(t) x(t+\tau)^{M R} \\ & R_{x x}(\tau)=\int S_{x x}(\omega) \cos (\omega \tau) d \tau \\ & \tau=0 \ldots \infty \end{aligned}$ |  |
| $x x^{5}$ | XXSR | (fundamental, statistical, stochastic) Power spectrum or autospectral power density of a stochastic process | $x x^{R R S R}$ |  |
| $x x^{\text {VR }}$ | XVR, XXVR | (fundamental, statistical) Variance of a random quantity | $x^{2 E}-x^{E 2}$ |  |
| $x x^{\text {VS }}$ | $X \mathrm{VS}, \mathrm{XXVS}$ | (fundamental, statistical) Sample variance of a random quantity | $\begin{aligned} & 1 /(n-1) \sum\left(x_{i}-x^{A}\right)^{2} \\ & i=1 \ldots n \end{aligned}$ <br> unbiased random estimate of the variance $\quad x^{V S E}=x^{V}$ |  |
| $x y^{\text {C }}$ | XYCR | (fundamental, statistical, stochastic) Cross-covariance of two stationary stochastic processes | $\left(x(t)-x^{E}\right)\left(y(t+\tau)-y^{E}\right)^{E}$ |  |
| $x y^{\text {CR }}$ | XYCR | (fundamental, statistical, stochastic) Cross-covariance of two stationary stochastic processes | $\left(x(t)-x^{E}\right)\left(y(t+\tau)-y^{E}\right)^{E}$ |  |
| $x y^{\text {MR }}$ | XYMR | (fundamental, statistical) Cross-correlation of two random quantities | $x y^{E}$ |  |
| $x y^{\text {PD }}$ | XYPD | (fundamental, statistical) Joint probability density of two random quantities | $\partial^{2} F_{x y} /(\partial x \partial y)$ |  |
| $x y^{\text {PF }}$ | XYPF | (fundamental, statistical) Joint probability function (distribution) function of two random quantities |  | 1 |
| $x y^{\text {R }}$ | XYMR | (fundamental, statistical) Cross-correlation of two random quantities | $x y^{E}$ |  |

## ITTC Symbols

Version 2021
X, x

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |$\quad$| SI- |
| :--- |
| Unit |


| $x y^{\mathrm{R}}$ | $X Y R R$ | (fundamental, statistical, <br> stochastic) Cross-correlation <br> of two stationary stochastic <br> processes | $x(t) y(t+\tau)^{E}=R_{x y}(\tau)$ <br> $R_{y x}(\tau)=R_{x y}(-\tau)$ <br> if $x, y$ are ergodic: <br> $R_{x y}(\tau)=x(t) y(t+\tau)^{\mathrm{MR}}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $x y^{\mathrm{S}}$ | $X Y \mathrm{SR}$ | (fundamental, statistical, <br> stochastic) Cross-power <br> spectrum of two stationary <br> stochastic processes | $x y^{R R S R}$ |  |
| $x y^{V}$ | $X Y V R$ | (fundamental, statistical) <br> Variance of two random <br> quantities | $x y^{E}-x^{E} y^{E}$ |  |
| $x y^{V R}$ | $X Y V R$ | (fundamental, statistical) <br> Variance of two random <br> quantities | $x y^{E}-x^{E} y^{E}$ |  |

ITTC Symbols
Version 2021
$\mathbf{Y}, \mathrm{y}$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Name | Definition or <br> Symbol | SI- <br> Explanation |
| :--- | :--- | :--- |


| $Y$ | FY | (solid body mechanics, loads, ships, manoeuvrability, seakeeping) Sway force, force in direction of body axis y |  | N |
| :---: | :---: | :---: | :---: | :---: |
| Y |  | (sailing vessels) Components of resultant force along designated axis |  | N |
| Y |  | A measurand. Estimated relative uncertainty of standard uncertainty $u\left(x_{i}\right)$ of inputs estimate $x_{i}$ |  |  |
| $Y_{\text {CG }}$ | YCG | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Lateral displacement of centre of gravity ( $\mathrm{Y}_{\mathrm{CG}}$ ) | Lateral distance from a reference point to the centre of gravity, G | m |
| $Y_{r}$ | YR | (ships, manoeuvrability, seakeeping) Derivative of sway force with respect to yaw velocity | $\partial Y / \partial r$ | Ns |
| $Y_{\text {R }}$ | YRU | (ships, manoeuvrability, seakeeping) Transverse rudder force |  | N |
| $Y_{U}$ | YU | (ships, propulsor performance) Pod unit side force |  | N |
| $Y_{\dot{r}}$ | YRRT | (ships, manoeuvrability, seakeeping) Derivative of sway force with respect to yaw acceleration | $\partial Y / \partial \dot{r}$ | Ns ${ }^{2}$ |
| $Y_{v}$ | YV | (ships, manoeuvrability, seakeeping) Derivative of sway force with respect to sway velocity | O / 2 | Ns/m |
| $Y_{i}$ | YVRT | (ships, manoeuvrability, seakeeping) Derivative of sway force with respect to sway acceleration | $\partial Y / \partial \dot{\nu}$ | Ns ${ }^{2} / \mathrm{m}$ |
| $Y_{z}(\omega)$ |  | (ships, seakeeping) Amplitude of frequency response function for translatory motions | $\begin{aligned} & z_{a}(\omega) / \zeta_{a}(\omega) \text { or } \\ & z_{a}(\omega) / \eta_{a}(\omega) \end{aligned}$ | 1 |
| $Y_{\delta}$ | YD | (ships, manoeuvrability, seakeeping) Derivative of sway force with respect to rudder angle | $\partial Y / \delta$ | N |

ITTC Symbols
Version 2021
$\mathbf{Y}, \mathbf{y}$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Name | Definition or <br> Symbol | SI- |  |
| :--- | :--- | :--- | :--- |


| $Y_{\theta j}(\omega)$ |  | (ships, seakeeping) Amplitude of frequency response function for rotary motions | $\begin{aligned} & \Theta_{a}(\omega) / \zeta_{a}(\omega) \text { or } \\ & \Theta_{a}(\omega) /\left(\omega^{2} /\left(g \zeta_{a}(\omega)\right)\right) \end{aligned}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| y | X, Y | (fundamental, statistical, stochastic) Stationary stochastic process | $x(\zeta, t), y(\zeta, t)$ |  |
| y | X, Y | (fundamental, statistical) Random quantities | $x(\zeta), y(\zeta)$ |  |
| y | Y | (ships, unsteady propeller forces) Cartesian coordinates | Origin O coinciding with the centre of the propeller. The longitudinal $x$-axis coincides with the shaft axis, positive forward; the trans-verse $y$ axis, positive to port; the third, $z$-axis, positive upward | m |
| y | $\begin{aligned} & \mathrm{X}, \mathrm{X}(1) \\ & \mathrm{Y}, \mathrm{X}(2) \\ & \mathrm{Z}, \mathrm{X}(3) \end{aligned}$ | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| y |  | Estimated of measurand $Y$ or Result of a measurement or Output estimate |  |  |
| $y_{0}$ | $\begin{array}{\|l} \mathrm{X0}, \mathrm{X0}(1) \\ \mathrm{Y0}, \mathrm{X}(2) \\ \mathrm{ZO}, \mathrm{X0}(3) \\ \hline \end{array}$ | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space | m |
| $y_{090}$ | Y090 | (ships, manoeuvrability, turning circles) Transfer at $90^{\circ}$ change of heading |  | m |
| $y_{0180}$ | Y0180 | (ships, manoeuvrability, turning circles) Tactical diameter (transfer at $180^{\circ}$ change of heading) |  | m |
| $y_{0 F}$ | Y0F | (ships, manoeuvrability, stopping manoeuvre) Lateral deviation |  | m |
| $y_{0 \text { max }}$ | Y0MX | (ships, manoeuvrability, turning circles) Maximum transfer |  | m |
| $y_{0 \text { max }}$ | Y0MX | (ships, manoeuvrability, zigzag manoeuvre) Maximum transverse deviation |  | m |
|  |  |  |  |  |

ITTC Symbols
Version 2021
$\mathbf{Y}, \mathbf{y}$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Name | Definition or <br> Symbol | SI- <br> Explanation |
| :--- | :--- | :--- |


|  |  | (ships, hydrostatics, stabil- <br> ity, seakeeping, large ampli- <br> tude motions capsizing) Lat- <br> eral displacement of centre <br> of gravity (YCG) | Lateral distance from a refer- <br> ence point to the centre of <br> gravity, G | m |
| :--- | :--- | :--- | :--- | :--- |
| $y_{\mathrm{D}}$ |  | (seakeeping, large amplitude <br> motions capsizing) Distance <br> of down flooding opening <br> from gunwale |  | m |
| $y_{\mathrm{D}^{\prime}}$ |  | (seakeeping, large amplitude <br> motions capsizing) Distance <br> of down flooding opening <br> off centreline | m |  |
| $y_{\mathrm{F}}$ | YF | (fundamental. coordinate <br> and space related) Flow <br> axes and corresponding <br> Cartesian coordinates | Right-hand orthogonal sys- <br> tem of coordinates fixed in <br> relation to the flow | m |
| $y_{i}$ | $Y(\mathrm{I})$ | (fundamental, statistical) <br> Samples of random quanti- <br> ties | $i=1 \ldots n$ <br> where $n$ : sample size |  |
| $y_{i}$ |  | Estimate of measurand $Y_{i}$ | Estimate of measurand $Y_{i}$ <br> when two or more measur- <br> ands are determined in the <br> same measurement |  |
| $y_{\mathrm{P}}$ | YP | (ships, propulsor geometry) <br> Lateral propeller position | Transverse distance of wing <br> propeller centre from middle <br> line | m |
| $y^{+}$ | (fluid mechanics, boundary <br> layers) Non-dimensional <br> distance from the wall | $u_{\tau} / v$ |  |  |

## ITTC Symbols

Version 2021
Z, z

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Symbol |  | Sxplanation |


| Z | Z, FZ, | (solid body mechanics, loads) Force in direction of body axis z |  | Nm |
| :---: | :---: | :---: | :---: | :---: |
| Z | NPB | (ships, propulsor geometry) Number of propeller blades |  | 1 |
| Z | ZRA | (ships, hydrostatics, stability) Intersection of righting arm with line of action of the centre of buoyancy |  |  |
| Z | FZ | (ships, manoeuvrability, seakeeping) Heave force on body, force along body $z$ axis |  | N |
| Z |  | (sailing vessels) Components of resultant force along designated axis |  | N |
| Z | ZRA | (seakeeping, large amplitude motions capsizing) Intersection of righting arm with line of action of the centre of buoyancy |  |  |
| Z |  | (seakeeping, large amplitude motions capsizing) Vertical distance from the centre of A to the centre of the underwater lateral area or approximately to a point at one half the draught - IMO/IS |  | m |
| Z |  | (seakeeping, large amplitude motions capsizing) Vertical distance from the centre of A to the waterline |  | m |
| $Z_{\text {CB }}$ | ZCB | (Ships, Hydrostatics and Stability) <br> Vertical centre of buoyancy | Vertical distance from reference point to the centre of buoyancy, B | m |
| $Z_{\text {CE }}$ | ZCE | (sailing vessels) Height of centre of effort of sails above waterline in vertical centre plane |  | m |
| $\mathrm{Z}_{\mathrm{H}}$ | ZH | (ACV and SES) Vertical spacing between inner and outer side skirt hinges or attachment points to structure | needs clarification | m |

ITTC Symbols
Version 2021
Z, z

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Eymbol |  | SI- <br> Explanation |


| z | Z | (fundamental. coordinate and space related) Body axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in the body | m |
| :---: | :---: | :---: | :---: | :---: |
| z | Z | (fundamental, time and frequency domain quantity) Complex variable |  |  |
| z | ZSURF | (environmental mechanics, wind) Height above the sea surface in meters |  | m |
| z | NPB | (ships, propulsor geometry)Number of propeller blades |  | 1 |
| z | Z | (ships, unsteady propeller forces) Cartesian coordinates | Origin O coinciding with the centre of the propeller. The longitudinal $x$-axis coincides with the shaft axis, positive forward; the trans-verse $y$ axis, positive to port; the third, $z$-axis, positive upward | m |
| $z_{0}$ | Z0 | (fundamental. coordinate and space related) Space axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the space, | m |
| $z_{6}$ |  | (ships, hull resistance, water jets) Vertical distance of nozzle centre relative to undisturbed surface |  | m |
| $z^{a}$ | ZAM | (fundamental, time and frequency domain quantity) Amplitude | $\bmod (z)=\operatorname{sqrt}\left(z^{r 2}+z^{i 2}\right)$ | m |
| $z^{c}$ | ZRE | (fundamental, time and frequency domain quantity) Real or cosine component | $z^{c}=\operatorname{real}(z)=z^{a} \cos \left(z^{p}\right)$ |  |
| $Z_{\text {D }}$ |  | (seakeeping, large amplitude motions capsizing) Height above waterline of down flooding opening |  | m |
| $z_{\text {F }}$ | ZF | (fundamental. coordinate and space related) Flow axes and corresponding Cartesian coordinates | Right-hand orthogonal system of coordinates fixed in relation to the flow | m |
| $z^{\text {i }}$ | ZIM | (fundamental, time and frequency domain quantity) Imaginary or sine component | $\operatorname{imag}(z)=z^{a} \sin \left(z^{p}\right)=z^{s}$ |  |

## ITTC Symbols

Version 2021
Z, z

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Symbol |  | SI- <br> Explanation |


| $z^{j}$ | ZCJ | (fundamental, time and frequency domain quantity) Conjugate | $z^{r}-i z^{i}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $z^{l}$ | ZLG | (fundamental, time and frequency domain quantity) (Phase) Lag | $-z^{p}$ |  |
| $z^{p}$ | ZPH | (fundamental, time and frequency domain quantity) Phase | $\operatorname{arc}(z)=\operatorname{arctg}\left(z^{i} / z^{r}\right)$ |  |
| ZP | ZP | (ships, propulsor geometry) Vertical propeller position | Height of propeller centre above base line | m |
| $z^{\text {r }}$ | ZRE | (fundamental, time and frequency domain quantity) Real or cosine component | $\operatorname{real}(z)=z^{a} \cos \left(z^{p}\right)=z^{c}$ | 1 |
| $z^{5}$ | ZIM | (fundamental, time and frequency domain quantity) Imaginary or sine component | $z^{s}=\operatorname{imag}(\mathrm{z})=z^{a} \sin \left(z^{p}\right)$ | 1 |
| $z_{S}$ | ZS | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) <br> Mean static sinkage | $\left(z_{\text {SF }}+z_{\text {SA }}\right) / 2$ | m |
| ZSA | ZSA | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Static sinkage at AP | Caused by loading | m |
| ZSF | ZSF | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Static sinkage at FP | Caused by loading | m |
| $Z_{V}$ | ZV | (ships, performance) Running sinkage of model or ship |  | m |
| ZVA | ZVA | (ships, hull resistance) Running sinkage at AP |  | m |
| $z_{\text {VF }}$ | ZVF | (ships, hull resistance) Running sinkage at FP |  | m |
| $z_{V M}$ | ZVM | (ships, hull resistance) Mean running sinkage | $\left(Z_{\mathrm{VF}}+\mathrm{Z}_{\mathrm{VA}}\right) / 2$ | m |


| Version 2021 |  |  | A, $\boldsymbol{\alpha}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or | SI- |
| Symbol | Symbol |  | Explanation | Unit |


| $\alpha$ | AA | (solid body mechanics, rigid body motions) Angular acceleration | $d \omega / d t$ | $\mathrm{rad} / \mathrm{s}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $\begin{array}{\|l} \text { AT } \\ \text { ALFA } \end{array}$ | (solid body mechanics, rigid body motions) Angle of attack | The angle of the longitudinal body axis from the projection into the principal plane of symmetry of the velocity of the origin of the body axes relative to the fluid, positive in the positive sense of rotation about the $y$-axis | rad |
| $\alpha$ | AA, ALFA | (fluid mechanics, lifting surfaces) Angle of attack or incidence | Angle between the direction of undisturbed relative flow and the chord line | rad |
| $\alpha$ | GC | (fluid mechanics, cavitation) Gas content | Actual amount of solved and undissolved gas in a liquid | ppm |
| $\alpha$ | AAPI | (ships, manoeuvrability) <br> Pitch angle | Angle of attack in pitch on the hull | rad |
| $\alpha$ | AA | (ships, propulsor geometry) Angle of inclination of the propeller shaft | Angle between propeller shaft and horizontal | deg |
| $\alpha_{0}$ | $\begin{aligned} & \text { AAZL } \\ & \text { ALF0 } \end{aligned}$ | (fluid mechanics, lifting surfaces) Angle of zero lift | Angle of attack or incidence at zero lift | rad |
| $\alpha_{B}$ | ALFSL | (planing, semi-displacement vessels) Angle of stagnation line | Angle between projected keel and stagnation line in a plane normal to centre plane and parallel to reference line | rad |
| $\alpha_{\text {BAR }}$ | ALFBAR | (planing, semi-displacement vessels) Barrel flow angle | Angle between barrel axis and assumed flow lines | rad |
| $\alpha_{c}$ | ALFTW | (hydrofoil boats) Geometric angle of twist |  | rad |
| $\alpha_{D}$ | AD | (ships, propulsor geometry) Duct profile-shaft axis angle | Angle between nose-tail line of duct profile and propeller shaft | rad |
| $\alpha_{\text {EFF }}$ | $\begin{array}{\|l} \text { AAEF, } \\ \text { ALFE } \end{array}$ | (fluid mechanics, lifting surfaces) <br> Effective angle of attack or incidence | The angle of attack relative to the chord line including the effect of induced velocities | rad |
| $\alpha_{\text {FB }}$ | ANFB | (ships, appendage geometry) Bow fin angle |  | rad |
| $\alpha_{\text {FS }}$ | ANFS | (ships, appendage geometry) <br> Stern fin angle |  | rad |

## ITTC Symbols

Version 2021
A, $\boldsymbol{a}$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Symbol |  | Explanation |


| $\alpha_{G}$ | AAGE, <br> ALFG | (fluid mechanics, lifting surfaces) <br> Geometric angle of attack or incidence | The angle of attack relative to the chord line neglecting the effect of induced velocities | rad |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha_{\mathrm{H}}$ | AAHY, <br> ALFI | (fluid mechanics, lifting surfaces) Hydrodynamic angle of attack | In relation to the position at zero lift | rad |
| $\alpha_{\text {I }}$ | $\begin{aligned} & \text { AAID, } \\ & \text { ALFS } \end{aligned}$ | (fluid mechanics, lifting surfaces) Ideal angle of attack | For thin airfoil or hydrofoil, angle of attack for which the streamlines are tangent to the mean line at the leading edge. This condition is usually referred to as "shockfree" entry or "smooth" | rad |
| $\alpha_{\text {IND }}$ | ALFIND | (hydrofoil boats) Downwash or induced angle |  | rad |
| $\alpha_{M}$ | ALFM | (hydrofoil boats) Angle of attack of mean lift coefficient for foils with twist |  | rad |
| $\alpha_{\text {S }}$ | GS | (fluid mechanics, cavitation) Gas content of saturated liquid | Maximum amount of gas solved in a liquid at a given temperature | ppm |
| $a_{\text {s }}$ | GR | (fluid mechanics, cavitation) Gas content ratio | $\alpha / \alpha_{s}$ | 1 |
| $\alpha_{\text {s }}$ | AFS | (hydrofoil boats) Angle of attack for which flow separation (stall) occurs |  | rad |
| $\alpha_{\text {то }}$ | ATO | (hydrofoil boats) Incidence angle at take-off speed |  | rad |

ITTC

Symbol $\quad$\begin{tabular}{llll}
Computer <br>
Symbol

$\quad$ Name $\quad$

Definition or <br>
Explanation

$\quad$

SI- <br>
Unit
\end{tabular}

| $\beta$ | $\begin{array}{\|l\|} \hline \mathrm{DR} \\ \mathrm{BET} \end{array}$ | (solid body mechanics, rigid body motions) Angle of drift or side-slip | The angle to the principal plane of symmetry from the velocity vector of the origin of the body axes relative to the fluid, positive in the positive sense of rotation about the $z$-axis | rad |
| :---: | :---: | :---: | :---: | :---: |
| $\beta$ | BETE | (fluid mechanics, boundary layers) <br> Equilibrium parameter | $\delta^{*} /\left(\tau_{w} d p / d x\right)$ | 1 |
| $\beta$ | BETD | (planing, semi-displacement vessels) <br> Deadrise angle of planing bottom | Angle between a straight line approximating body section and the intersection between basis plane and section plane | rad |
| $\beta$ | APSF | (ships, performance) Appendage scale effect factor | Ship appendage resistance divided by model appendage resistance | 1 |
| $\beta$ | AADR | (ships, manoeuvrability) Drift angle | Angle of attack in yaw on the hull | rad |
| $\beta$ | BETB | (ships, propulsor performance) Advance angle of a propeller blade section | $\operatorname{arctg}\left(V_{\mathrm{A}} / R \omega\right)$ | rad |
| $\beta_{\text {C }}$ | DRCI | (ships, manoeuvrability, turning circles) Drift angle at steady turning |  | rad |
| $\beta_{\text {D }}$ | BD | (ships, propulsor geometry) Diffuser angle of duct | Angle between inner duct tail line and propeller shaft | rad |
| $\beta_{\mathrm{I}}$ | BETI | (ships, propulsor, performance) Hydrodynamic flow angle of a propeller blade section | Flow angle taking into account induced velocity | rad |
| $\beta_{\mathrm{L}}$ | BETAL | (sailing vessels) leeway angle |  | rad |
| $\beta_{\mathrm{M}}$ | BETM | (planing, semi-displacement vessels) Deadrise angle at midship section |  | rad |
| $\beta_{\text {T }}$ | BETT | (planing, semi-displacement vessels) Dead rise angle at transom |  | rad |
| $\beta_{\text {WA }}$ | BETWA | (environmental mechanics, wind, sailing vessels) apparent wind angle (relative to boat course) |  | rad |

## ITTC Symbols

| Version 2021 |  |  |  | $\boldsymbol{B}, \boldsymbol{\beta}$ |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Eymbol | Symbol |


| $\beta_{\mathrm{WR}}$ | ANWIRL | (ships, manoeuvrability) <br> Angle of attack of relative <br> wind |  | rad |
| :--- | :--- | :--- | :--- | :--- |
| $\beta_{\mathrm{WT}}$ | BETWT | (environmental mechanics, <br> wind, sailing vessels) True <br> wind angle (relative to ves- <br> sel course) | rad |  |
| $\beta^{*}$ | BETS | (ships, propulsor perfor- <br> mance) Effective advance <br> angle | $\operatorname{arctg}\left(V_{\mathrm{A}} /(0.7 R \omega)\right)$ | rad |


| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$| Name |  | Definition or <br> Explanation |
| :--- | :--- | :--- |


| $\Gamma$ | CC | (fluid mechanics, flow fields) Circulation | $\int V d s$ along a closed line | $\mathrm{m}^{2} / \mathrm{s}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\Gamma$ | VD | (fluid mechanics, flow fields) Vortex density | Strength per length or per area of vortex distribution | m/s |
| $\Gamma^{\mathrm{n}}$ | CN | (fluid mechanics, flow fields) Normalized circulation | $\Gamma /(\pi D V)$ <br> $\pi$ is frequently omitted | 1 |
| $\gamma$ | MR | (ships, basic quantities) Relative mass or weight, in English speaking called specific gravity | Mass density of a substance divided by mass density of distilled water at $4^{\circ} \mathrm{C}$ | 1 |
| $\gamma$ | RO GAMR | (solid body mechanics, rigid body motions) Projected angle of roll or heel | The angular displacement about the $x_{0}$ axis of the principal plane of symmetry from the vertical, positive in the positive sense of rotation about the $\mathrm{X}_{0}$ axis | rad |
| $\gamma$ | ANSW | (fluid mechanics, lifting surfaces) Sweep angle |  | rad |
| $\gamma_{1}$ |  | (ships, propulsor performance) Resistance fraction for one propeller | The portion of the resistance (load fraction, $\gamma_{1}$ ) that the $\mathrm{i}^{\text {th }}$ propeller is responsible for | 1 |

Version 2021
$\Delta, \delta$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $\Delta$ | DISPF | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Displacement (buoyant) force | $g \rho \nabla$ | N |
| :---: | :---: | :---: | :---: | :---: |
| $\Delta_{\text {APP }}$ | DISPFAP | (ships, hull geometry) Displacement force (buoyancy) of appendages | $g \rho \nabla_{\mathrm{AP}}$ | N |
| $\Delta_{\text {BH }}$ | DISPFBH | (ships, hull geometry) Displacement force (buoyancy) of bare hull | $g \rho \nabla_{\mathrm{BH}}$ | N |
| $\Delta C_{\text {F }}$ | DELCF | (ships, hull resistance) <br> Roughness allowance |  | 1 |
| $\Delta_{\text {c }}$ | DFCAN | (sailing vessels) Displacement force (weight) of canoe body |  | N |
| $\Delta_{\mathrm{K}}$ | DFK | (sailing vessels) Displacement force (weight) of keel |  | N |
| UM | DMF | Change of momentum flux |  | N |
| $\Delta \bar{M}_{x}$ |  | (ships, hull resistance, water jets) Change in Momentum Flux in $x$ direction |  | N |
| $\Delta_{m}$ | DISPM | (ships, hull geometry, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Displacement mass | $\rho \nabla$ | kg |
| $\Delta R_{\text {waves }}$ | DRWA | (ships, ship performance) <br> Added waves resistance |  | N |
| $\Delta R_{\text {wind }}$ | DRWI | (ships, ship performance) <br> Added wind resistance |  | N |
| $\Delta_{\text {R }}$ | DFR | (sailing vessels) Displacement force (weight) of rudder |  | N |
| $\Delta_{U}$ | UDEF | (fluid mechanics, boundary layers) Velocity defect in boundary layer | $\left(U_{\mathrm{e}}-U\right) / u_{\tau}$ | 1 |
| $\Delta w$ | DELW | (ships, performance) Shipmodel correlation factor for wake fraction | $w_{T, \mathrm{M}}-w_{T, \mathrm{~S}}$ | 1 |
| $\Delta w \mathrm{C}$ | DELWC | (ships, performance) Shipmodel correlation factor with respect to $w_{T, S}$ method formula of ITTC 1978 method |  | 1 |

Version 2021

| ITTC | Computer |  |  |  |
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| Symbol | Symbol | Name | Definition or <br> Explanation | SI- <br> Sit |


| $\delta$ | DELTT | (fluid mechanics, lifting surfaces) Thickness ratio of foil section (general) | $t / c$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\delta$ | ADCT | (ships, propulsor performance) <br> Taylor's advance coefficient | $n D / V_{\mathrm{A}}$ with $n$ in revs $/ \mathrm{min}, D$ in feet, $V_{\mathrm{A}}$ in kn | 1 |
| $\delta$ | D | (ships, hydrostatics, stability) Finite increment in... | Prefix to other symbol | 1 |
| $\delta$ |  | (seakeeping, large amplitude motions capsizing) Tank block coefficient |  | 1 |
| $\delta$ | ANCS | (ships, manoeuvrability) Angle of a control surface, rudder angle, helm angle |  | rad |
| $\delta$ | ANRU | (ships, manoeuvrability) Rudder angle, helm angle |  | rad |
| $\delta_{0}$ | ANRU0 | (ships, manoeuvrability) Neutral rudder angle |  | rad |
| $\delta_{1}$ | DELS | (fluid mechanics, boundary layers) Displacement thickness of boundary layer | $\int\left(U_{\mathrm{e}}-U\right) / U_{\mathrm{e}} d y$ | m |
| $\delta 995$ | DEL | (fluid mechanics, boundary layers) Thickness of a boundary layer at $U=0.995 U_{\mathrm{e}}$ |  | m |
| $\delta B_{\mathrm{C}}$ | DBCV | (ACV and SES) Increase in cushion breadth due to water contact |  | m |
| $\delta_{\text {FB }}$ | ANFB | (ships, manoeuvrability) Bow fin angle |  | rad |
| $\delta_{\text {B }}$ | DELTB | (fluid mechanics, lifting surfaces) Thickness ratio of trailing edge of struts | $t_{\mathrm{B}} / \mathrm{Cs}$ | 1 |
| $\delta_{\mathrm{C}}$ | HC | (fluid mechanics, cavitation) Cavity height or thickness | Maximum height of a fullydeveloped cavity, normal to the surface and the stream-wise direction of the cavity | m |
| $\delta_{i j}$ | DEL(I,J) | (fundamental. coordinate and space related) Delta operator | $\begin{gathered} +1: i j=11,22,33 \\ 0: \text { if otherwise } \end{gathered}$ |  |
| $\delta_{\text {EFF }}$ | ANRUEF | (ships, manoeuvrability) Effective rudder inflow angle |  | rad |

ITTC Symbols
Version 2021
$\Delta, \delta$

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $\delta_{\mathrm{F}}$ | DELTF | (fluid mechanics, lifting sur- <br> faces) Camber ratio of mean <br> line (general) | $f / c$ | 1 |
| :--- | :--- | :--- | :--- | :--- |
| $\delta_{\mathrm{F}}$ | DELFS | (ships, appendage geometry) <br> Flap angle (general) | Angle between the planing <br> surface of a flap and the bot- <br> tom before the leading edge |  |
| $\delta_{\mathrm{FB}}$ | ANFB | Bow fin angle | rad |  |
| $\delta_{\mathrm{FL}}$ | DLTFL | (fluid mechanics, lifting sur- <br> faces) <br> Angle of flap deflection |  | rad |
| $\delta_{\mathrm{FR}}$ | ANFR | (ships, appendage geometry) <br> Flanking rudder angle |  | rad |
| $\delta_{\mathrm{FRin}}$ | ANFRIN | (ships, appendage geometry) <br> Assembly angle of flanking <br> rudders | Initial angle set up during <br> the assembly as zero angle <br> of flanking rudders | rad |
| $\delta_{\mathrm{FS}}$ | ANFS | (ships, manoeuvrability) <br> Stern fin angle |  | rad |
| $\delta_{\mathrm{I}}$ | ELIC | (environmental mechanics, <br> ice) Deflection of ice sheet | Vertical elevation of ice sur- <br> face | m |
| $\delta_{\mathrm{L}}$ | DELTL | (fluid mechanics, lifting sur- <br> faces) Camber ratio of lower <br> side of foil | $f_{L} / c$ | c |

Version 2021
$\Delta, \delta$

| ITTC | Computer |
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| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
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| $\delta t_{\mathrm{KL}}$ | DTR | (ships, hydrostatics, stability, seakeeping, large amplitude motions capsizing) Change in static trim |  | m |
| :---: | :---: | :---: | :---: | :---: |
| $\delta_{\mathrm{U}}$ | DELTU | (fluid mechanics, lifting surfaces) Camber ratio of upper side | $f_{u} / c$ | 1 |
| $\delta_{u}$ | DP(U) | (ships, unsteady propeller forces) Generalized vibratory displacement | $\begin{aligned} & u=1, . ., 6 \\ & u=1,2,3: \text { linear } \\ & u=4,5,6: \text { angular } \end{aligned}$ | $\begin{aligned} & \mathrm{M} \\ & \mathrm{~m} \\ & \mathrm{rad} \end{aligned}$ |
| $\delta_{\text {w }}$ | DELWG | (ships, appendage geometry) Wedge angle | Angle between the planing surface of a wedge and the bottom before the leading edge | rad |
| $\delta_{\lambda}$ | DLAM | (planing, semi-displacement vessels) Dimensionless increase in total friction area | Effective increase in friction area length-beam ratio due to spray contribution to drag | 1 |
| $\delta^{*}$ | DELS | (fluid mechanics, boundary layers) Displacement thickness of boundary layer | $\int\left(U_{\mathrm{e}}-U\right) / U_{\mathrm{e}} d y$ | m |
| $\delta^{* *}$ | ENTH | (fluid mechanics, boundary layers) Energy thickness | $\int\left(U / U_{\text {e }}\left(1-U^{2} / U_{\mathrm{e}}{ }^{2}\right) d y\right.$ | m |
| $\dot{\delta}_{u}$ | DPVL(U) | (ships, unsteady propeller forces) Generalized vibratory velocity | $\begin{aligned} & u=1, . ., 6 \\ & u=1,2,3: \text { linear } \\ & u=4,5,6: \text { angular } \end{aligned}$ | $\begin{aligned} & \mathrm{m} / \mathrm{s} \\ & \mathrm{~m} / \mathrm{s} \\ & \mathrm{rad} / \mathrm{s} \end{aligned}$ |
| $\ddot{\delta}_{u}$ | DPAC(U) | (ships, unsteady propeller forces) Generalized vibratory acceleration | $\begin{aligned} & u=1, . ., 6 \\ & u=1,2,3: \text { linear } \\ & u=4,5,6: \text { angular } \end{aligned}$ | $\begin{aligned} & \mathrm{m} / \mathrm{s}^{2} \\ & \mathrm{~m} / \mathrm{s}^{2} \\ & \mathrm{rad} / \mathrm{s}^{2} \end{aligned}$ |


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| Explanation |$\quad$| SI- |
| :--- |
| Unit |


| $\varepsilon$ | EPSLD | (fluid mechanics, lifting surfaces) Lift-Drag ratio | L/D | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\varepsilon$ | EPSG | (ships, hull resistance) Resistance-displacement ratio in general | $R / 4$ | 1 |
| $\varepsilon$ | PSIBP | (ships, propulsor geometry) <br> Propeller axis angle measured to body fixed coordinates | Angle between reference line and propeller shaft axis | rad |
| $\varepsilon_{\mathrm{F}}$ | EPSLDF | (hydrofoil boats) <br> Lift/ Drag ratio of foil | $L / D$ | 1 |
| $\varepsilon_{i}$ | EWPH(I) | Phases of harmonic components of a periodic wave | $\eta^{\text {ESp }}$ | rad |
| $\varepsilon_{i j k}$ | EPS(I,J,K) | (fundamental. coordinate and space related) Epsilon operator | $\begin{aligned} & +1: i j k=123,231,312 \\ & -1: i j k=321,213,132 \\ & 0: \end{aligned}$ |  |
| $\varepsilon_{\text {I }}$ | STIC | (environmental mechanics, ice) Ice strain | Elongation per unit length | 1 |
| $\varepsilon_{\mathrm{R}}$ | EPSR | (ships, hull resistance) Residuary resistancedisplacement ratio | $R_{\mathrm{R}} / \Delta$ | 1 |
| $\varepsilon_{\text {SH }}$ | EPSSH | (planing, semi-displacement vessels) Shaft angle | Angle between shaft line and reference line (positive, shaft inclined downwards) | rad |
| $\varepsilon_{\text {WL }}$ | EPSWL | (planing, semi-displacement vessels) Wetted length factor | $L_{\mathrm{M}} / L_{\text {WL }}$ | 1 |
| $\varepsilon$ ws | EPSWS | (planing, semi-displacement vessels, ACV and SES) Wetted surface area factor, wetted surface factor |  | 1 |
| $\dot{\varepsilon}$ I | STRTIC | (environmental mechanics, ice) Ice strain rate | $\partial \varepsilon / \partial \tau$ | 1/s |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $\zeta$ |  | (fundamental, statistical, <br> stochastic) Outcome of a <br> random "experiment" |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\zeta$ | DW | (environmental mechanics, <br> waves) Instantaneous wave <br> depression | Z-axis positive vertical <br> down, zero at mean water <br> level | m |
| $\zeta_{13}$ | ZETA13 | (ships, hull resistance, <br> water jets) Inlet duct loss <br> coefficient: | $\frac{E_{3}-E_{1}}{\frac{1}{2} \rho U_{0}^{2}}$ | 1 |
| $\zeta_{57}$ | ZETA57 | (ships, hull resistance, water <br> jets) Nozzle duct loss <br> coefficient: | $\frac{E_{7}-E_{5}}{\frac{1}{2} \rho \bar{u}_{\text {e6 }}}$ | 1 |
| $\zeta_{\mathrm{A}}$ | WAMP | (environmental mechanics, <br> waves) Wave amplitude | Radius of orbital motion of a <br> surface wave particle | m |
| $\zeta_{\mathrm{C}}$ | (ACV and SES) Height of <br> cushion generated wave <br> Zabove mean water plane at <br> leading edge side of the skirt | m |  |  |
| $\zeta_{i j}$ | ZETAC <br> (ships, hull resistance, water <br> jets) Energy loss coefficient <br> between station $i$ and $j$ | 1 |  |  |

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $\eta$ | EW | (ships, hull resistance, environmental mechanics, waves) <br> Instantaneous wave elevation at a given location | $z$-axis positive vertical up, zero at mean water level; | m |
| :---: | :---: | :---: | :---: | :---: |
| $\eta$ | EF, ETA | (ships, basic quantities) Efficiency | Ratio of powers |  |
| $\eta_{0}$ |  | (ships, hull resistance, water jets) Free stream efficiency: | $\eta_{\mathrm{P}} \eta_{\text {duct }} \eta_{\mathrm{I}}$ | 1 |
| $\eta_{\text {APP }}$ | ETAAP | (ships, performance) Appendage efficiency | $P_{\text {EwoApp }} / P_{\text {Ewapp }}, R_{\text {TBH }} / R_{\text {T }}$ | 1 |
| $\eta^{a}{ }_{i}$ | EWAM(I) | (environmental mechanics, waves) Amplitudes of harmonic components of a periodic wave | $\eta^{\text {FSa }}$ | m |
| $\eta_{\mathrm{B}}$ | $\begin{array}{\|l} \text { ETAB, } \\ \text { EFTP } \end{array}$ | (ships, performance) Propeller efficiency behind ship | $P_{\mathrm{T}} / P_{\mathrm{D}}=T V_{\mathrm{A}} /(Q \omega)$ | 1 |
| $\eta \mathrm{C}$ | EC | (environmental mechanics, waves) Maximum of elevations of wave crests in a record |  | m |
| $\eta_{\text {D }}$ | ETAD, EFRP | (ships, performance, hull resistance, water jets) Propulsive efficiency or quasi-propulsive coefficient | $P_{\mathrm{E}} / P_{\mathrm{D}}=P_{\mathrm{R}} / P_{\mathrm{P}}$ | 1 |
| $\eta_{\text {Did }}$ | ETADID | (ships, performance) Propulsive efficiency in ideal condition, from model test |  | 1 |
| $\eta_{\text {duct }}$ |  | (ships, hull resistance, water jets) Ducting efficiency: | $\frac{P_{\mathrm{JSE}}}{P_{\mathrm{PE}}}$ | 1 |
| $\eta_{\text {el }}$ |  | (ships, hull resistance, water jets) Energy interaction efficiency: | $\frac{P_{\mathrm{JSE0}}}{P_{\mathrm{JSE}}}$ | 1 |
| $\eta_{\mathrm{G}}$ | ETAG, EFGP | (ships, performance, basic quantities) Gearing efficiency |  | 1 |
| $\eta_{\mathrm{H}}$ | ETAH, EFRT | (ships, performance) <br> Hull efficiency | $\begin{aligned} & P_{\mathrm{E}} / P_{\mathrm{T}}=P_{\mathrm{R}} / P_{\mathrm{T}} \\ & =(1-t) /(1-w) \end{aligned}$ | 1 |
| $\eta_{\text {I }}$ | EFID | (ships, propulsor performance) Ideal propeller efficiency | Efficiency in non-viscous fluid | 1 |

Version 2021

| ITTC | Computer |
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| $\eta_{\text {I }}$ |  | (ships, hull resistance, water jets) Ideal efficiency, equivalent to jet efficiency in free stream conditions | $\frac{P_{\text {TE0 }}}{P_{\mathrm{JSE} 0}}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\eta_{\text {ID }}$ | EFDIC | (ice going vessels) Propulsive efficiency in ice | $R_{\text {IT }} V /\left(2 \pi n_{\text {IA }} Q_{\text {IA }}\right)$ | 1 |
| $\eta_{\text {ICE }}$ | ERIC | (ice going vessels) Relative propulsive efficiency in ice | $\eta_{\text {ID }} / \eta_{\text {D }}$ | 1 |
| $\eta_{\text {INT }}$ |  | (ships, hull resistance, water jets) Total interaction efficiency: | $\frac{\eta_{\mathrm{eI}}}{\eta_{\mathrm{mI}}}(1-t)$ | 1 |
| $\eta_{\text {inst }}$ | ETAIN | (ships, hull resistance, water jets) Installation efficiency to account for the distorted flow delivered by the jet intake to the pump |  | 1 |
| $\eta_{\text {jet }}$ |  | (ships, hull resistance, water jets) Momentum or jet efficiency: | $\frac{P_{\mathrm{TE}}}{P_{\mathrm{JSE}}}$ | 1 |
| $\eta_{\text {JP }}$ | EFJP | (ships, propulsor performance) Propeller pump or hydraulic efficiency | $P_{\mathrm{J}} / P_{\mathrm{D}}=P_{\mathrm{J}} / P_{\mathrm{P}}$ | 1 |
| $\eta_{\text {JP0 }}$ | $\begin{aligned} & \text { ZET0, } \\ & \text { EFJP0 } \end{aligned}$ | (ships, propulsor performance) <br> Propeller pump efficiency at zero advance speed, alias static thrust coefficient | $T /(\rho \pi / 2)^{1 / 3} /\left(P_{\mathrm{D}} D\right)^{2 / 3}$ | 1 |
| $\eta_{\text {Js }}$ |  | (ships, hull resistance, water jets) Jet system efficiency: | $\frac{P_{\mathrm{JSE}}}{P_{\mathrm{D}}}$ | 1 |
| $\eta_{\mathrm{M}}$ | ETAM | Mechanical efficiency of transmission between engine and propeller | $P_{\mathrm{D}} / P_{\text {B }}$ | 1 |
| $\eta_{\text {mI }}$ |  | (ships, hull resistance, water jets) Momentum interaction efficiency: | $\frac{T_{\text {net0 }}}{T_{\text {net }}}$ | 1 |
| $\eta$ о | ETAO, EFTPO | (ships, propulsor performance, performance) Propeller efficiency in open water | $P_{\mathrm{T}} / P_{\mathrm{D}}=T V_{\mathrm{A}} /(Q \omega)$ all quantities measured in open water tests | 1 |
| $\eta_{\mathrm{P}}$ | ETAP | (ships, performance) <br> Propulsive efficiency coefficient | $P_{\mathrm{E}} / P_{\mathrm{B}}$ | 1 |
| $\eta_{\mathrm{P}}$ | ETAP | (ships, hull resistance, water jets) Pump efficiency | $\frac{P_{\mathrm{PE}}}{P_{\mathrm{D}}}$ | 1 |

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
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| $\eta_{\mathrm{P} 0}$ |  | (ships, hull resistance, water <br> jets) Pump efficiency from a <br> pump loop test |  | 1 |
| :--- | :--- | :--- | :--- | :--- |
| $\eta^{p_{i}, \varepsilon_{i}}$ | EWPH(I) | (environmental mechanics, <br> waves) Phases of harmonic <br> components of a periodic <br> wave | $\eta^{\mathrm{FS}}$ | rad |
| $\eta_{\mathrm{R}}$ | ETAR, <br> EFR0 | (ships, performance) Rela- <br> tive rotative efficiency | $\eta_{\mathrm{B}} / \eta_{0}$ | 1 |
| $\eta_{\mathrm{S}}$ | ETAS, <br> EFPS | (ships, performance) <br> Shafting efficiency | $P_{\mathrm{D}} / P_{\mathrm{S}}=P_{\mathrm{P}} / P_{\mathrm{S}}$ | 1 |
| $\eta_{\mathrm{T}}$ | ET | (environmental mechanics, <br> waves) <br> Wave trough depression | Negative values! | m |
| $\eta_{T}$ | ET | (environmental mechanics, <br> waves) Elevations of wave <br> troughs in a record | Negative values! | m |
| $\eta_{\mathrm{TJ}}$ | EFTJ | (ships, propulsor perfor- <br> mance) Propeller jet effi- <br> ciency | $2 /\left(1+\left(1+C_{T h}\right)^{1 / 2}\right)$ | 1 |
| $\eta_{\mathrm{TP} 0}$ | ETA0, <br> EFTP0 | (ships, propulsor perfor- <br> mance) Propeller efficiency <br> in open water | $P_{\mathrm{T}} / P_{\mathrm{D}}=T V_{\mathrm{A}} /(Q \omega)$ all <br> quantities measured in open <br> water tests | 1 |


| ITTC | Computer | Name | Definition or | SI- |
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| Symbol | Symbol | Name | Explanation | Unit |


| $\Theta$ | THETA | (fluid mechanics, boundary layers) Momentum thickness | $\int\left(U / U_{e}\right)\left(1-U / U_{e}\right) d y$ | m |
| :---: | :---: | :---: | :---: | :---: |
| $\theta$ | $\begin{aligned} & \mathrm{X}(5), \mathrm{TR}, \\ & \text { TETP } \end{aligned}$ | (solid body mechanics, rigid body motions) Angle of pitch or trim | Positive in the positive sense of rotation about the $y$-axis | rad |
| $\theta$ | CWD | (environmental mechanics, waves) Component wave direction |  | rad |
| $\theta$ | PI | (ships, manoeuvrability) Pitch angle |  | rad |
| $\theta$ | RAKA | (ships, propulsor geometry) Angle of rake |  | rad |
| $\theta_{0}$ | TRIMS | (planing, semi-displacement vessels) Static trim angle | Angle between ship design waterline and actual water line at rest (positive bow up) $\tan ^{-1}\left(\left(Z_{\mathrm{SF}}-Z_{\mathrm{SA}}\right) / L\right)$ | rad |
| $\theta_{\text {B }}$ | TETB | (ACV and SES) Bag contact deformation angle |  | rad |
| $\theta_{\text {C }}$ |  | (seakeeping, large amplitude motions capsizing) Capsizing angle under the action of a gust of wind IMO/IS |  | rad |
| $\theta_{\text {D }}$ | TRIMV | (ships, hull resistance, planing, semi-displacement vessels) Running (dynamic) trim angle | Angle between actual water line at rest and running water line (positive bow up) $\tan ^{-1}\left(\left(z_{V F}-Z_{V A}\right) / L\right)$ | rad |
| $\theta_{\text {DH }}$ | DIHED | (hydrofoil boats) Dihedral angle |  | rad |
| $\theta_{\text {DWL }}$ | TRIMDWL | (planing, semi-displacement vessels) Running trim angle based on design waterline | Angle between design waterline and running waterline (positive bow up) | rad |
| $\theta_{\text {Ext }}$ | TEMX | (ships, propulsor geometry) <br> Skew angle extent | The difference between maximum and minimum local skew angle | rad |
| $\theta_{\text {F }}$ | TETF | (ACV and SES) Finger outer face angle |  | rad |
| $\theta_{\mathrm{f}}$ | HEELANGF | (seakeeping, large amplitude motions capsizing) Heel angle at flooding |  | rad |
| $\theta_{\mathrm{m}}$ | MWD <br> THETAMOX | (environmental mechanics, waves) Mean or dominant wave direction |  | rad |
| $\theta_{\text {n }}$ |  | (ships, hull resistance, water jets) Jet angle relative to the |  | rad |


| ITTC | Computer |  | Definition or | SI- |
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| Symbol | Symbol | Name | Explanation | Unit |


|  |  | horizontal at the nozzle (station 6) |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\theta \mathrm{s}$ | TRIMS | (ships, hydrostatics, stability, planing, semi-displacement vessels, seakeeping, large amplitude motions capsizing) Static trim angle | Angle between ship design waterline and actual water line at rest (positive bow up) $\tan ^{-1}\left(\left(Z_{\mathrm{SF}}-Z_{\mathrm{SA}}\right) / L\right)$ | rad |
| $\theta_{\text {s }}$ | TETS | (ships, propulsor geometry) <br> Skew angle | The angular displacement about the shaft axis of the reference point of any blade section relative to the generator line measured in the plane of rotation. It is positive when opposite to the direction of ahead rotation | rad |
| $\theta_{V}$ | TRIMV | (ships, hull resistance, planing, semi-displacement vessels) Running (dynamic) trim angle | Angle between actual water line at rest and running water line (positive bow up) $\tan ^{-1}\left(\left(Z_{V F}-Z_{V A}\right) / L\right)$ | rad |
| $\theta_{\mathrm{w}}$ | TETW | (ACV and SES) Slope of mean water plane for surface level beneath cushion periphery |  | rad |
| $\theta_{\mathrm{W}}$ | TETWI | (environmental mechanics, wind) Wind direction |  | rad |
| $\theta^{*}$ | ENTH | (fluid mechanics, boundary layers) Energy thickness | $f(U / U e)\left(1-U^{2} / U_{e}^{2}\right) d y$ | m |

## ITTC Symbols

Version 2021
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## ITTC Symbols

| Version 2021 |  |  | K, K |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |


| $K$ | K | (fluid mechanics, boundary <br> layers) von Karman constant | 0.41 | 1 |
| :--- | :--- | :--- | :--- | :--- |
| $\kappa$ | CK | (fluid mechanics, flow pa- <br> rameter) Kinematic capillar- <br> ity | $\sigma / \rho$ | $\mathrm{m}^{3} / \mathrm{s}^{2}$ |
| $\kappa$ | WN | (environmental mechanics, <br> waves) Wave number | $2 \pi / L_{\mathrm{W}}=\omega^{2} / g$ | $1 / \mathrm{m}$ |
| $\kappa$ S | KS | (ships, propulsor perfor- <br> mance) Roughness height of <br> propeller blade surface | m |  |


| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Symbol |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $\Lambda$ | AS | (fluid mechanics, lifting surfaces) Aspect ratio | $b^{2} / A$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\Lambda$ | PRGR | (fluid mechanics, boundary layers) Pressure gradient parameter | $\delta_{995} /\left(v d U_{e} / d x\right)$ | 1 |
| 4 |  | Tuning factor | $\begin{aligned} & L_{z}=\frac{w_{E}}{w_{z}} \quad L_{q}=\frac{w_{E}}{w_{q}} \quad L_{f}=\frac{w_{E}}{w_{j}} \\ & L_{z}=\frac{w_{E}}{w_{z}} \quad L_{q}=\frac{w_{E}}{w_{q}} \quad L_{i}=\frac{w_{E}}{w_{j}} \\ & \text { or } \\ & L_{z}=\frac{T_{z}}{T_{E}} \quad L_{q}=\frac{T_{q}}{T_{E}} \quad L_{i}=\frac{T_{i}}{T_{E}} \end{aligned}$ | 1 |
| $\Lambda_{\text {FR }}$ | ASRF | (ships, appendage geometry) <br> Flanking rudder aspect ratio |  | 1 |
| $\Lambda_{\text {R }}$ | ASRU | (ships, appendage geometry, manoeuvrability) Rudder aspect ratio | $b^{2} / A, b_{\mathrm{R}}{ }^{2} / A_{\mathrm{R}}, b_{\mathrm{R}}{ }^{2} / A_{\mathrm{RT}}$ | 1 |
| $\lambda$ | TA | (fluid mechanics, lifting surfaces) Taper ratio | $c_{t} / C_{r}$ | 1 |
| $\lambda$ | SC | (ships, basic quantities, ships, hull geometry) Scale ratio, Linear scale of ship model | Ship dimension divided by corresponding model dimension $\begin{aligned} \lambda & =L_{\mathrm{S}} / L_{\mathrm{M}}=B_{\mathrm{S}} / B_{\mathrm{M}} \\ & =T_{\mathrm{S}} / T_{\mathrm{M}} \end{aligned}$ | 1 |
| $\lambda$ | ADR | (ships, propulsor performance) Advance ratio of a propeller | $V_{\mathrm{A}} /(n D) / \pi=J / \pi$ | 1 |
| $\lambda_{\text {d }}$ | LD | (environmental mechanics, waves) Wave length by zero down-crossing | The horizontal distance between adjacent down crossing in the direction of advance | m |
| $\lambda_{\text {FR }}$ | TAFR | (ships, appendage geometry) <br> Flanking rudder taper |  | 1 |
| $\lambda_{\mathrm{R}}$ | TARU | (ships, appendage geometry) Rudder taper | $c_{R} / c_{T}$ | 1 |
| $\lambda_{u}$ | LU | (environmental mechanics, waves) Wave length by zero up-crossing | The horizontal distance between adjacent up crossing in the direction of advance | m |
| $\lambda_{\mathrm{w}}$ | LW | (environmental mechanics, waves) Wave length | The horizontal distance between adjacent wave crests in the direction of advance | m |
| $\lambda_{W}$ | LAMS | (planing, semi-displacement vessels) Mean wetted lengthbreadth ratio | $L_{\mathrm{M}} /\left(B_{L C G}\right)$ | 1 |


| ITTC | Computer | Name | Definition or | SI- |
| :---: | :---: | :---: | :---: | :---: |
| Symbol | Symbol | Name | Explanation | Unit |


| $\mu$ | VI | (fluid mechanics, flow pa- <br> rameter) Viscosity |  | $\mathrm{kg} / \mathrm{ms}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mu$ | CWD | (environmental mechanics, <br> waves) Component wave di- <br> rection | rad |  |
| $\mu$ | PMVO | (ships, hydrostatics, stabil- <br> ity, seakeeping, large ampli- <br> tude motions capsizing) Vol- <br> umetric permeability | The ratio of the volume of <br> flooding water in a compart- <br> ment to the total volume of <br> the compartment | 1 |
| $\mu$ | (ships, seakeeping) Wave |  |  |  |
| encounter angle |  |  |  |  | | Angle between ship positive |
| :--- |
| x axis and positive direction |
| of waves (long crested) or |
| dominant wave direction |
| (short crested) |$\quad$ rad | POIIC |
| :--- |
| $\mu_{1}$ |
| $\mu_{p}$ |
| $\mu_{x}$ |

## ITTC Symbols

Version 2021

| ITTC | Computer |
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| Symbol |  |$\quad$ Symbol $\quad$| Definition or |
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$\left.\begin{array}{|l|l|l|l|l|}\hline v & \text { VK } & & \begin{array}{l}\text { (fluid mechanics, flow pa- } \\ \text { rameter) Kinematic viscos- } \\ \text { ity }\end{array} & \mu / \rho \\ \hline v & & \begin{array}{l}\text { Degrees of freedom (gen- } \\ \text { eral) }\end{array} & & \mathrm{m}^{2} / \mathrm{s} \\ \hline v_{\text {eff }} & \text { Effective degrees of freedom }\end{array} \begin{array}{l}\text { Effective degrees of freedom } \\ \text { of } u_{c}(y) \text { used to obtain } t_{p}\left(v_{e f f}\right) \\ \text { for calculating expanded un- } \\ \text { certainty } U_{p}\end{array}\right)$

## ITTC Symbols

Version 2021

| $\xi_{n}$ |  | ships, ship performance) <br> Load variation coefficient of <br> the shaft revolution speed |  |
| :--- | :--- | :--- | :--- |
| $\xi_{P}$ | (ships, ship performance) <br> Load variation coefficient of <br> the delivered power | 1 |  |
| $\xi_{V}$ | (ships, ship performance) <br> Load variation coefficient of <br> the ship speed | 1 |  |

## ITTC Symbols

Version 2021
O, 0
ITTC
Symbol
Computer
Name
Definition or
SI-
Symbol
Explanation
Unit


## ITTC Symbols

| Version $\mathbf{2 0 2 1}$ |  |  | $\boldsymbol{\Pi}, \boldsymbol{\pi}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |


| $\pi$ | PI | Circular constant | 3.1415926535 | 1 |
| :--- | :--- | :--- | :--- | :--- |


| Version 2021 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or <br> Eymbol | Symbol |


| $\rho$ | DN, RHO | (fluid mechanics, flow parameter, ships, basic quantities, seakeeping, large amplitude motions capsizing, hull resistance, water jets) Mass density of fluid | $d m / d V$ | $\mathrm{kg} / \mathrm{m}^{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\rho_{0}$ | RHO0 | (ships, basic quantities, sailing vessels) water density for reference water temperature and salt content |  | kg/m3 |
| $\rho_{\text {A }}$ | DNA, RHOA | (Ships, basic quantities, ACV and SES, seakeeping, large amplitude motions capsizing) Mass density of air | Mass of air per unit volume | $\mathrm{kg} / \mathrm{m}^{3}$ |
| $\rho_{\text {I }}$ | DNIC | (environmental mechanics, ice) Mass density of ice | Mass of ice per unit volume | $\mathrm{kg} / \mathrm{m}^{3}$ |
| $\rho_{\text {SN }}$ | DNSN | (environmental mechanics, ice) Mass density of snow | Mass of snow per unit volume | $\mathrm{kg} / \mathrm{m}^{3}$ |
| $\rho_{\mathrm{W}}$ | DNWA | (environmental mechanics, ice) Mass density of water |  | $\mathrm{kg} / \mathrm{m}^{3}$ |
| $\rho_{\Delta}$ | DNWI | (environmental mechanics, ice) Density difference | $\rho_{\Delta}=\rho_{\mathrm{W}}-\rho_{\mathrm{I}}$ | $\mathrm{kg} / \mathrm{m}^{3}$ |


| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Symbol |  | SI- <br> Explanation |


| $\sigma$ | CA | (fluid mechanics, flow parameter) Capillarity | Surface tension per unit length | $\mathrm{kg} / \mathrm{s}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\sigma$ | CNPC | (fluid mechanics, cavitation) Cavitation number | $\left(p_{\mathrm{A}}-p_{\mathrm{C}}\right) / q$ | 1 |
| $\sigma$ | SN, SIGS | (ships, basic quantities) Normal stress |  | Pa |
| $\sigma$ | FC | (environmental mechanics, waves) Circular wave frequency | $2 \pi f_{\mathrm{W}}=2 \pi / T_{\mathrm{W}}$ | rad/s |
| $\sigma$ |  | Standard deviation of a probability distribution | Standard deviation of a probability distribution, equal to the positive square root of $\sigma^{2}$ |  |
| $\sigma_{\text {CI }}$ | SCIC | (environmental mechanics, ice) Compressive strength of ice |  | Pa |
| $\sigma_{\text {FI }}$ | SFIC | (environmental mechanics, ice) Flexural strength of ice |  | Pa |
| $\sigma_{\text {I }}$ | CNPI | (fluid mechanics, cavitation) Inception cavitation number |  | 1 |
| $\sigma_{\text {TI }}$ | SNIC | (environmental mechanics, ice) Tensile strength of ice |  | Pa |
| $\sigma_{\mathrm{V}}$ | CNPV | (fluid mechanics, cavitation) <br> Vapour cavitation number | $\left(p_{\mathrm{A}}-p_{\mathrm{V}}\right) / q$ | 1 |
| $\sigma_{x}$ | XDR | (fundamental, statistical) Standard deviation of a random quantity | $x^{V R^{1 / 2}}$ |  |
| $\sigma_{\theta}$ | DIRSF <br> SIGMAOX | (environmental mechanics, waves) Directional spreading function | $\begin{aligned} & S(f, \theta)=S(f) D \mathrm{x}(f, \theta) \text { where } \\ & \int_{0}^{2 \pi} D_{\mathrm{x}}(f, \theta) d \theta=1 \end{aligned}$ | rad |
| $\sigma(\bar{q})$ |  | Standard deviation of $\bar{q}$ | Standard deviation of $\bar{q}$, equal to the positive root of $\sigma^{2}(\bar{q}) \sigma^{2}(\bar{q})$ |  |
| $\sigma[s(\bar{q})]$ |  | Standard deviation of experimental standard deviation $s(\bar{q})_{s}(\bar{q})$ of $\bar{q}$, equal to the positive square root of $\sigma^{2}[s(\bar{q})] \sigma^{2}[s(\bar{q})]$ |  |  |

## ITTC Symbols

Version 2021
$\Sigma, \sigma$

| ITTC | Computer |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Symbol | Name | Definition or <br> Explanation | SI- <br> Symbol |  |


| $\sigma^{2}$ |  | Variance of a probability | Variance of a probability <br> distribution of (for example) <br> a randomly-variing quantity <br> q, estimated by s $s^{2}\left(q_{k}\right)$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $\sigma^{2}(\bar{q})$ |  | Variance of $\bar{q}$ | Variance of $\bar{q}$, equal to $\sigma^{2} /$ <br> $n$, estimated by <br> $s^{2}(\bar{q})=\frac{s^{2}\left(q_{k}\right)}{n}$ <br> $s^{2}(\bar{q})=\frac{s^{2}\left(q_{k}\right)}{n}$ |  |
| $\sigma^{2}[s(\bar{q})]$ |  | Variance of experimental <br> standard deviation $s(\bar{q})$ of $\bar{q}$ |  |  |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |

\(\left.$$
\begin{array}{|l|l|l|l|l|}\hline \tau & \text { TICV } & \begin{array}{l}\text { (fundamental, statistical, } \\
\text { stochastic) Covariance or } \\
\text { correlation time }\end{array} & & \mathrm{s} \\
\hline \tau & \text { ST, TAU } & \begin{array}{l}\text { (ships, basic quantities) Tan- } \\
\text { gential stress }\end{array} & & \text { Pa } \\
\hline \tau & \text { TMR } & \begin{array}{l}\text { (ships, propulsor perfor- } \\
\text { mance) Ratio between pro- } \\
\text { peller thrust and total thrust } \\
\text { of ducted propeller }\end{array} & T_{\mathrm{P}} / T_{\mathrm{T}} & 1 \\
\hline \tau & \text { TRIMDWL } & \begin{array}{l}\text { (special craft, Planing and } \\
\text { Semi-Displacement Vessels }\end{array}
$$ <br>
Running trim angle based on <br>

design waterline\end{array}\right) ~\)| Angle between design water- |
| :--- |
| line and running waterline |
| (positive bow up) |$\quad$ deg | TAUDWL |
| :--- |
| $\tau_{\mathrm{B}}$ |

## ITTC Symbols

| Version 2021 |  |  | Y, v |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or | SI- |
| Symbol | Symbol |  | Explanation | Unit |



| Version 2021 |  |  | $\boldsymbol{\Phi}, \boldsymbol{\varphi}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| ITTC | Computer | Name | Definition or | SI- |
| Symbol | Symbol |  | Explanation | Unit |


| $\phi$ | HEELANG | (seakeeping, large amplitude motions capsizing) Heel angle |  | rad |
| :---: | :---: | :---: | :---: | :---: |
| $\varphi$ | $\begin{aligned} & \mathrm{X}(4), \mathrm{RO}, \\ & \mathrm{PHIR} \end{aligned}$ | (solid body mechanics, rigid body motions) Angle of roll, heel or list | Positive in the positive sense of rotation about the x -axis | rad |
| $\varphi$ | HEELANG | (ships, hydrostatics, stability) Heel angle |  | rad |
| $\varphi$ | RO | (ships, manoeuvrability) Roll angle |  | rad |
| $\phi 0$ |  | (seakeeping, large amplitude motions capsizing) Heel angle during offset load tests |  | rad |
| $\phi_{0}(\mathrm{PMT})$ |  | (seakeeping, large amplitude motions capsizing) Maximum permitted heel angle during ... |  | rad |
| \$0 (REQ) |  | (seakeeping, large amplitude motions capsizing) Maximum permitted heel angle during ... |  | rad |
| $\phi_{D}$ |  | (seakeeping, large amplitude motions capsizing) Actual down flooding angle according to ... |  | rad |
| $\phi_{\text {D(REQ) }}$ |  | (seakeeping, large amplitude motions capsizing) Required down flooding angle, see... |  | rad |
| $\phi_{\mathrm{DC}}$ |  | (seakeeping, large amplitude motions capsizing) Down flooding angle to non-quick draining cockpits |  | rad |
| $\phi_{\text {DH }}$ |  | (seakeeping, large amplitude motions capsizing) Down flooding angle to any main access hatchway |  | rad |
| $\phi_{\text {F }}$ | HEELANGF | (ships, hydrostatics, stability seakeeping, large amplitude motions capsizing) Heel angle at flooding |  | rad |
| $\phi_{\text {Gzmax }}$ |  | (seakeeping, large amplitude motions capsizing) Angle of heel at which maximum righting moment occurs |  | rad |

Version 2021
$\Phi, \varphi$

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |


| $\phi_{\mathrm{m}}$ |  | Heel angle corresponding to <br> the maximum of the statical <br> stability curve |  | rad |
| :--- | :--- | :--- | :--- | :--- |
| $\phi_{\mathrm{R}}$ |  | (seakeeping, large amplitude <br> motions capsizing) Assumed <br> roll angle in a seaway |  | rad |
| $\phi_{\mathrm{vs}}$ | HEELANGV | (ships, hydrostatics, stabil- <br> ity) Heel angle for vanishing <br> stability |  | rad |
| $\phi_{\mathrm{w}}$ | PHIP | (seakeeping, large amplitude <br> motions capsizing) Heel an- <br> gle due to calculation wind | (ships, propulsor geometry) <br> Pitch angle of screw propel- <br> ler | arctg $(P /(2 \pi R))$ |

## ITTC Symbols

Version 2021
$\mathbf{X}, \chi$

| ITTC | Computer | Name | Definition or | SI- |
| :--- | :--- | :--- | :--- | :--- |


| $\chi$ | YX | Yaw angle |  | rad |
| :--- | :--- | :--- | :--- | :--- |

## ITTC Symbols

Version 2021

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $\psi$ | $\begin{aligned} & \mathrm{X}(6), \mathrm{YA}, \\ & \text { PSIY } \end{aligned}$ | (solid body mechanics, rigid body motions, ships, manoeuvrability) Angle of yaw, heading or course | Positive in the positive sense of rotation about the z -axis | rad |
| :---: | :---: | :---: | :---: | :---: |
| $\psi$ | SF | (fluid mechanics, flow fields) Stream function | $\psi=$ const <br> is the equation of a stream surface | $\mathrm{m}^{3} / \mathrm{s}$ |
| $\Psi_{\text {O }}$ | YAOR | (ships, manoeuvrability) Original course |  | rad |
| $\psi_{01}$ | PSI01 | (ships, manoeuvrability, zigzag man..) First overshoot angle |  | rad |
| $\psi_{02}$ | PSI02 | (ships, manoeuvrability, Zigzag man..) Second overshoot angle |  | rad |
| $\psi^{\text {ap }}$ | PSIAP | (ships, propulsor geometry) Propeller axis angle measured to space fixed coordinates | Angle between horizontal plane and propeller shaft axis | rad |
| $\psi^{\text {bP }}$ | PSIBP | (ships, propulsor geometry) Propeller axis angle measured to body fixed coordinates | Angle between reference line and propeller shaft axis | rad |
| $\psi_{\text {C }}$ | COCU | (ships, manoeuvrability) Course of current velocity |  | rad |
| $\psi$ s | PSIS | (ships, manoeuvrability, zigzag man..) Switching value of course angle |  | rad |
| $\psi^{\text {WA }}$ | COWIAB | (ships, manoeuvrability) Absolute wind direction |  | rad |
| $\psi_{\text {WR }}$ | COWIRL | (ships, manoeuvrability) Relative wind direction |  | rad |


| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| $\omega$ | FC, OMF | (ships, basic quantities) Cir- <br> cular frequency | $2 \pi f$ | $1 / \mathrm{s}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\omega$ | V0, OMN | (ships, basic quantities) Ro- <br> tational velocity | $2 \pi n$ | $\mathrm{rad} / \mathrm{s}$ |
| $\omega$ | V0P | (ships, propulsor perfor- <br> mance) Propeller rotational <br> velocity | $2 \pi n$ | $1 / \mathrm{s}$ |
| $\omega_{\mathrm{E}}$ | FE | (environmental mechanics, <br> waves) Circular wave fre- <br> quency of encounter | $2 \pi f_{\mathrm{E}}=2 \pi / T_{\mathrm{E}}$ | $\mathrm{rad} / \mathrm{s}$ |
| $\omega_{\mathrm{W}}$ | FC | (environmental mechanics, <br> waves) Circular wave fre- <br> quency | $2 \pi f_{\mathrm{W}}=2 \pi / T_{\mathrm{W}}$ | $\mathrm{rad} / \mathrm{s}$ |
| $\omega_{x}$ | P, OMX, | (solid body mechanics, rigid <br> body motions) Rotational ve- <br> locity around body axis $x$ | $\mathrm{rad} / \mathrm{s}$ |  |
| $\omega_{y}$ | $\mathrm{Q}, \mathrm{OMY}$, <br> V0(2), V(5) | (solid body mechanics, rigid <br> body motions) Rotational <br> velocity around body axis $y$ | $\mathrm{rad} / \mathrm{s}$ |  |
| $\omega_{z}$ | R, OMZ, <br> V0(3), V(6) | (solid body mechanics, rigid <br> body motions) Rotational ve- <br> locity around body axis |  | $\mathrm{rad} / \mathrm{s}$ |

## ITTC Symbols

Version 2021

| ITTC | Computer <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- | Name $\quad$| Definition or |
| :--- |
| Explanation |


| $\nabla$ | DISPVOL | (ships, hull geometry, hydro- <br> statics, stability,) Displace- <br> ment volume | $\Delta /(\rho g)=\nabla_{\mathrm{BH}}+\nabla_{\mathrm{AP}}$ | $\mathrm{m}^{3}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\nabla_{\mathrm{APP}}$ | DISPVAP | (ships, hull geometry) Dis- <br> placement volume of ap- <br> pendages | $\Delta_{\mathrm{AP}} /(\rho \mathrm{g})$ | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{BH}}$ | DISPVBH | (ships, hull geometry) Dis- <br> placement volume of bare <br> hull | $\Delta_{\mathrm{BH}} /(\rho \mathrm{g})$ | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{C}}$ | DVCAN | (sailing vessels) Displaced <br> volume of canoe body |  | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{F}}$ | DISVF | (hydrofoil boats) Foil dis- <br> placement volume |  | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{fw}}$ | DISVOLFW | (ships, hydrostatics, stabil- <br> ity) Displacement volume of <br> flooded water | $\Delta f_{\mathrm{w}} /(\rho g)$ | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{K}}$ | DVK | (sailing vessels) Displaced <br> volume of keel |  | $\mathrm{m}^{3}$ |
| $\nabla_{\mathrm{R}}$ | DVR | (sailing vessels) Displaced <br> volume of rudder | $\mathrm{m}^{3}$ |  |

## ITTC Symbols

Version 2021
Identifiers (Subscripts)

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- |$\quad$| Definition or |
| :--- |
| Explanation |$\quad$| SI- |
| :--- |

$\left.\begin{array}{|l|l|l|l|l|}\hline 0 & & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) Initial }\end{array} & & \\ \hline \text { A } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) attained }\end{array} & & \\ \hline \text { a } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) apparent }\end{array} & & \\ \hline \text { AB } & \begin{array}{l}\text { (ships, hull geometry) After } \\ \text { body }\end{array} & & \\ \hline \text { AP } & \begin{array}{l}\text { (ships, hull geometry) After } \\ \text { perpendicular }\end{array} & & \\ \hline \text { APP } & \begin{array}{l}\text { (ships, hull geometry) Ap- } \\ \text { pendages }\end{array} & & \\ \hline \text { att } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) attained }\end{array} & & \\ \hline \text { BH } & \begin{array}{l}\text { (ships, hull geometry) Bare } \\ \text { hull }\end{array} & & \\ \hline \text { BK } & \begin{array}{l}\text { (ships, appendage geometry) } \\ \text { Bilge keel }\end{array} & & \\ \hline \text { BS } & \begin{array}{l}\text { (ships, appendage geometry) } \\ \text { Bossing }\end{array} & & \\ \hline \text { D } & \begin{array}{l}\text { (ships, propulsor geometry) } \\ \text { Duct }\end{array} & & \\ \hline \text { d } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) dynamic }\end{array} & & \\ \hline \text { DW } & \begin{array}{l}\text { (ships, hull geometry) De- } \\ \text { sign waterline }\end{array} & & \\ \hline \text { dyn } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) dynamic }\end{array} & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) effective }\end{array} & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) effective }\end{array} & \begin{array}{l}\text { (ships, hull geometry) Entry } \\ \text { (spacing }\end{array} \\ \hline \text { e } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) false }\end{array} & \begin{array}{l}\text { (ships, hull geometry) Fore } \\ \text { (sody }\end{array} & \begin{array}{l}\text { (ships, appendage geometry) } \\ \text { Bow foil }\end{array} & \\ \hline \text { (ships, hull geometry) Fore } \\ \text { perpendicular }\end{array}\right)$

## ITTC Symbols

Version 2021
Identifiers (Subscripts)

| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |$\quad$| SI- |
| :--- |

$\left.\begin{array}{|l|l|l|l|l|}\hline \text { FS } & & \begin{array}{l}\text { (ships, appendage geometry) } \\ \text { Stern foil }\end{array} & & \\ \hline \text { FW } & \begin{array}{l}\text { (ships, hull resistance) Fresh } \\ \text { water }\end{array} & & \\ \hline \text { HE } & \text { (ships, hull geometry) Hull } & & \\ \hline \text { KL } & \begin{array}{l}\text { (ships, appendage geometry) } \\ \text { Keel }\end{array} & & \\ \hline \text { KL } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) keel line }\end{array} & & \\ \hline \text { L } & \begin{array}{l}\text { (ships, hydrostatics, stabil- } \\ \text { ity) longitudinal }\end{array} & & \\ \hline \text { LR } & \begin{array}{l}\text { (ships, hull geometry) Refer- } \\ \text { ence Line }\end{array} & & \\ \hline \text { LP } & \begin{array}{l}\text { (ships, hull geometry) Based } \\ \text { on Lpp }\end{array} & & \\ \hline \text { LW } & \begin{array}{l}\text { (ships, hull geometry) Based } \\ \text { on LwL }\end{array} & & \\ \hline \text { M } & \begin{array}{l}\text { (General) Model }\end{array} & \\ \hline \text { (ships, hydrostatics, stabil- } \\ \text { ity) maximum }\end{array} \quad \begin{array}{l}\text { (ships, hull resistance) } \\ \text { Faired model data }\end{array}\right)$

## ITTC Symbols

Version 2021
Identifiers (Subscripts)

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |



| ITTC | Computer |
| :--- | :--- | :--- | :--- | :--- |
| Symbol |  |$\quad$| Symbol |
| :--- | :--- | :--- |$\quad$ Name $\quad$| Definition or |
| :--- |
| Explanation |



## ITTC Symbols

Version 2021
Operators (Superscripts)

| ITTC | Computer | Name | Definition or <br> Symbol | Symbol |
| :--- | :--- | :--- | :--- | :--- |


| RR |  | (fundamental, statistical, <br> stochastic) Population corre- <br> lation |  |  |
| :--- | :--- | :--- | :--- | :--- |
| RS | (fundamental, statistical, <br> stochastic) Sample correla- <br> tion |  |  |  |
| V | (fundamental, statistical, <br> stochastic) Population vari- <br> ance |  |  |  |
| VR | (fundamental, statistical, <br> stochastic) Population vari- <br> ance |  |  |  |
| VS | (fundamental, statistical, <br> stochastic) Sample variance |  |  |  |

